

**Digital Design and Implementation of  
Narrowband IoT Physical Downlink Shared  
Channel Receiver Chain**

**3GPP REL. 14**

**“NPDSCH RX R14”**

*Authors:*

**Hesham Khaled Abdel-Latif**

**Mohamed Ammar Mohamed**

**Reem Saleh Elshawarby**

**Youssef Ahmed Mohamed Galal**

**Youssef Taha Esmail**

*Supervised by:*

**Dr. Hassan Mostafa**

Cairo University

Faculty of Engineering

Department of Electronics and Digital Communications

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# Abstract

Narrowband Internet of Things (NB-IoT) is a new cellular technology introduced in 3GPP Release 13 for providing wide-area coverage for the IoT devices. This thesis provides a hardware implementation of the physical downlink shared channel “NPDSCH” receiver chain in Release 14. We describe how algorithms were constructed and hardware designed in accordance with the requirements of the 3GPP standard to achieve specifications and good performance, low area, low power and low complexity of design. We also provide insight on how the chain was integrated, synthesized, simulated and tested.

## Abbreviations

<b>3GPP</b>	3rd Generation Partnership Project
<b>AWGN</b>	Additive White Gaussian Noise
<b>BER</b>	Bit Error Rate
<b>CBER</b>	Channel Bit Error Rate
<b>CP</b>	Cyclic Prefix
<b>CDF</b>	Cumulative Density Function
<b>CFO</b>	Carrier Frequency Offset
<b>CORDIC</b>	Coordinate Rotation Digital Computer
<b>ETU</b>	Extended Typical Urban
<b>FFO</b>	Fractional Frequency Offset
<b>ICI</b>	Inter-Carrier Interference
<b>IFO</b>	Integer Frequency Offset
<b>ISI</b>	Inter-Symbol Interference
<b>NPSS</b>	Narrowband Primary Synchronization Signal
<b>PMF</b>	Probability Mass Function
<b>RF</b>	Radio Frequency
<b>SINR</b>	Signal to Interference Noise Ratio
<b>SNR</b>	Signal to Noise Ratio
<b>CRC</b>	Cyclic Redundancy Code or Cyclic Redundancy Check
<b>FFT</b>	Fast Fourier Transform
<b>IFFT</b>	Inverse Fast Fourier Transform
<b>IoT</b>	Internet of Things
<b>LTE</b>	Long-Term Evolution
<b>MSB</b>	Most Significant Bit
<b>NB-IoT</b>	Narrowband Internet of Things
<b>NPBCH</b>	Narrowband Physical Broadcast Channel
<b>NPDCCH</b>	Narrowband Physical Downlink Control Channel

**NPDSCH** Narrowband Physical Downlink Shared Channel

**NPRACH** Narrowband Physical Random-Access Channel

**NPSS** Narrowband Primary Synchronization Signal

**NPUSCH** Narrowband Physical Uplink Shared Channel

**NRS** Narrowband Reference Signal

**NSSS** Narrowband Secondary Synchronization Signal

**OFDM** Orthogonal Frequency-Division Multiplexing

**QPSK** Quadrature Phase-Shift Keying

**RE** Resource Element

**TBS** Transport Block Size

**UE** User Equipment

**WAVA** Wrap Around Viterbi Algorithm

**Z-F** Zero-Forcing

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## 1.1. Motivation and Purpose

The number of wireless devices is rapidly increasing. So, we want to connect these devices together to able to develop useful applications. This connectivity can be done through IoT.

The main concept of IoT is to have a network of wireless devices to collect and exchange data between them over the internet or any communication network. IoT doesn't require the device, software or sensor to be connected to public internet it should only be connected to a specific network and can be addressed.

There is a lot of IoT applications such smart cities, traffic management, smart metering and many more.

These IoT devices and network should follow certain specifications, as the devices should be of low cost and long battery life and the network should support low latency and coverage requirements for wide area.

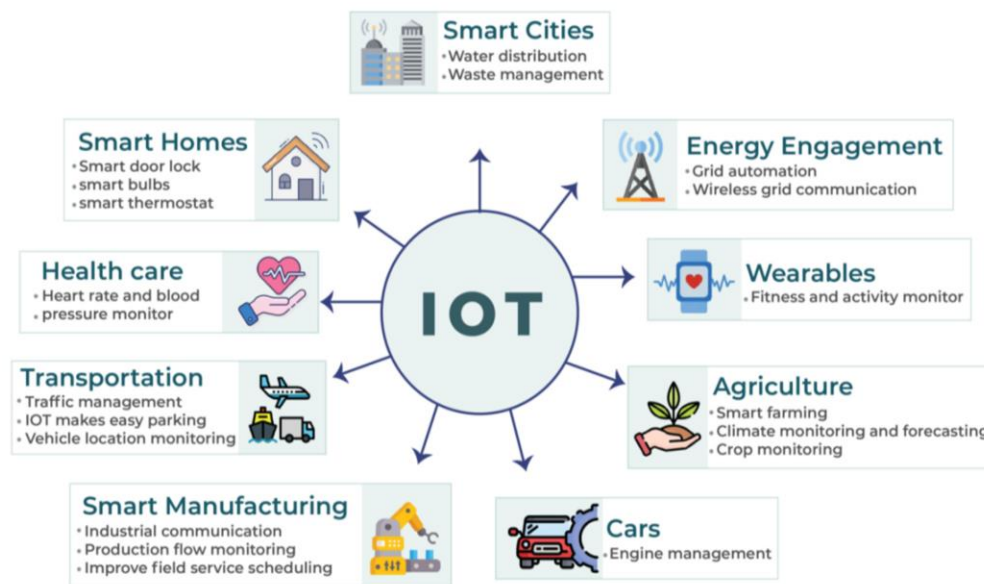


Figure [1]: IoT Applications

NB-IoT is a new mobile network that only used for IoT applications and it's based on LTE. NB-IoT supports a range of data rate depending on the channel quality and the bandwidth besides it offers energy saving capabilities to increase battery life and it support.

It is designed to achieve the perfect co-existence performance along with other technologies. For NB-LTE Rel.14 it works with one resource block occupying a bandwidth of 180 KHz.

NB-IoT is designed to support three deployment modes

1. Standalone mode

An NB-IoT carrier is deployed independently of any LTE carrier and it can function as replacement for GSM carrier. Besides it also provides deployment flexibility based on spectrum availability.

2. Guard band

An NB-IoT carrier is deployed within the guard band of an LTE carrier by using a used Resource Block within LTE carrier Guard Band. This doesn't consume any capacity from the primary LTE traffic carrier

3. In band

An NB-IoT carrier is deployed occupying a physical resource block (PRB) within an LTE carrier. This mode is the most efficient one as it allows the base station schedule to multiplex LTE and NB-IoT traffic in the same spectrum.

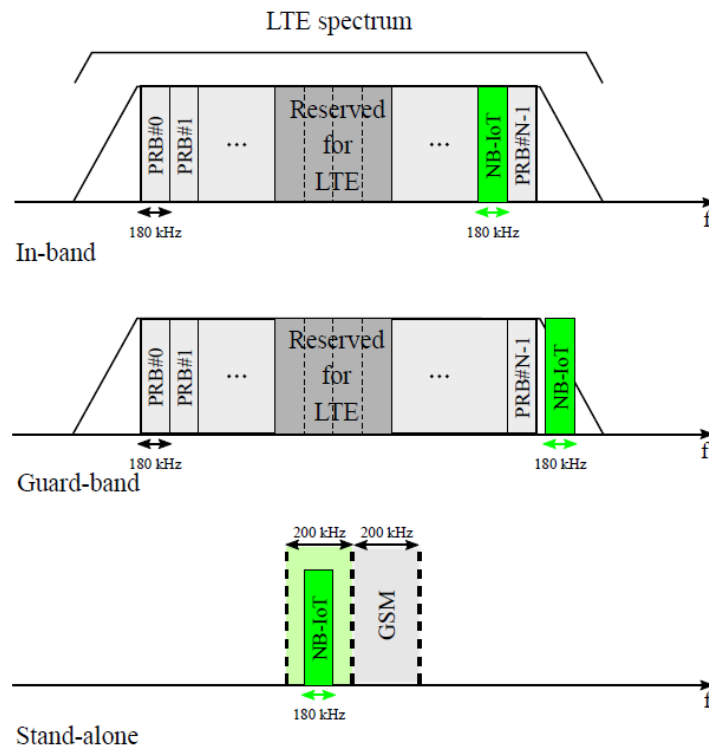


Figure [2]: NB-IoT deployment modes

## 1.2. NB-IoT with Competitors

Low Power Wide Area Network LPWAN connects wireless devices designed for Internet of Things IoT and manages to combine efficient energy devices with wide transmission ranges so they can run for a very long time on battery-based systems.

There are three famous technology nodes using LPWA, NB-IoT, Long Range Wide Area Network (LoRaWAN) and Sigfox.



So, what makes NB-IoT special? NB-IoT is based on Long Term Evolution LTE, so that makes it an open standard not proprietary as LoRaWAN and Sigfox so they are used in.

NB-IoT is also a leading technology in terms of data throughput, data rates and energy efficiency. As the chart shows. LoRaWAN suffers from interference in ISM band which reduces data rates while Sigfox connection is lost in poor conditions.

Typical data rate (bits per second)

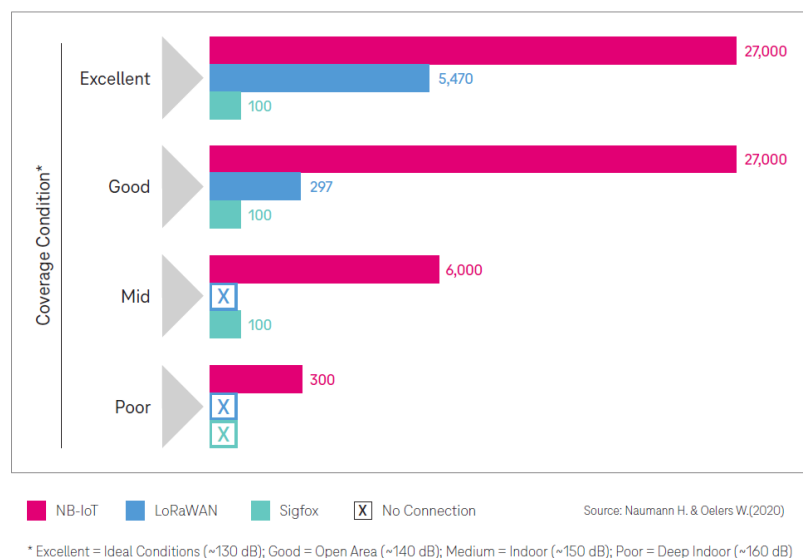


Figure [3]: Data Rates Comparison

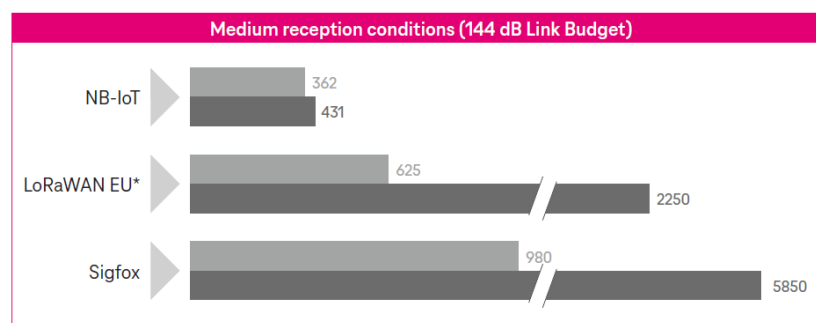


Figure [4]: Energy Efficiency Comparisons

### 1.3. NPDSCH Receiver based on Rel14. 3GPP

3GPP first introduced the NB-LTE in release 13 and further enhancements were made later in release 14 to improve the Quality-of-Service QoS. And also increased the transport block size up to 2536 bits instead of being 680 in release 13.

## 1.4. OFDM

Orthogonal Frequency Division Multiplexing (OFDM) is a method of data transmission in which information is split among several closely spaced narrowband subchannel frequencies instead of using wide band frequency channel.

The spacing is precisely chosen so as to provide orthogonality which gives us immunity to interference and letting the demodulators blind to any other frequency than the intended one.

### 1.4.1. Cyclic Prefix

As we need to be more immune to fading effects so, we need to cancel the Inter Symbol Interference (ISI). This is done by adding a guard time. This time is chosen larger than the expected delay spread in order to a multipath component of one symbol can interfere with the next symbol.

Making this guard time consists of no signal give us a problem which is Inter Carrier Interference (ICI). ICI is the crosstalk between different subcarrier meaning that we lost orthogonality.

We eliminate this ICI by making OFDM symbols cyclically extended in the guard time by this we maintain the orthogonality by ensuring that delayed replicas of the OFDM symbol always have integer number of cycles within the FFT interval.

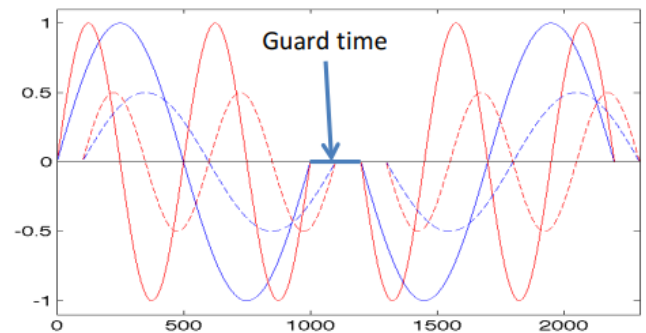


Figure [5]: Guard Time

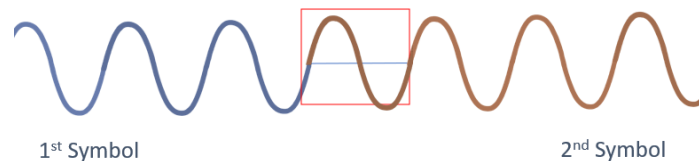


Figure [6]: Guard Time with CP

### 1.4.2. Advantages of OFDM

- OFDM efficiently deals with multipath fading as for a given delay spread the complexity is significantly lower than that of single carrier system.
- Data rates and number of subcarriers can adaptively change according to channel quality.
- Unlike FDM there is no guard bands here so it gives better spectral utilization

### 1.4.3. Disadvantages of OFDM

With all the previous advantages OFDM offers some challenges to be solved as it very sensitive to frequency offset and doppler shifts. Hence, we need to correct these offsets to able to use OFDM reliably.

## 1.5. System Overview

### 1.5.1. Transmission Modes

LTE Supports 3 types of frame structures

- Type 1 for Frequency Division Duplex (FDD)
- Type 2 for Time Division Duplex (TDD)
- Type 3 for LAA secondary cell operation

The main difference between FDD and TDD is that FDD uses different frequency bands for the uplink and downlink transmission while TDD uses the same frequency band but with time slots dedicated for uplink and other for downlink transmission.

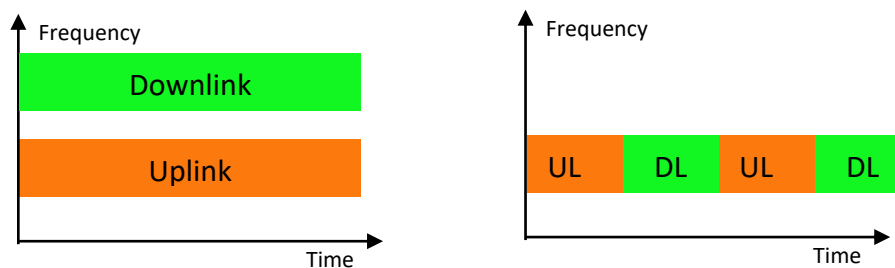


Figure [7]: Frequency/Time Division Duplex Structure

In NB-IoT, frame structure type 1 is used, here is a closer look on how NB-IoT uplink and downlink transmission takes place.

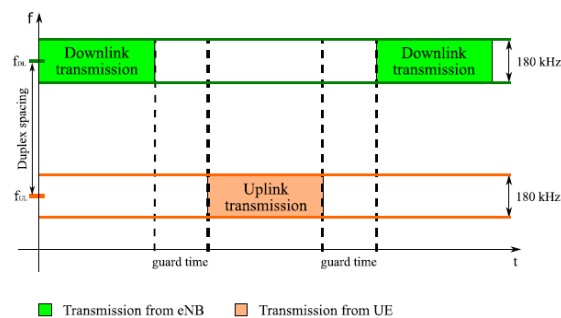


Figure [8]: UL/DL in NB-IoT

### 1.5.2. Frame Structure

Each NB-IoT radio frame has duration of 10 ms and consists of 10 subframes with 1 ms duration each. Every subframe consists of 2 slots of 0.5 ms each. The slot consists of 7 OFDM symbols. And the frequency band of 180 kHz is divided into 12 sub carriers of 15 kHz each.

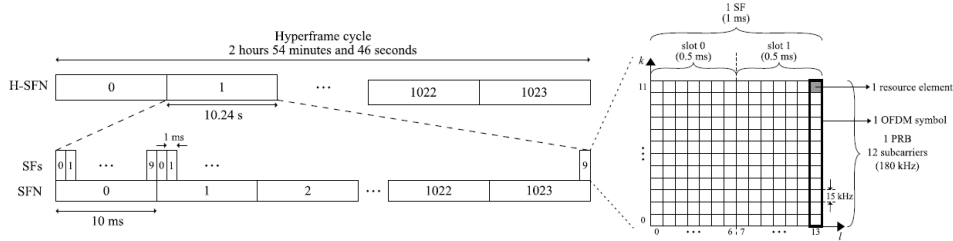
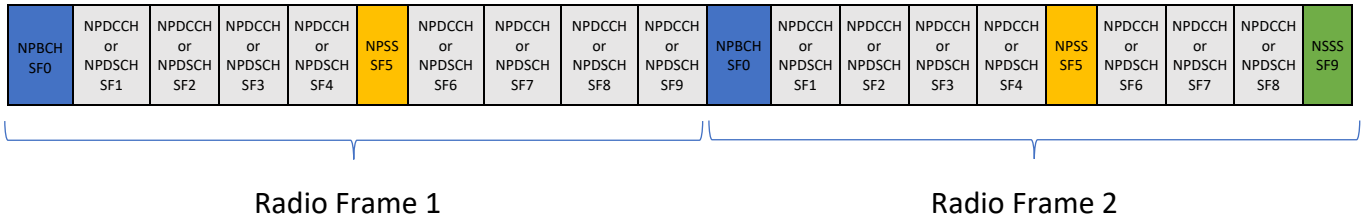


Figure [9]: Frame Structure

There are subframes that carries different types of information such as the broadcast subframes and the Control Subframes the synchronization subframes such as the Narrowband Primary Synchronization Signal NPSS and the Narrowband Secondary Synchronization Signal NSSS.



According to 3GPP

$$\text{Frame time } T_f = 307200T_s = 10\text{ms}, T_{\text{subframe}} = 30720T_s = 1\text{ms}$$

$$T_s = \frac{1}{15000 \times 2048} \text{ms}$$

$$T_{cp} = 5.2 \mu\text{s} \text{ for } 1^{\text{st}} \text{ OFDM symbol and } 4.7 \mu\text{s} \text{ for the rest}$$

$$T_u = \frac{1}{15K} = 66.67 \mu\text{s} \text{ and } T_{\text{symbol}} = \frac{1\text{ms}}{14} = 71.4 \mu\text{s}$$

Number of samples for cp = 160 for the first OFDM symbol and 144 for the rest. So, the minimum number of samples used in LTE is 128 to get integer number of samples for cp = 10 for the first OFDM symbol and 9 for the rest.

For NB-IoT LTE it follows the number of minimum samples which is 128 although its number of subcarriers is 12. Hence, we use down sampler in our design from 128 to 16.

$$\text{So, the sampling rate } T_s = \frac{1}{(15000)(128)} = \frac{1\text{ms}}{1.92} = 520\text{ns}$$



### 1.5.3. Scheduling in NPDSCH

Scheduling is handled by the downlink control information DCI. In case of not carrying system information block SIBs-NB the NPDSCH carries user data towards the UE and it takes place after transmission of NPDCCH in order for the receiver to be able to decode the DCI.

The DCI of the NPDSCH is DCI format type N1 for CRC not masked with RA-RNTI which is random access response and it consists of:

Field	Number of bits	Description
Flag for format N0/format N1 differentiation	1	0 for N0, 1 for N1
Subcarrier order indicator	1	
Scheduling delay $I_{delay}$	3	indicates the start of the codeword
Resource Assignment $I_{SF}$	3	indicates the number of subframes
Modulation and coding scheme $I_{MCS}$	4	indicates the transport block size
Repetition number $I_{Rep}$	4	indicates the number of repetitions
New data indicator	1	
HARQ-Ack resource	4	
DCI subframe repetition number	2	
<b>Total number of bits</b>	<b>23</b>	

#### 1. Scheduling delay $I_{delay}$

The scheduling delay is indicating the start of the codeword successive subframes after  $n + 5 + k_o$  subframes, the NPDCCH that ends in n subframes so usually the NPDSCH follows the NPDCCH after 5 or more subframes.

$I_{delay}$	$k_o$	
	$R_{max} < 128$	$R_{max} \geq 128$
0	0	0
1	4	16
2	8	32
3	12	64
4	16	128
5	32	256
6	64	512
7	128	1024

2. Resource Assignment  $I_{SF}$

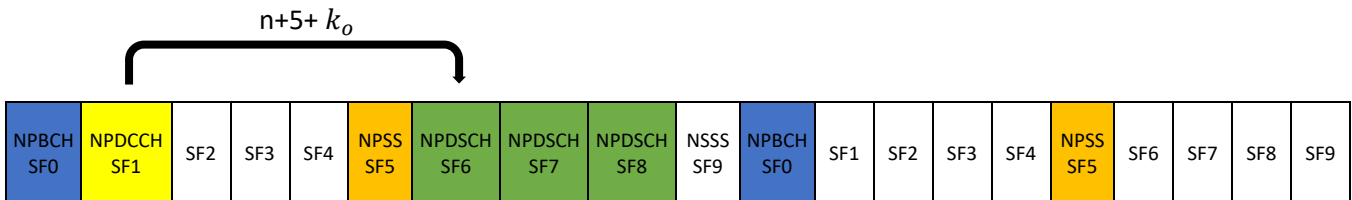
The resource assignment indicates the number of subframes that is constituting the NPDSCH message.

$I_{SF}$	$N_{SF}$
0	1
1	2
2	3
3	4
4	5
5	6
6	8
7	10

Example:

$$I_{delay} = 0, k_o = 0$$

$$I_{SF} = 2, N_{SF} = 3$$



3. Modulation and coding scheme  $I_{MCS}$

The modulation and coding scheme in case of NPDSCH not carrying system information block SIBs-NB is the same as  $I_{TBS}$  where  $I_{TBS} = I_{MCS}$  indicates the transport block size that is used in transmission and it is an important parameter in order to decode the data correctly and hand it over from the physical layer to upper layer. There's no segmentation in NB-IoT because the maximum TBS is 2536 which is less than 6144.

$I_{TBS}$	$I_{SF}$							
	0	1	2	3	4	5	6	7
0	16	32	56	88	120	152	208	256
1	24	56	88	144	176	208	256	344
2	32	72	144	176	208	256	328	424
3	40	104	176	208	256	328	440	568
4	56	120	208	256	328	408	552	680
5	72	144	224	328	424	504	680	872
6	88	176	256	392	504	600	808	1032
7	104	224	328	472	584	680	968	1224
8	120	256	392	536	680	808	1096	1352
9	136	296	456	616	776	936	1256	1544

10	144	328	504	680	872	1032	1384	1736
11	176	376	584	776	1000	1192	1608	2024
12	208	440	680	904	1128	1352	1800	2280
13	224	488	744	1032	1256	1544	2024	2536

4. Repetition number  $I_{Rep}$

The repetition number indicates the number of repetitions of the codeword.

$I_{Rep}$	$N_{Rep}$
0	1
1	2
2	4
3	8
4	16
5	32
6	64
7	128
8	192
9	256
10	384
11	512
12	768
13	1024
14	1536
15	2048

## 1.6. Project Flow

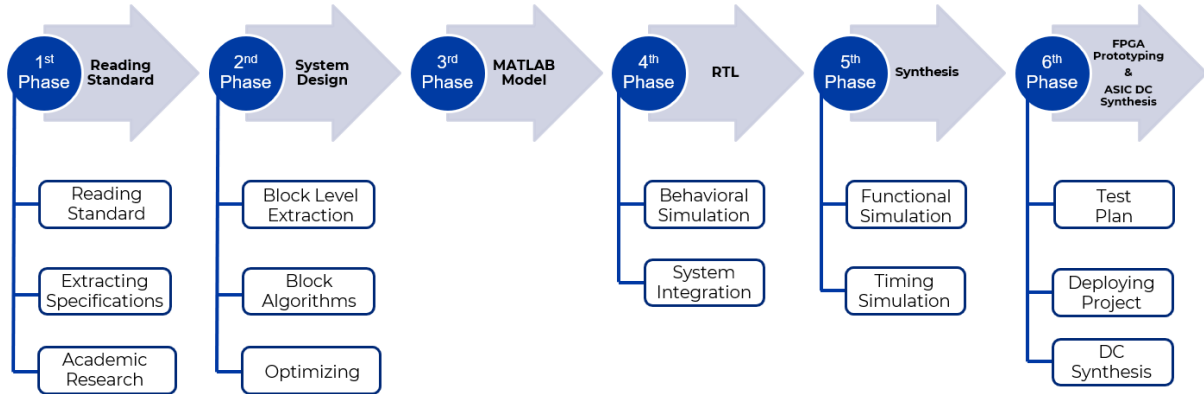


Figure [10]: Project Flow

## 1.7. Design Architecture

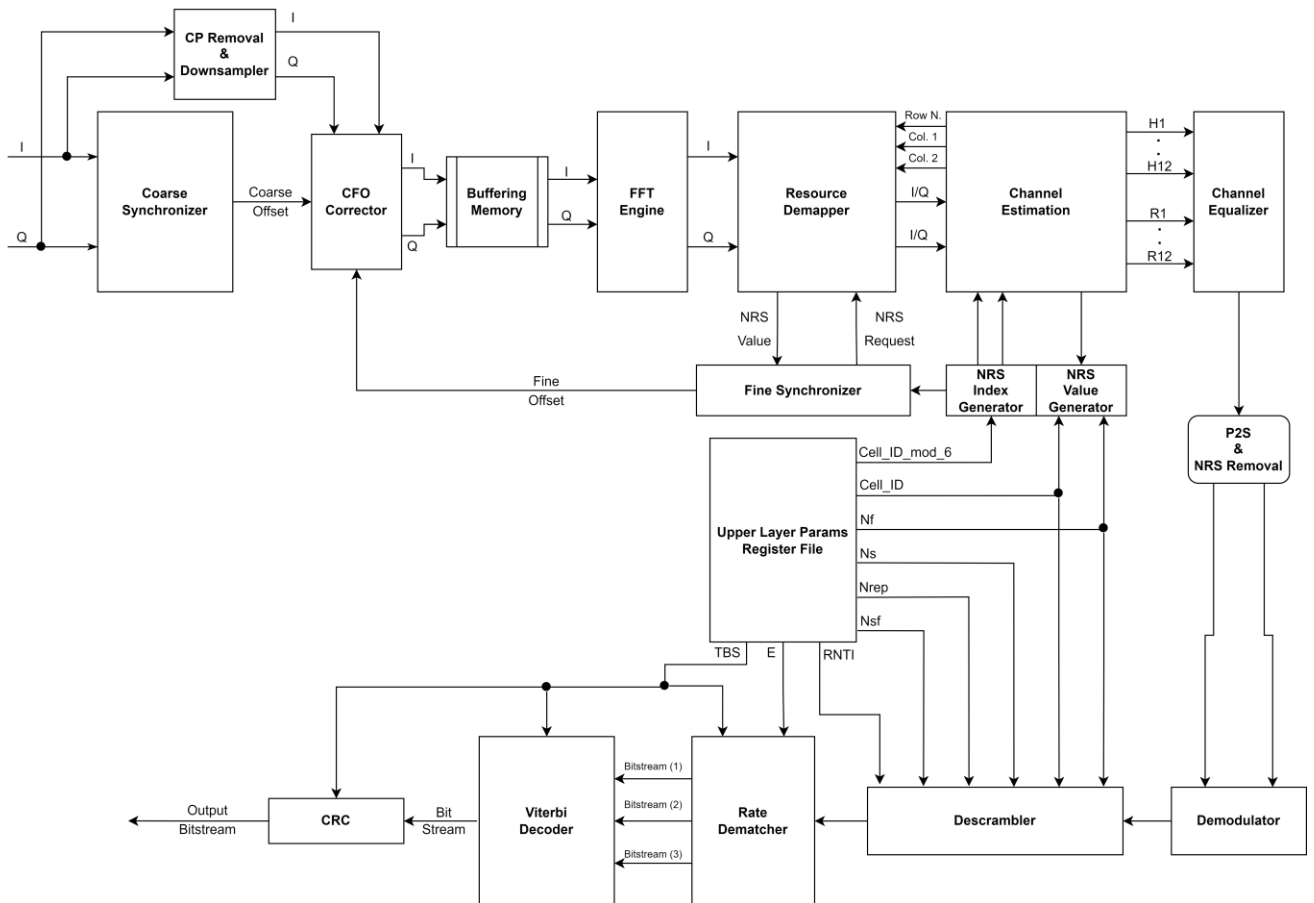


Figure [11]: NPDSCH Rx Chain Block Diagram

The in-phase and quadrature phase data enter the receiver chain through the Coarse Synchronizer.

After the synchronization happens, we remove the cyclic prefix using CP Removal and we down sample the data.

Then these data pass through CFO Corrector to correct the frequency offset using the estimated frequency offset given by the Coarse Synchronizer.

Fine Synchronization is used to keep tracking of time and frequency offset.

There is a FIFO based memory used to store samples to prepare them for the FFT which will transform these samples from time domain to frequency domain.

The Resource Demapper then stores the QPSK symbols output from the FFT till it has a full subframe. It is used to ensure storing the subframe constant during processing time.

The Channel Estimation then extracts the pilots from the subframe using NRS Index Generator and with the use of NRS Value Generator it tries to estimate the channel effect and send these estimates to the Channel Equalizer to compensate this effect.

Data then pass through the Parallel to Serial and NRS Remove block to remove the pilots and convert the parallel to serial data stream.

This QPSK symbol stream consists of real and imaginary data pass through the demodulator to convert it into bits based on the constellation then goes to the descrambler to restore the scrambled data at transmitter.

The bit stream finally goes through the Rate De-matcher to improve the channel efficiency by changing the code rate of the transmitted data.

Then data pass through the Viterbi decoder which is used to decode the data encoded in convolutional code at the transmitter side then finally reach CRC block to get an acknowledgement signal.

### 2.1. Coarse Synchronizer

#### 2.1.1. Problem Definition

OFDM based systems faces two challenging problems, ICI (Inter-Carrier Interference) and ISI (Inter-Symbol Interference). ICI problem arises from the basic assumption of the subcarrier orthogonality, this assumption means that the spectrum of an arbitrary signal on an arbitrary subcarrier must have nulls at all other subcarriers. Thus, a frequency offset introduced from the channel will inevitably introduce ICI as shown in figure (12).

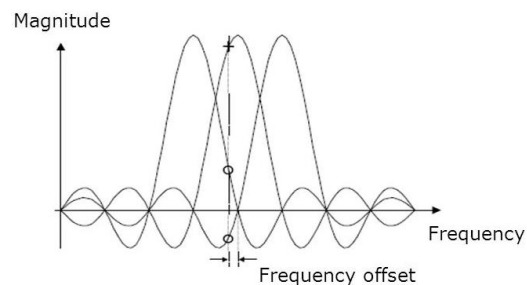


Figure [12]: ICI Frequency Offset

ISI problem isn't exclusive for OFDM based systems, as it takes place when two symbols interfere with each other in time domain because of multipath propagation dispersion, poor pulse shaping at the transmitter or a synchronization error at the receiver. Both problems cause a degradation in the overall system performance and SINR. Thus, these problems will be addressed later in order to solve them.

#### 2.1.2. Frequency & Time Offsets

Regarding ICI, it has two main sources;

1<sup>st</sup> source is Carrier Frequency Offset (CFO) which is the difference between the carrier frequency at the transmitter and the RF oscillators at the receiver. CFO can take a value up to 18KHz assuming a maximum mismatch of 20ppm between the transmitter and receiver oscillators and a carrier frequency around 900 MHz.

2<sup>nd</sup> source is the raster offset. When a UE turns on it conducts a search in frequency domain looking for a carrier to facilitate the synchronization process, referred to as "anchor carrier", this carrier is searched for on a 100 KHz raster, so the offset between the 100 KHz raster and the center frequency of the anchor carrier is defined as the raster offset. the NB-IoT's cell search and acquisition are designed for the UE to be able to synchronize having up to 7.5KHz raster offset. Assuming that sampling oscillator and carrier oscillator are unified, thus, Sampling Frequency Offset (SFO) will be accounted for if we considered the CFO.

Thus, the total maximum frequency offset is assumed to be  $\pm 25.5$  KHz.

Considering ISI, for this context, perfect pulse shaping is assumed; also, it is assumed that the cyclic prefix (CP) is longer than the multipath channel’s maximum excess tap delay. Thus, errors in estimating the beginning of symbols in the synchronization process are the source of ISI of interest in this context.

### 2.1.3. Operating Environment & Conditions

Due to coverage enhancement in the 14th release of 3GPP on NB-IoT, the minimum SNR when assuming a maximum coupling loss of 164dB is -12.6dB in a guard-band or an in-band deployment. The multipath fading channel is modeled by the Extended Typical Urban (ETU) model, which is considered the worst-case channel, having 9 taps with a maximum excess tap delay of 5 us and a maximum Doppler frequency of 5 Hz due to the stationary nature of the applications of NB-IoT.

### 2.1.4. Narrowband Synchronization Signal (NPSS)

The NPSS is a subframe that is sent along every NB-IoT frame and used by the devices to achieve synchronization, in both time and frequency, to an NB-IoT cell. The NPSS needs to be designed so that it is detectable even with a very large frequency offset. Because of the consideration of device complexity required for NPSS detection, all the cells in an NB-IoT network uses the same NPSS. figure (13) below shows the NPSS signal within NB-IoT frame.

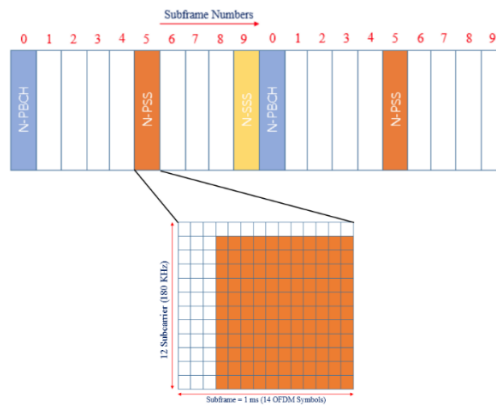


Figure [13]: NPSS Subframe

NPSS base waveform in time domain is generated from a Zadoff-Chu (ZC) sequence of a root index equals to 5 in frequency domain occupying 11 subcarriers of an OFDM symbol in 11 OFDM symbols. It’s required from a ZC sequence to work on a prime number. Thus, the 12<sup>th</sup> subcarrier and first three OFDM symbols are left unused. The sequence is generated by:

$$d(l) = S(l) \cdot e^{\frac{-j\pi u n(n+1)}{11}} \rightarrow u = 5, n = 0,1,2, \dots,10$$

$$S(l) = \{1, 1, 1, 1, -1, -1, 1, 1, 1, -1, 1\}$$

Where  $S(l)$  is the 3GPP standardized code cover.

The reason behind the choice of ZC sequence is that it guarantees zero-crossing auto/cross correlation when correlated with any different signal and a maximum value when correlated with itself so it satisfies the Constant Amplitude Zero Autocorrelation (CAZAC) property which limits the Peak to Average Power Ratio (PAPR) and provides ideal cyclic autocorrelation.

## 2.1.5. Acquisition and CFO Extraction Algorithm

### 2.1.5.1. Channel Modelling

The channel is modelled to be Rayleigh ETU Fading channel with AWGN noise. According to standard release 14, ETU can be modelled with channel tabs and gains of

Table [1]: ETU Channel Tabs and Gains

Channel Tabs (ns)	0	50	120	200	230	500	1600	2300	5000
Channel Gains (dB)	-1	-1	-1	0	0	0	-3	-5	-7

The received time domain signal at the receiver should be modelled as:

$$r(n) = ((x[n] \otimes h[n]) * e^{-j2\pi.\epsilon.n.Ts}) + w[n]$$

where:  $x[n]$  is the baseband signal,  $h[n]$  is the channel impulse response, exponent models the CFO ( $\epsilon$ ) where  $\epsilon = \epsilon_f + \epsilon_I$ ,  $w[n]$  represents the AWGN noise.

### 2.1.5.2. Initial Acquisition Stage

Slide and correlate algorithm is used to calculate the auto-correlation metric for a single frame period with a window of 10 symbols. This is made by multiplying each OFDM symbol to the conjugate of the proceeding symbol (sample by sample). This is done after multiplying each sample with the NPSS code cover to correct symbols that might have been multiplied by “-1” in the transmitter.

$$R(k) = \sum_{i=1}^{N_{window}} \left( r(i) \cdot S\left(\frac{i}{N_S} \% 11\right) \right) \cdot \left( \left( r(i + N_S) \cdot S\left(\frac{i}{N_S} + 1\right) \% 11\right) \right)^*$$

where:

- $k$ : Represents the sample shift
- $N_{window}$ : Number of samples per window
- $N_S$ : Number of samples per symbol
- $i$ : Sample iterator for the same sample shift ( $k$ )
- $R(k)$ : Auto-Correlation Metric for different sample shifts ( $k$ )



For hardware memory utilization purposes, we can't afford having a memory to store this huge metric, thus, it is reduced by a factor of 16, which is done by adding each consecutive 16 windows, resulting in a memory of just 1200 locations instead of 19200 locations.

$$R_{reduced}(k) = \sum_{i=16k}^{16(k+1)-1} R(k)$$

Due to low SNR environments mentioned earlier, this metric has to be averaged over many consecutive frames (M) so it can a reliable outcome. Nevertheless, due to this low SNR, stochastic random peaks might appear in the metric, so, to suppress those peaks we will apply a running average filter on the reduced metric value using the following TD Filter. Where (m) covers 1200 locations only.

$$A(m) = A(m). (1 - \alpha) + R_r(m). (\alpha) \rightarrow 0 < \alpha < 1$$

Coarse Timing and FFO can be estimated then using:

$$\tau = \operatorname{argmax} \forall_m (|A| * 16) - 8$$

$$\epsilon_f = \frac{N}{2\pi N_s} \operatorname{angle} \left( A \left( \frac{\tau + 8}{16} \right) \right)$$

This decision is taken only when the absolute value of the metric of any index exceeds a specific threshold that we extracted by simulating over 500 LTE Frames.

### 2.1.5.3. CFO Extraction and Fine-Tuning Stage

This stage is done by cross-correlating a clean locally generated version of NPSS with the incoming time domain received signal.

$$C(\tau_c, \epsilon_c) = \sum_{i=\tau_c}^{\tau_c+N_p-1} r(i). \left( p(i - \tau_c). e^{\frac{-j2\pi\epsilon_c(i-\tau_c)}{N}} \right)^*$$

Where;

- $r(i)$  is received time domain signal
- $p(i)$  is locally generated NPSS
- $\tau_c = [\tau - \delta, \tau + \delta]$
- $\epsilon_c = ([-2 \sim 2] * 14 \text{ KHZ}) + \epsilon_f$

Deltas in Coarse Timing is a design parameter, chosen to start from 16 until it reaches 1 with the following offsets ( $\pm 8, \pm 4, \pm 2$ ). Number of averaged frames in 2<sup>nd</sup> stage is also a design parameter chosen to be 5 frames for each internally tuning stage. Thus, Final Coarse Timing and CFO can be calculated using

$$(\tau_c, \epsilon_c) = \operatorname{argmax} \forall_{\tau_c, \epsilon_c} |C|$$

## 2.2. CP Remover and Downsampler

Baseband transmitters upsamples the baseband signal from 16 point to 128 point to increase resolution, improve anti-aliasing filter performance and reduce noise. Nevertheless, after upsampling time domain signal baseband transmitters use cyclic prefix in Frequency Division Multiplexing schemes including OFDM to primarily act as a guard band between successive symbols to overcome inter-symbol interference, ISI. Use of cyclic prefix is a key element of enabling the OFDM signal to operate reliably. This is done by copying the last 9 and/or 10 samples to the OFDM symbol start in all NB-IoT subframes according to table (2) below:

Table [2]: Cyclic Prefix Lengths

Symbol #	1	2	3	4	5	6	7	8	9	10	11	12	13	14
CP Length	10	9	9	9	9	9	9	10	9	9	9	9	9	9

So, we need to remove cyclic prefix and then downsample the time domain signal by a factor of 8. We approached this by using a Finite State Machine (FSM) of the following states;

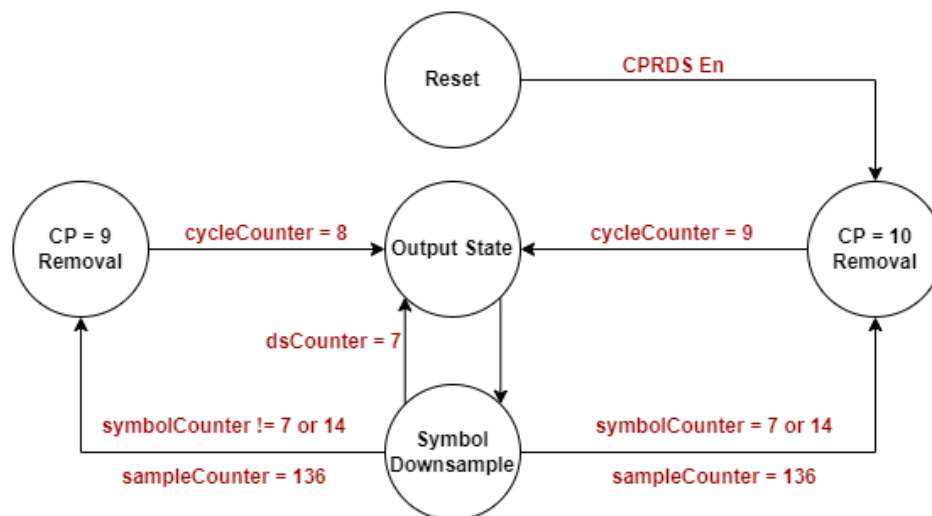


Figure [14]: CPRDS Finite State Machine

Table [3]: CPRDS State Table

State	Description
Reset	Considered as idle state until start of operation
CP10 Removal	Used for 1 <sup>st</sup> and 8 <sup>th</sup> symbols CP Removal
CP9 Removal	Used for rest of subframe symbols CP Removal
Downsample	Used to skip samples in each symbol
Output	Outputs one TD sample in every 8 samples

## 2.3. CFO Corrector

### 2.3.1. CORDIC Algorithm

CFO Corrector is based on CORDIC Algorithm which is used to correct time introduced frequency offset by successively rotating time domain symbols with fixed predetermined angles. CORDIC algorithm is an iterative approach for generating trigonometric functions such as sine and cosine that uses rotations to calculate a wide range of elementary functions using simply shift and add.

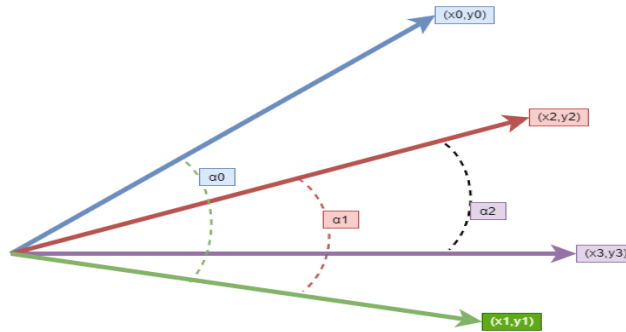


Figure [15]: CORDIC Algorithm Rotations

So, to rotate a vector with a given angle  $\theta$  using CORDIC algorithm as shown in Figure(X) we rotate the vector with constant angles  $\alpha_i$  using the following rotation matrix:

$$\begin{pmatrix} x_{i+1} \\ y_{i+1} \end{pmatrix} = \begin{pmatrix} \cos \alpha_i & -\sin \alpha_i \\ \sin \alpha_i & \cos \alpha_i \end{pmatrix} \begin{pmatrix} x_i \\ y_i \end{pmatrix}$$

$$x_{i+1} = x_i \cos \alpha_i - y_i \sin \alpha_i$$

$$y_{i+1} = x_i \sin \alpha_i + y_i \cos \alpha_i$$

$$\theta_{i+1} = \theta_i - d_i \alpha_i$$

Where  $d_i$  is the sign of  $\theta_i$ . So, after n iteration the  $\theta_n = 0$ , we can take  $\cos \alpha_i$  common factor we get:

$$x_{i+1} = \cos \alpha_i (x_i - y_i \tan \alpha_i)$$

$$y_{i+1} = \cos \alpha_i (y_i + x_i \tan \alpha_i)$$

$$\theta_{i+1} = \theta_i - d_i \alpha_i$$

To simplify the implementation of the CORDIC algorithm we chose  $\tan \alpha_i$  to be equals to  $2^{-i}$  to implement the multiplication using shifting operations so the final form of equations, where  $d_i$  is the sign of  $\theta_i$ :

$$x_{i+1} = \cos \alpha_i (x_i - d_i y_i 2^{-i})$$

$$y_{i+1} = \cos \alpha_i (y_i + d_i x_i 2^{-i})$$

$$\theta_{i+1} = \theta_i - d_i \alpha_i$$

So, after n iterations the new vector will be as follows:

$$\begin{pmatrix} x_n \\ y_n \end{pmatrix} = \cos \alpha_1 * \cos \alpha_2 * \dots * \cos \alpha_n \begin{pmatrix} 1 & -\tan \alpha_1 \\ \tan \alpha_1 & 1 \end{pmatrix} \begin{pmatrix} 1 & -2^{-1} \\ 2^{-1} & 1 \end{pmatrix} \begin{pmatrix} 1 & -2^{-2} \\ 2^{-2} & 1 \end{pmatrix} \dots \begin{pmatrix} 1 & -2^{-n} \\ 2^{-n} & 1 \end{pmatrix} \begin{pmatrix} x_1 \\ y_1 \end{pmatrix}$$

So, we can pre calculate the value of the multiplication of the  $\cos \alpha_i$  as it will be constant k

$$x_n = k(x_0 - d_n y_0 2^{-n})$$

$$y_n = k(y_0 + d_n x_0 2^{-n})$$

$$\theta_n = 0$$

The set of angles that will be used are in range  $-99.7 \leq \theta \leq 99.7$  as the sum of all angles obeying the law of  $\tan \alpha_i$  equals to  $2^{-i}$  is 99.7

Table [4]: CORDIC Micro-Rotation Steps

$\tan \alpha$	$\alpha$	$\cos \alpha$
1	45	0.707106781
0.5	26.5650511771	0.894427191
0.25	14.0362434679	0.9701425
0.125	7.1250163489	0.992277877
0.0625	3.5763343750	0.998052578
0.03125	1.7899106082	0.999512078
0.015625	0.8951737102	0.999877952
0.0078125	0.4476141709	0.999969484
0.00390625	0.2238105004	0.999992371
0.001953125	0.1119056771	0.999998093
0.000976562	0.0559528919	0.999999523
0.000488281	0.0279764526	0.999999881
0.00024414	0.0139882271	0.99999997

From the table we can compute the value of  $k = 0.607252941$

## 2.4. FFT Engine

FFT Engine is used for time domain processing, where it takes 16-point time domain samples and transforms them into frequency components (QPSK Symbols) for farther processing later on.

We chose the Radix  $2^2$  algorithm as it has the same multiplicative complexity as radix 4 algorithm (which is lower than radix 2), but retains the butterfly structure of radix 2 algorithm, which is very suitable for simple and efficient hardware implementation. As shown below in table (5)

Table [5]: FFT Radix Complexity

Radix	# Complex Additions	# Complex Multiplications	Hardware Complexity
Radix-2	64	17	Simple
Radix-4	96	9	Complex
Radix- $2^2$	64	8	Simple

Single Delay Line Feedback (SDF) architecture is used instead of memory based because SDF architecture has very much lower latency as it saves the memory accessing time in both read/write cycles. SDF architectures also minimize the required memory, which can dominate circuit area and power dissipation. Figure (X) below shows Radix  $2^2$  butterfly diagram;

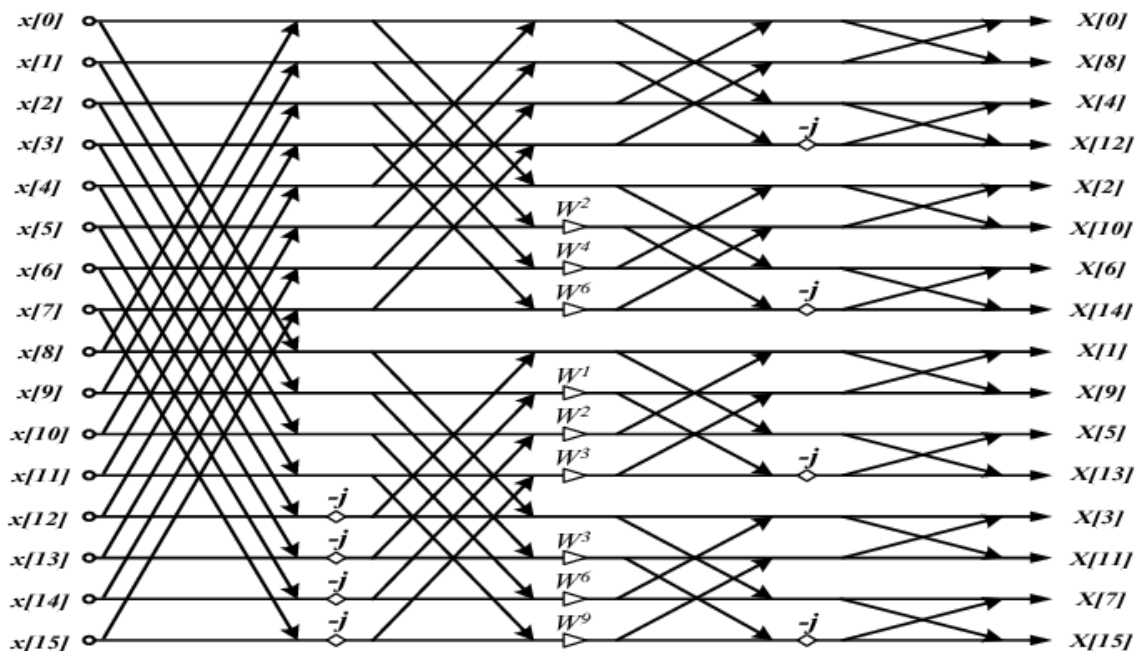


Figure [16]: Radix  $2^2$  Butterfly Diagram

## 2.5. Resource Demapper

Each frame is 10ms in time and consisting of 10 subframe, 1ms each. These subframes are divided into two slots of 0.5ms each. This slot is known as our resource block with 7 OFDM symbols.

A resource block represents one time slot consisting of seven consecutive OFDM symbols  $N_{symbol}^{DL} = 7$  and twelve subcarriers  $N_{sc}^{RB} = 12$ , giving us a total of  $N_{symbol}^{DL} \times N_{sc}^{RB}$  of resource elements.

A resource block is (RB) is the smallest unit of resources that can be allocated to a user. It is used to represent mapping of certain physical channel to a resource element.

As in NB-LTE we use one RB with normal cyclic prefix (CP) giving  $\Delta f = 15KHz$ . Hence, each resource element is 15KHz wide giving us  $BW = 12 * 15 = 180KHz$

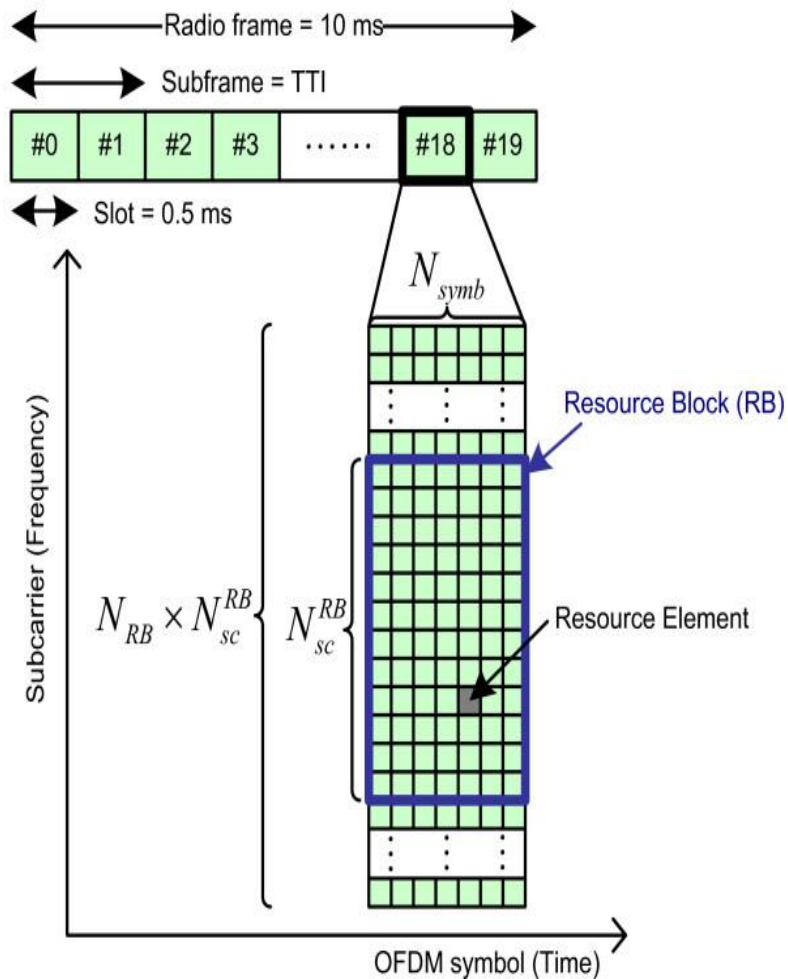


Figure [17]: Downlink resource grid

## 2.6. Channel Estimation

### 2.6.1. Problem Definition

As we deal with wireless channel, we need to take into consideration the environment of our channel and model it properly.

Any wireless channel would suffer from fading which can be classified into

- 1- Large scale fading
- 2- Small scale fading

#### Large Scale Fading:

It is for the large variation found in the received signal amplitude it mainly happens because of

Path Loss:

It is a reduction in the power of the wave as it propagates through the space and it's inversely proportional to the distance.

Shadowing:

It is caused by the obstacles in the path of propagation between Tx and Rx

#### Small Scale Fading:

Caused by interference between versions of the transmitted signal which arrive at the receiver in slightly different times. This interference can be constructive or destructive and as it happening between slightly delayed version so, it may result in rapid variation in phase or amplitude.

Mobile communication also suffers from which is called High-Speed train conditions which arise from moving of the user equipment (UE) while receiving the signal.

#### Power Delay Profile:

It gives the intensity of the signal received through a multi-path fading channel as function of the time delay. This time delay is the difference in travel time between the multipath arrivals.

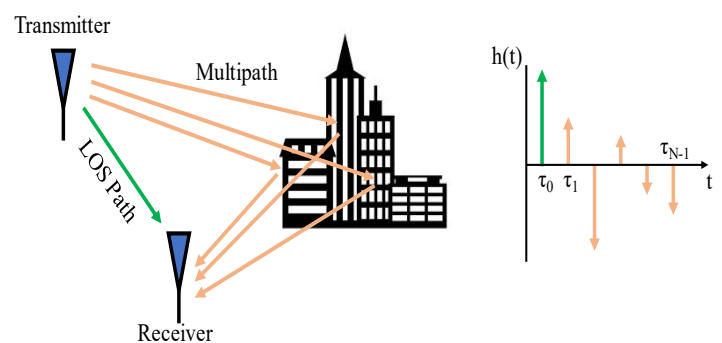


Figure [18]: PDP of a multipath system

### 2.6.2. Used channel model

We used a multipath fading channel model as the channel is modeled as Extended Typical Urban (ETU) with the following delay profile as specified by 3GPP standard.

Table [6]: Power Delay Profile of ETU channel

Excess tap delay (ns)	Relative power (dB)
0	-1
50	-1
120	-1
200	0
230	0
500	0
1600	-3
2300	-5
5000	-7

Maximum doppler frequency shift is 5 Hz and with sampling frequency 1.92 MHz

### 2.6.3. Types of Channel Estimation

There are mainly three types to estimate the channel effect on the signal to be able to compensate it.

There are mainly three types of channel estimation

**Pilot based:** transmitter send certain symbols, which is known to the receiver, to be used in channel estimation process

**Blind:** it uses statistics from the incoming data to estimate the channel effect without the need of known symbols

**Semi-blind:** it uses both statistics from sent data as well as pilots to estimate the channel effect

The channel estimation of the Narrowband Physical Downlink Shared Channel (NPDSCH) is a pilot-based process in which transmitter sends some known symbol and the receiver generate a noiseless version of these symbol then tries to find the relation between the locally generated and the received pilots.

The pilots are called as Narrowband Reference Signal (NRS) there are certain equations and sequence generators to calculate its value and location as per the standard.



These pilots are found in every subframe except for the Narrowband Primary Synchronization Signal (NPSS) and Narrowband Secondary Synchronization Signal (NSSS).

The NRS are found in four subcarriers in each slot with constant magnitude of  $\frac{1}{\sqrt{2}}$ .

#### 2.6.4. Channel estimation algorithm

Pilot based channel estimation used in NB-IoT has many algorithms with a tradeoff between performance with complexity and requirements of low power and area.

Table [7]: Channel Estimation Algorithms

Algorithm	Complexity
Least square	$O(N)$
Minimum Mean Square (classic)	$O(N^3)$
Minimum Mean Square (improved)	$O(N^2)$

We used least square method for its low complexity then used interpolation to compensate for accuracy.

#### 2.6.5. Least Square Channel Estimation

Assume received signal  $y$  that is equal

$$y = xH + AWGN$$

$x$ : transmitted signal

$H$ : channel effect

$AWGN$ : additive white gaussian noise

Least square channel estimated  $H_{est}$

$$H_{est} = \frac{y}{x}$$

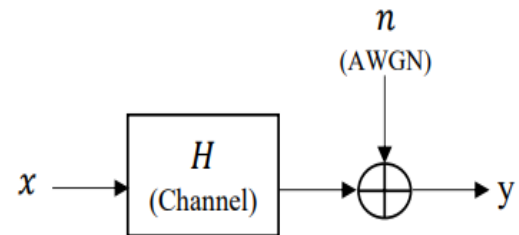


Figure [19]: Channel effect on the signal

By that we see that the algorithm neglects the effect of the additive white gaussian noise which indicates less accuracy but it is less complexity also.

The block aims to effectively divide the received pilot over the locally generated pilots to get the channel effect and then interpolation is done to have better estimate for the channel after that the estimated channel values are given to the equalizer.

#### 2.6.6. Interpolation

As the pilots are found in only four subcarriers while we have twelve subcarriers so interpolation process must be done.

Interpolation can be done in three different techniques

2.6.6.1. Zero order interpolation

Here the interpolation is constant in which each three subcarriers having one pilots will be divided by its channel estimate.  $H_{LS}$

The channel estimation gives four estimates per slot as there are four NRS. Each estimate will be used by three consecutive subcarriers.

This is the simplest one but with lowest performance.

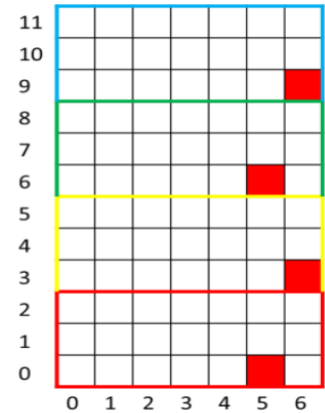


Figure [20]: Zero-Order interpolation

2.6.6.2. Interpolation over slot

Linear interpolation is calculated over the slot, in each slot we have four estimates we use them and interpolate giving twelve different outputs  $H_{LS}$  each one used by the equalizer with its corresponded subcarrier.

More complex than the previous with slight increase in the performance.

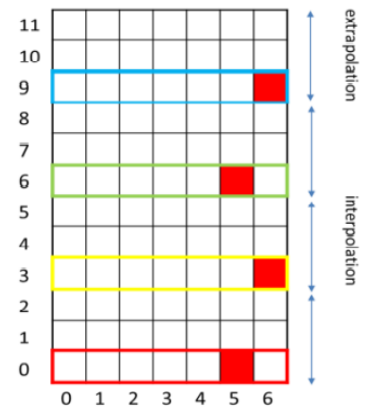


Figure [21]: Interpolation over slot

2.6.6.3. Interpolation over subframe

Linear interpolation is calculated over the subframe, in each subframe we have two slots giving a total of eight estimates.

Averaging first is done over every two on the same subcarrier then liner interpolation over the twelve subcarriers giving twelve different estimates to be used by the equalizer.

The most complex of the three but with noticeable impact on the performance.

This is the one to be used in our system.

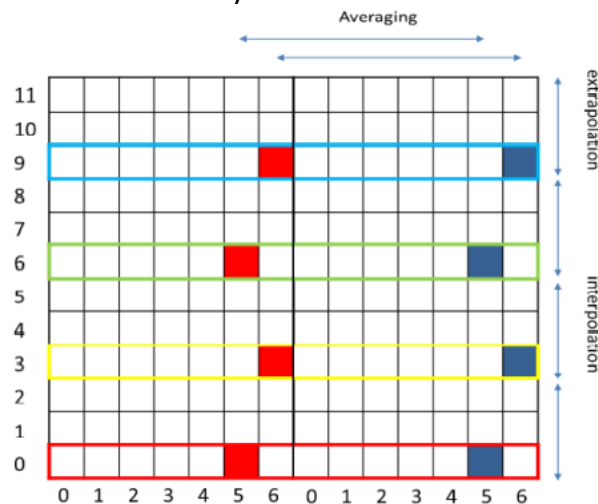


Figure [22]: Interpolation over subframe

## 2.6.6.4. Comparison

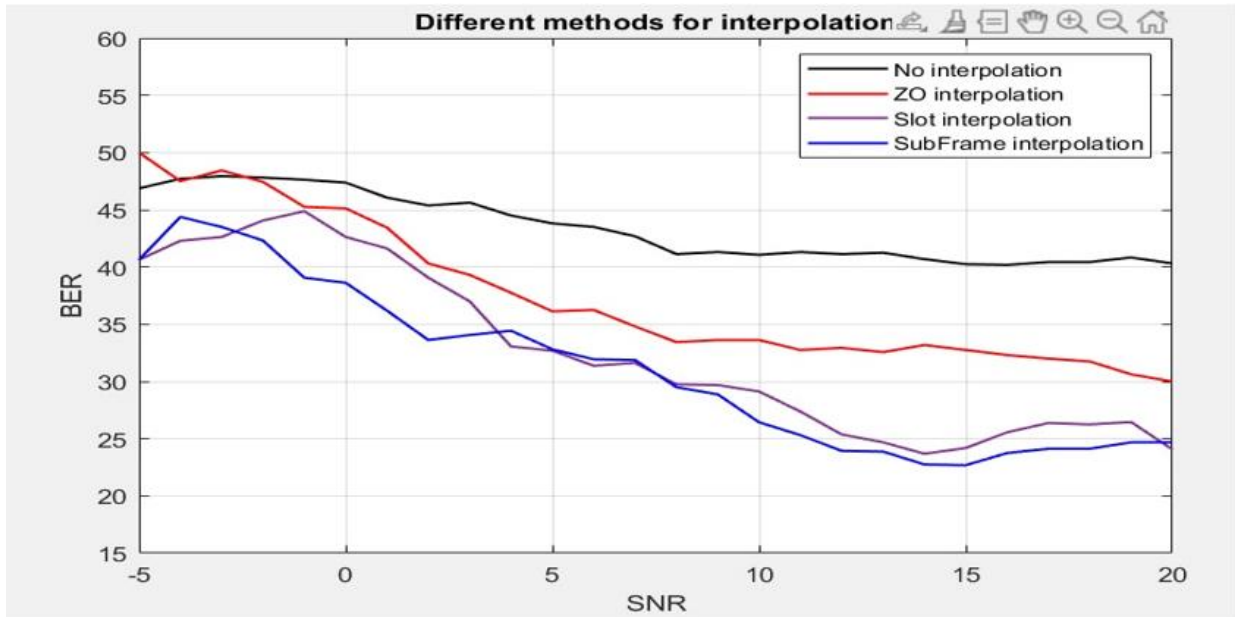


Figure [23]: BER vs SNR for different types of interpolations

## 2.7. NRS Value Generator

NRS are our pilots which will be used to estimate the channel effect so, we need to locally generate these pilots. According to 3GPP standard there are specific equations to get the values of our pilots.

### 2.7.1. Generating the NRS values

#### 2.7.1.1. Variables

NRS values change every slot depending on three variables

*l*: number of OFDM symbol carrying the NRS (5,6)

*m*:  $m = 0, 1, \dots, 2N_{RB}^{maxDL} - 1 \rightarrow$  so  $m = 0, 1$

Where  $N_{RB}^{maxDL}$  is the maximum downlink resource block which is equal to 1 in narrowband case.

*ns*: number of slot ranges from 0 to 19

#### 2.7.1.2. Equations

$$r_{l,ns}(m) = \frac{1}{\sqrt{2}} (1 - 2C(2m)) + \frac{j}{(\sqrt{2})} (1 - 2C(2m + 1))$$

Where C refers to pseudo random sequence generated by 31-length golden sequence defined below

$$C(n) = (x1(n + Nc) + x2(n + NC)) \bmod 2$$

And sequences  $x1$  and  $x2$  defined as follow:

$$x1(n + 31) = (x1(n + 3) + x1(n)) \bmod 2$$

Initialized with  $x1(0) = 1$  and  $x1(n) = 0$  for  $n = 1, 2, 3, \dots, 30$

$$x2(n + 31) = (x2(n + 3) + x2(n + 2) + x2(n + 1) + x2(n)) \bmod 2$$

Initialized with sequence  $c_{init}$

$$c_{init} = 2^{10} (7(ns + 1) + l + 1) (2N_{ID}^{cell} + 1) + 2N_{ID}^{cell} + N_{cp}$$

And

$$Nc = 1600$$

$N_{ID}^{cell} \in (0, 504)$  and it's input from upper layer.

$N_{cp} = 1$  for normal cyclic prefix

## 2.8. NRS Index Generator

There are set of defined equation in the standard for the NRS location as their location vary, we must track it to extract it from the resource block.

### 2.8.1. Generating NRS Indices

#### 2.8.1.1. Variables

NRS location within the resource block depend on

$v$ : variable which change with OFDM symbol number

$v_{shift}$ : which depend on  $N_{ID}^{cell}$

$m$ :  $m = 0, 1, \dots, 2N_{RB}^{maxDL} - 1 \rightarrow$  so  $m = 0, 1$

#### 2.8.1.2. Equations

$$k = 6m + (v + v_{shift})$$

$N_{symb}^{DL}$ : number of symbols in one slot which is 7

$l = N_{symb}^{DL} - 2, N_{symb}^{DL} - 1 = 5, 6$  in each slot

$k$ : refers to the subcarrier carrying the pilot

So, it can be said that  $k$  refers to the number of rows in which the pilot is placed within the resource block

$v = 0$ , if  $l = 5$

$v = 1$ , if  $l = 6$

$v_{shift} = N_{ID}^{cell} \bmod 6$

Note:  $N_{ID}^{cell} \bmod 6$  is assumed to be given from upper layer

## 2.9. Channel Equalizer

The data transmitted through wireless medium suffer from multipath fading and noise so, we need received data as receiver can be expressed as follow in time domain

$$r_k = s_k \otimes h_k + n_k$$

In which

$r_k$ : represent the received data.

$s_k$ : represent the sent data.

$h_k$ : represent the channel effect

$n_k$ : represent the AWGN

To receive the data correctly we should compensate to this channel effect. So, we need to know it as correct as possible in order to cancel it from the received data.

First the channel estimation tries to estimate the channel effect and pass these estimates to the channel equalizer. The equalizer will cancel the effect by dividing each symbol by the corresponding channel estimated value

$$y_k = s_k \times \frac{h_k}{h_{eq}} + \frac{n_k}{h_{eq}}$$

In which

$h_{eq}$ : estimated value of the channel

In the equalizer we divide the symbol by the channel effect that was estimated by the channel estimation.

We get the symbols from resource demapper and divide them by the estimates one by one. So, the block is based on complex division.

### 2.9.1. Complex division

It is possible to use a complex divider directly but it is not common and not a good practice as it consumes area and power. So, we replace it with complex multipliers.

Consider  $a + ib$  and  $c + id$  so dividing them gives  $\frac{a+ib}{c+id}$  then multiply numerator and denominator with conjugate.

$$\frac{a + ib}{c + id} \times \frac{c - id}{c - id} = \frac{(ac + bd) + i(bc - ad)}{c^2 + d^2}$$

The numerator is output of a complex multiplier and the denominator is a real positive scaling value which won't affect the accuracy of demodulating a QPSK symbol as we concerned only with phase not magnitude.

---

## 2.10. Parallel to Serial and NRS removal

After equalization and till the end of the chain the data should be serial and the NRS are useless after channel estimation as it is not actual data and the real data at the transmitter doesn't contain these NRS. So, the data must be converted from parallel to serial and the NRS should be removed.

## 2.11. Fine Synchronizer

### 2.11.1. Problem Definition

Assuming channel impulse response is not changed over a subframe, continuous tracking of the residual frequency offset takes place for every received subframe after successive acquisition is done at the beginning in the Coarse Synchronizer. This offset is used to correct the received symbols in carrier frequency offset block at the beginning of our chain.

The residual frequency offset extraction is done by tracking the frequency offset effects on the Narrowband Reference Signals (NRS) of different OFDM symbols, which are sent over 4 different subcarriers in the two slots of each subframe.

### 2.11.2. Narrowband Reference Signals NRS

They are reference signals that are used as pilots to estimate the channel effects on the received data. They are distributed within the subframe at four different subcarriers with frequency spacing of 45 kHz between each two consecutive subcarriers carrying NRS signals.

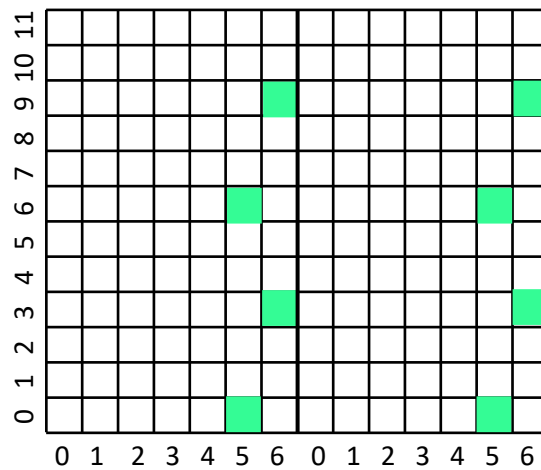


Figure [24]: Frame Pilot Locations

### 2.11.3. Frequency Offset Estimation

By using NRS signals of the same subcarrier we can estimate the frequency offset as we have 4 pairs of NRS signals in each subframe,

The ratio between the complex multiplication of two NRS signals of the received subframe and the locally generated NRS signals which are supposed to be received is given by the following equation

$$\frac{R_l(p)R_{l+N_s}^*(p)}{X_l(p)X_{l+N_s}^*(p)} = K e^{\frac{-i2\pi N_s(N+N_{CP})\epsilon_r}{N}}$$



Where:

$X_l(p)$  : Generated NRS OFDM symbol

$R_l(p)$  : Received NRS OFDM symbol

$N_s$  : Number of OFDM symbols in one slot,  $N_s = 7$  in NB-IoT

$p$  : The subcarrier frequency index

$l$  : The OFDM time symbol index

$N$  : Number of samples in subframe

$N_{CP}$  : Length of Cyclic Prefix in number of samples

$\varepsilon_r$  : Residual frequency offset.

Repeating this operation for each pair of NRS signals at each given subcarrier. The phase of the result is proportional to the required frequency offset so the frequency offset is given by:

$$\varepsilon_r = \frac{N}{2\pi N_s(N + N_{CP})} \angle \left( \sum_{p \in \mathcal{V}} \frac{R_l(p)R_{l+N_s}^*(p)}{X_l(p)X_{l+N_s}^*(p)} \right)$$

Where:

$\mathcal{V}$  : set of the four subcarriers where NRS are sent in subframe.

The phase of this residual frequency offset is desired to be calculated in order to be used in the carrier frequency offset block to eliminate this offset by correcting the received symbols.

## 2.12. Demodulator

### 2.12.1. Problem Definition

The stated demodulation scheme for the NPDSCH is the Quadrature Phase Shift keying (QPSK) which changes the carrier phase based on the input data bits. So, the demodulator reverses this operation.

QPSK modulation Scheme maps each 2 bits of data to a specific QPSK symbol having In-Phase and quadrature components as shown in the following table.

Table [8]: In phase and Quadrature components of QPSK

$b_i, b_{i+1}$	I	Q
00	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$
01	$\frac{1}{\sqrt{2}}$	$-\frac{1}{\sqrt{2}}$
10	$-\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$
11	$-\frac{1}{\sqrt{2}}$	$-\frac{1}{\sqrt{2}}$

So, the Demodulator in the same manner receives the QPSK symbol after equalizing the channel effects and processes them.

Using Hard Decision, the data bits are determined based on the signs of the received I and Q components in the QPSK constellation, this helps using hard decision in the rest of the receiving chain as well.

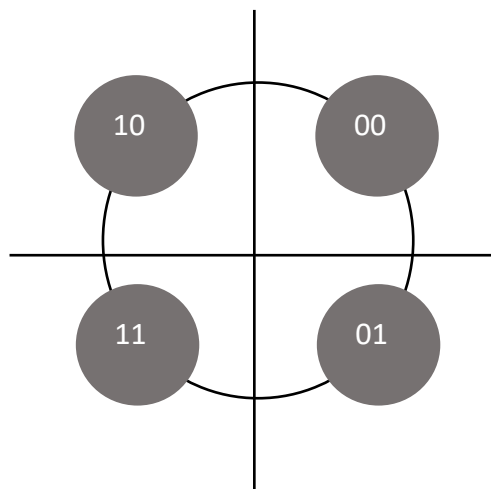


Figure [25]: QPSK Constellation Diagram

## 2.13. Descrambler

### 2.13.1. Problem Definition

Scrambling is important as it is used to eliminate long sequences of 0's and 1's by conditionally inverting some bits based on a Pseudo-random Noise sequence generated from two Linear Feedback Shift Registers and also helps in security of received data as it depends on specific parameters such as the cell identifier, and the Radio Network Temporary Identifier.

### 2.13.2. Polynomials and Equations

Descrambler is implemented in the same manner as the scrambler because they use the same polynomial shown down below:

$$C(n) = (x_1(n + N_c) + x_2(n + N_c)) \bmod 2$$

And sequences  $x_1$  and  $x_2$  defined as follow

$$x_1(n + 31) = (x_1(n + 3) + x_1(n)) \bmod 2$$

Initialized with  $x_1(0) = 1, x_1(n) = 0, n = 1, 2, \dots, 30$

$$x_2(n + 31) = (x_2(n + 3) + x_2(n + 2) + x_2(n + 1) + x_2(n)) \bmod 2$$

Initialized with sequence  $c_{init}$

$$c_{init} = n_{RNTI} \cdot 2^{14} + n_f \bmod 2 \cdot 2^{13} + \lfloor n_s/2 \rfloor \cdot 2^9 + N_{ID}^{N_{cell}} \text{ for NPDSCH}$$

Where:

$$N_c = 1600$$

$N_{ID}^{cell} \in (0, 503)$  Cell Identifier Number and it's input from upper layer.

$n_f$  System frame number

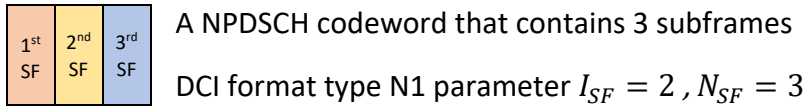
$n_s \in (0, 19)$  Slot number

$n_{RNTI}$  Radio Network Temporary Identifier

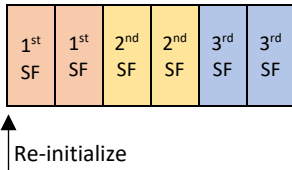
Initialization takes 1600 cycle then the sequence should stop until the input is valid then with each cycle the PN sequence is XORed with the input.

### 2.13.3. Descrambler Re-Initialization

The Linear feedback shift registers get re-initialized every  $\min(N_{rep}, 4)$  transmissions of the codeword. Repetitions in NPDSCH is done by repeating the message. The generated codeword in  $N_{SF}$  subframes are repeated  $N_{Rep}$  times.



Case:  $N_{Rep} = 2$



Case:  $N_{Rep} = 8$

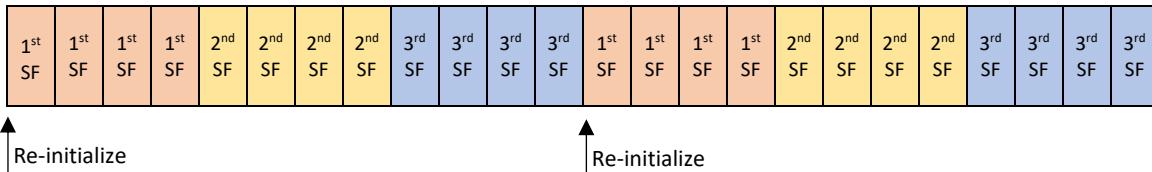


Figure [26]: Descrambler Re-initialization

## 2.14. Rate De-Matcher

### 2.14.1. Problem Definition

The rate matcher is used to improve the system performance as it sends 3 streams of the encoded data and interleaves them by a specified inter-column permutation matrix which changes the code rate of the transmitted data and distributes the information so that they don't face the same channel effects to grantee diversity.

Repetitions are handled by this block as the same codeword length can be transmitted multiple times to decrease the possibility of failure and re-transmissions.

Maximum voting technique is used to handle repetitions in the bit collection stage.

### 2.14.2. The Rate matcher

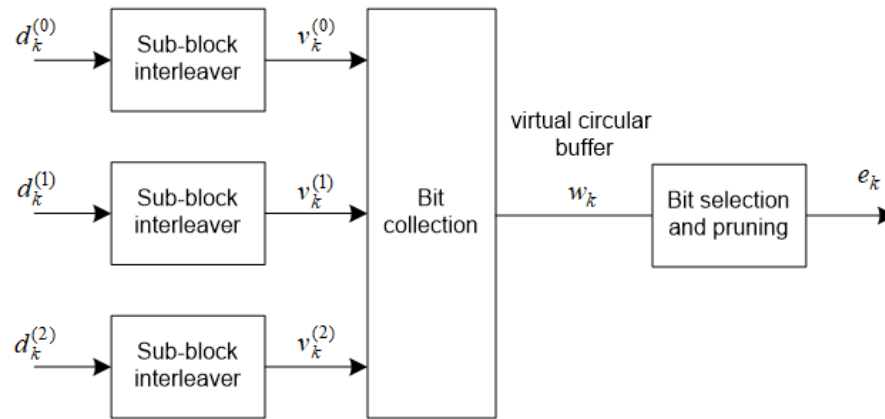


Figure [27]: Rate Matcher Subblocks

The input to the Rate matcher block is the 3 outputs of the tail-biting convolutional encoder  $d_k^{(1)}$ ,  $d_k^{(2)}$ ,  $d_k^{(3)}$  each of length  $D$  as  $D$  is the number of bits

#### 2.14.2.1. Sub-block interleaver

A reshape matrix of number of columns equal 32 and number of rows equal the ceiling of division of number of bits by 32, then dummy bits of number  $N_D$  are added to the beginning of this matrix such that

$$C_{subblock}^{CC} = 32$$

$$R_{subblock}^{CC} = \left\lceil \frac{D}{C_{subblock}^{CC}} \right\rceil$$

$$K_{\pi} = C_{subblock}^{CC} \times R_{subblock}^{CC}$$

$$N_D = K_{\pi} - D$$

And the interleavers are filled by  $y_k$  where:

$$y_k = \langle NULL \rangle \text{ for } k = 0, 1, \dots, N_D$$

$$y_{N_D+k} = d_k^{(1)} \text{ for } k = 0, 1, \dots, D$$

The three encoded data streams are stored in three matrices by filling them row by row using the incoming data after the first  $N_D$  bits which are dummy bits.

$$\begin{bmatrix} y_0 & y_1 & y_2 & \dots & y_{C_{subblock}^{CC}-1} \\ y_{C_{subblock}^{CC}} & y_{C_{subblock}^{CC}+1} & y_{C_{subblock}^{CC}+2} & \dots & y_{2C_{subblock}^{CC}-1} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ y_{(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}} & y_{(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}+1} & y_{(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}+2} & \dots & y_{(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}} \end{bmatrix}$$

Figure [28]: Interleaver Matrix

The Encoded bits of each bit stream gets interleaved based on an intercolumn permutation pattern shown:

Number of columns $C_{subblock}^{CC}$	Inter-column permutation pattern $\langle P(0), P(1), \dots, P(C_{subblock}^{CC}-1) \rangle$
32	$\langle 1, 17, 9, 25, 5, 21, 13, 29, 3, 19, 11, 27, 7, 23, 15, 31, 0, 16, 8, 24, 4, 20, 12, 28, 2, 18, 10, 26, 6, 22, 14, 30 \rangle$

Figure [29]: Interleavers Intercolumn Permutation Pattern

Then after performing the inter-column permutation the result is

$$\begin{bmatrix} y_{P(0)} & y_{P(1)} & y_{P(2)} & \dots & y_{P(C_{subblock}^{CC}-1)} \\ y_{P(0)+C_{subblock}^{CC}} & y_{P(1)+C_{subblock}^{CC}} & y_{P(2)+C_{subblock}^{CC}} & \dots & y_{P(C_{subblock}^{CC}-1)+C_{subblock}^{CC}} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ y_{P(0)+(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}} & y_{P(1)+(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}} & y_{P(2)+(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}} & \dots & y_{P(C_{subblock}^{CC}-1)+(R_{subblock}^{CC}-1) \times C_{subblock}^{CC}} \end{bmatrix}$$

Figure [30]: Interleaver Matrix after performing intercolumn change

#### 2.14.2.2. Bit Collection and transmission

The output of the block interleaver is read column by column and fill the circular buffer of length  $K_w = 3K_\pi$  with the data of each interleaver in the following manner,

$$w_k = v_k^{(1)}$$

$$w_{K_\pi+k} = v_k^{(2)}$$

$$w_{2K_\pi+k} = v_k^{(3)}$$

After that, data is read from the circular buffer by eliminating the dummy bits until reach E

where E is the output sequence length

The following Pseudo code represents how the output is generated.

output=  $e_k$  where  $k = 0,1, \dots, E-1$

```

Set  $k = 0$  and  $j = 0$ 
while  $\{k < E\}$ 
  if  $w_{j \bmod K_w} \neq \langle NULL \rangle$ 
     $e_k = w_{j \bmod K_w}$ 
     $k = k + 1$ 
  end if
   $j = j + 1$ 
end while
    
```

### 2.14.3. The Rate De-matcher:

#### 2.14.3.1. Bit collection

Bit collecting which is a memory of size that should cover the length of the circular buffer for the maximum TBS that can be transmit which is 2536 and the maximum repetitions number which is 2048 in release 14.

$$\text{Circular buffer length} = 3 * (\text{Max TBS} + 24 \text{ bits CRC}) * \log_2(\text{max repetition size})$$

There are 3 possibilities for the value of the input data length E:

1.  $E = K_w$ , then the value saved in the buffer will be passed to the interleavers
2.  $E > K_w$ , then the incoming bit stream is added to the previous repetitions of data and then take the average of them and compare it to 0.5, if it is greater than or equal the value is assumed to be 1 else, it is a 0, which is called maximum voting
3.  $E < K_w$ , then the buffer is zero-padded

#### 2.14.3.2. Sub-block De-interleaver

Interleavers which are three memories of size that should cover the length of  $K_\pi$  and consists of  $C_{subblock}^{CC}$  columns and  $R_{subblock}^{CC}$  rows.

$$\text{Interleaver length} = C_{subblock}^{CC} * \left\lceil \frac{\text{Max TBS} + 24 \text{ bits CRC}}{C_{subblock}^{CC}} \right\rceil$$

The bit collection stage output is the input for the interleavers which are written in a specific order following the permutation pattern and then read in another order to execute the interleaving process.

Rate De-matcher de-interleavers input writing direction:

$$\downarrow \begin{bmatrix} a_{0,0} & a_{0,1} & a_{0,2} & a_{0,3} & a_{0,4} & \dots & a_{0,31} \\ a_{1,0} & a_{1,1} & a_{1,2} & a_{1,3} & a_{1,4} & \dots & a_{1,31} \\ a_{2,0} & a_{2,1} & a_{2,2} & a_{2,3} & a_{2,4} & \dots & a_{2,31} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ a_{r,0} & a_{r,1} & a_{r,2} & a_{r,3} & a_{r,4} & \dots & a_{r,31} \end{bmatrix}$$

Rate De-matcher de-interleavers output reading direction:

$$\begin{matrix} \longrightarrow \\ \begin{bmatrix} a_{0,1} & a_{0,17} & a_{0,9} & a_{0,25} & a_{0,5} & \dots & a_{0,30} \\ a_{1,1} & a_{1,17} & a_{1,9} & a_{1,25} & a_{1,5} & \dots & a_{1,30} \\ a_{2,1} & a_{2,17} & a_{2,9} & a_{2,25} & a_{2,5} & \dots & a_{2,30} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ a_{r,1} & a_{r,17} & a_{r,9} & a_{r,25} & a_{r,5} & \dots & a_{r,30} \end{bmatrix} \end{matrix}$$



## 2.15. Viterbi Decoder

### 2.15.1. Tail Biting Convolutional Encoder

A Tail Biting Convolutional Encoder (TBCC) with constraint length 7 and a rate of 1/3 is defined in 3GPP 36.212 standard as shown in the figure with polynomials  $G_0 = 133$ ,  $G_1=171$ ,  $G_2=165$  (octal).

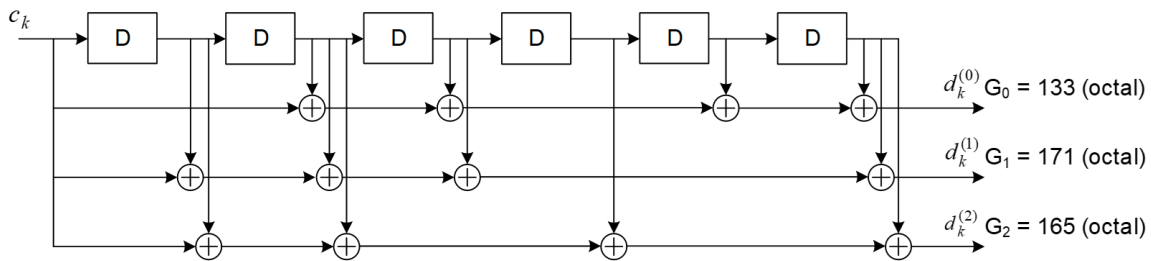


Figure [31]: Tail Biting Convolutional Encoder for NB-IOT LTE

Another requirement is defined to initialize the states of encoder’s shift register. The initial value of the shift register is the last 6 bits of the transmitted block. This results in having the initial state of the shift register equal to the final state of the shift register. This increases the decoder complexity but also doesn’t affect the code rate.

### 2.15.2. Viterbi Algorithm

Viterbi algorithm is a maximum likelihood method to detect the most probable sequence of states given certain bits. It calculates the similarities (Hamming Distance in hard decision decoders) between the received bits and all trellis paths entering each state at a time as shown in the figure.

### 2.15.3. System Requirements

The algorithm needed for the system must have a lower complexity as we need to reduce the power, the winning path must be a tail biting path as the encoder implicitly made the initial state and the final state equal, the available states in the trellis diagram are 64 states as we have a 6-bit shift register and the code rate is 1/3 so the received message will be divided into 3-bit segments. The algorithm chosen for the system is Wrap Around Viterbi Algorithm (WAVA).

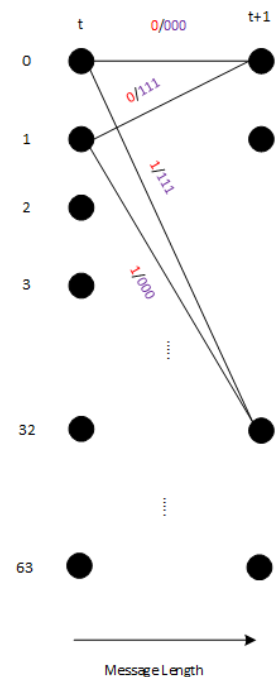


Figure [32]: Trellis Diagram

#### 2.15.4. Wrap Around Viterbi Algorithm

It is an iterative algorithm that applies the non-fixed state Viterbi algorithm and keeps applying itself until the winning path becomes a tail biting path where the initial and final states become equal. Steps of the algorithm are as shown:

1. Start from all the state with state metrics set to 0
2. Proceed in the trellis diagram calculating Branch Metrics, Path Metrics and Survived Paths for all states.
3. Perform the traceback operation to reach the initial state to evaluate the Tailbiting Condition.
4. If the Tailbiting Condition is true, assert the valid signal and start the output stream of decoded bits.
5. If the Tailbiting Condition is false, go to step 2 and keep the current values of the path metrics saved for the next iteration.
6. If the number of iterations becomes 3, assert the valid signal and start the output stream of decoded bits.

## 2.16. Cyclic Redundancy Check

Cyclic redundancy check is an error detecting code used to validate received data integrity by appending a specific value to the data which is the remainder in case of dividing this data by  $w$  specific polynomial, which makes the result divisible by this polynomial so at the receiver the result of this operation should result in Zero which means the received data is correct.

The parity bits are generated by the following cyclic generator polynomial:

$$g_{CRC24A}(D) = D^{24} + D^{23} + D^{18} + D^{17} + D^{14} + D^{11} + D^{10} + D^7 + D^6 + D^5 + D^4 + D^3 + D + 1$$

Where the input bits are denoted by  $a_0, a_1, a_2, a_3, \dots, a_{A-1}$ , while the parity bits are denoted by  $p_0, p_1, p_2, p_3, \dots, p_{L-1}$

After appending the CRC parity bits, the output is denoted by  $b_0, b_1, b_2, b_3, \dots, b_{B-1}$  where  $B=A+L$

$$b_k = a_k \text{ for } k = 0, 1, 2, \dots, A-1$$

$$b_k = p_{k-A} \text{ for } k = A, A+1, A+2, \dots, A+L-1.$$



Figure [33]: CRC appending

Cyclic redundancy check is implemented in the same manner in the receiver because they use the same polynomial.

### 3.1. Coarse Synchronizer

#### 3.1.1. Top Module

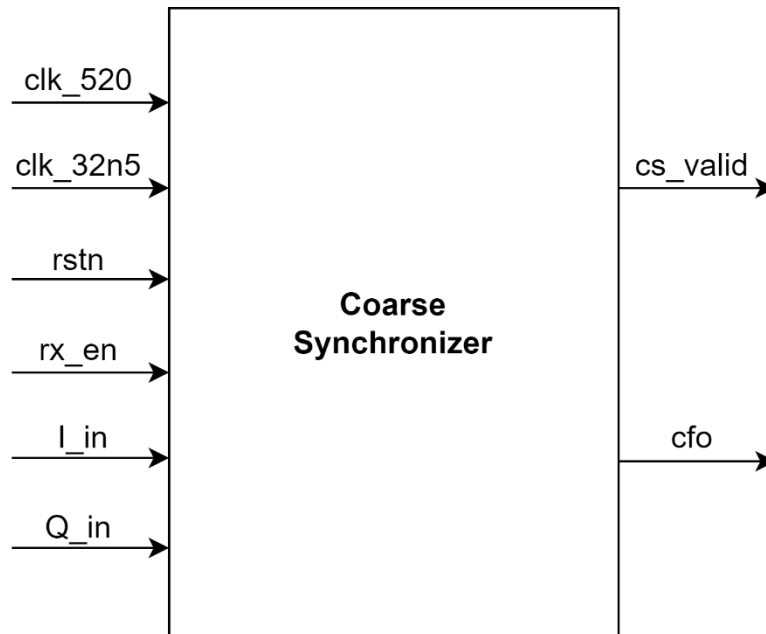


Figure [34]: Coarse Synchronizer Top Module

Table [9]: Coarse Synchronizer Interface Table

Signal Name	Direction	Width	Description
clk_520	Input	1	1.92 MHz clock signal
clk_32n5	Input	1	30.769 MHz clock signal for internal CORDIC units in Fine-Tuning Stage
rstn	Input	1	Global reset signal
rx_en	Input	1	Enable Signal that indicates the start of NB-IoT Receiver Operation
I_in	Input	16	Real serial input samples
Q_in	Input	16	Imaginary serial input samples
cs_valid	Output	1	Valid Signal indicating the validity of the output CFO
cfo	Output	19	Estimated Carrier Frequency Offset

### 3.1.2. Detailed Hardware

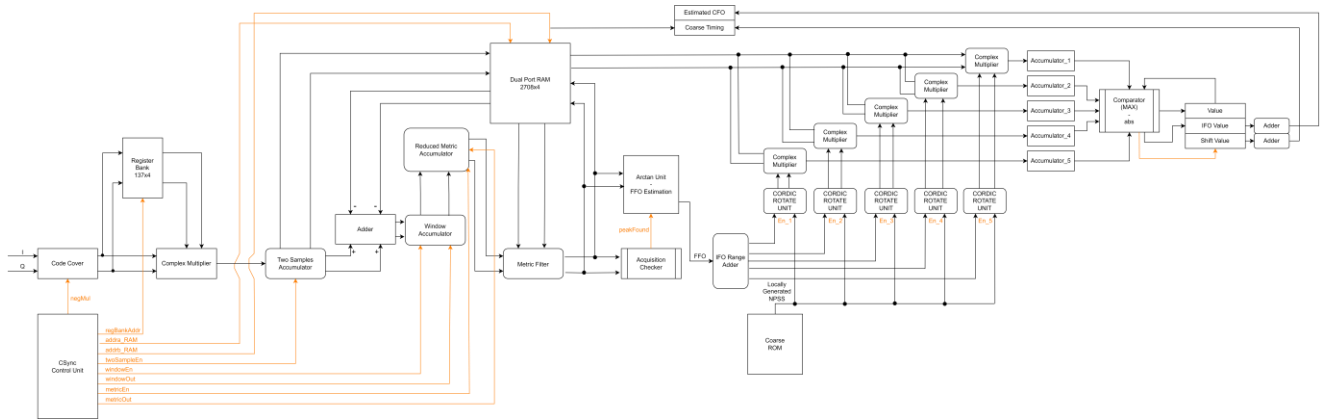


Figure [35]: Coarse Synchronizer Detailed Hardware

### 3.1.3. Design Challenges and Solutions

#### 3.1.3.1. High Power Consumption

Coarse Synchronizer is the most power-hungry block in the RX chain as it is one of the largest in area and contains many arithmetic circuits for metric calculations and frame processing. In order to minimize the power consumption, we used some of the **Low Power Design Techniques** in the block design

- **Operand Isolation:** By inserting pipeline registers before any arithmetic operation, this is because one of the operands bits might arrive at different time than other bits within the same clock cycle, making the arithmetic circuit operate multiple times within the same clock cycle. By Registering the input operands, we ensure that the arithmetic circuit will operate only once as they are already after the active clock edge.

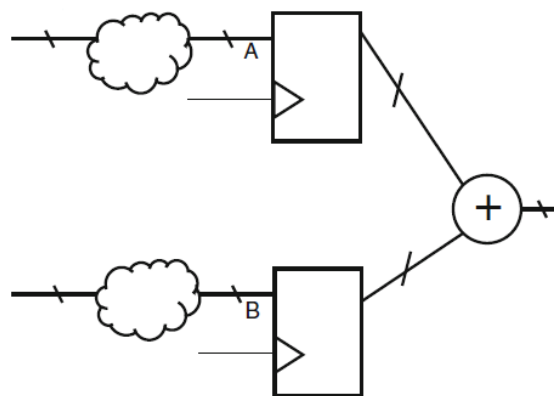


Figure [36]: LPDT-Operand Isolation

- Comparison Priority: Coarse Synchronizer continuously compares metric values with the Acquisition Threshold which consumes high power as comparator operations involve XORs which have high switching activity factor, thus, consuming more power. So, when we have to compare large data busses, we avoided comparing all the bits in one go but rather we compared the MSB's first, if it satisfies the condition, there's no need to evaluate the rest of the bit XORing. If not, then we compare the rest of the bus bits.

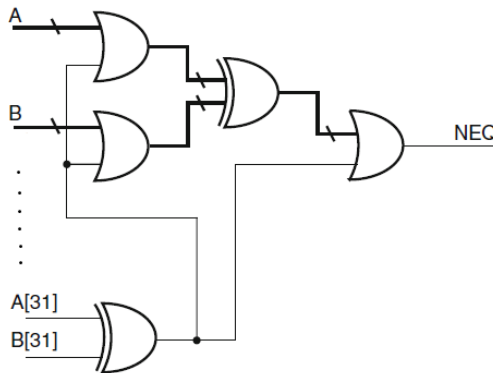


Figure [37]: LPDT-Comparison Priority

### 3.1.3.2. Large Memory Requirements

Coarse Synchronizer requires storing different window metric values along the NB-IoT frame which consumes around  $\left(\frac{19200 \cdot 32}{8 \cdot 1024} = 75 \text{ KB}\right)$ . We solved this problem by successive addition of every 16-window metric with each other and fine-tuning these metric accumulations in the Fine-Tuning Stage to preserve the CFO extraction accuracy. Resulting in the need of only  $\frac{1200 \cdot 32}{8 \cdot 1024} = 4.6875 \text{ KB}$ .

### 3.1.3.3. Window's Metric Huge Latency

Window sliding to calculate coarse timing requires processing on 1508 samples in every window over the entire NB-IoT frame which introduces huge latency in the block. Thus, we decided to store the window sample multiplications so that this processing occurs only once for the first window, and every new sample, a new window is evaluated by subtracting the multiplication of first samples and adding the multiplication of the newer samples. Thus, decreasing block's latency.

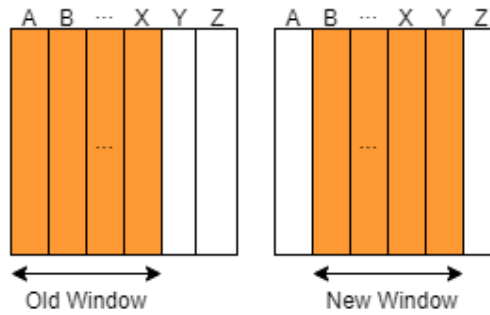


Figure [38]: Window Sliding

### 3.1.4. MATLAB Results

MathsWorks LTE Toolbox were used to generate input vectors to the Coarse Synchronizer MATLAB model for algorithm’s accuracy testing.

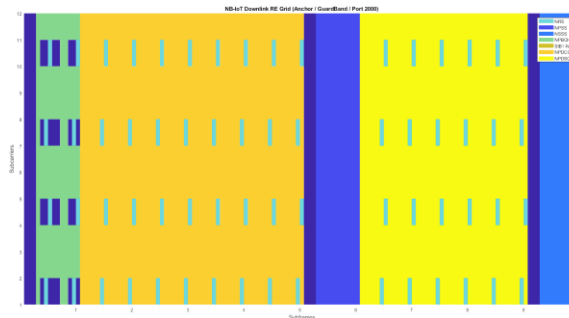


Figure [39]: NB-IoT One Frame RE Grid

Operating on randomly generated data on  $SNR = -15\text{ dB}$ , the figure below shows the acquisition results along with estimated coarse timing and CFO extraction errors.

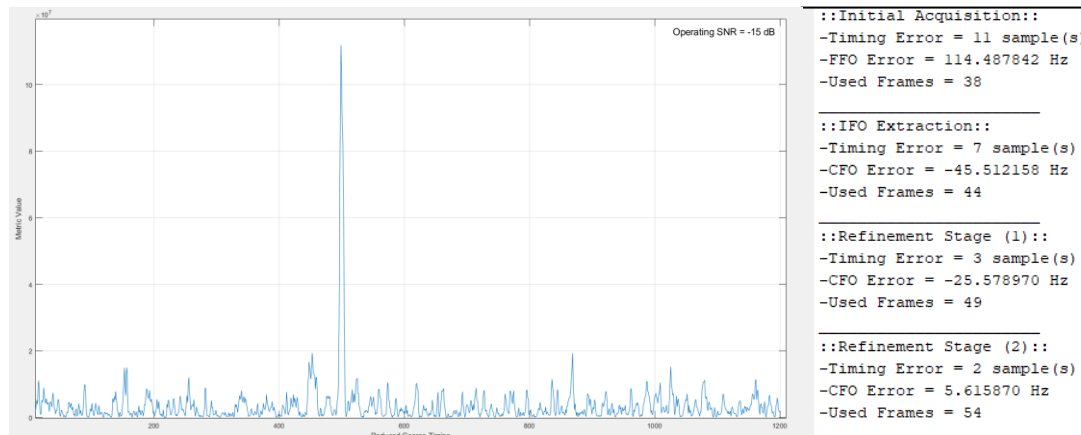


Figure [40]: Acquisition and CFO Extraction MATLAB Results

### 3.1.5. Synthesis Results

The Figure below shows the overall synthesized area in FPGA cells on the targeted FPGA. Synthesis is done using Vivado Design Suite which includes block’s utilization in resources (LUTs, FFs, DSPs, etc.)

Utilization		Post-Synthesis		Post-Implementation	
Resource	Estimation	Available	Utilization %		
LUT	2440	53200	4.59		
LUTRAM	96	17400	0.55		
FF	1193	106400	1.12		
DSP	48	220	21.82		
IO	56	200	28.00		
BUFG	2	32	6.25		

Figure [41]: Coarse Synchronizer Synthesis Utilization

## 3.2. CP Remover and Downsampler

### 3.2.1. Top Module

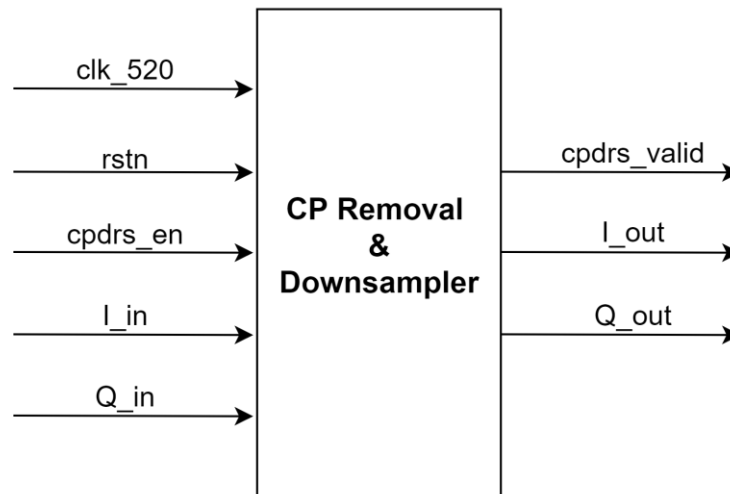


Figure [42]: CP Remover and Downsampler Top Module

Table [10]: CP Remover and Downsampler Interface Table

Signal Name	Direction	Width	Description
clk_520	Input	1	1.92 MHz clock signal
rstn	Input	1	Global reset signal
cprds_en	Input	1	Enable Signal that indicates the start block's operation
I_in	Input	16	Real serial input samples
Q_in	Input	16	Imaginary serial input samples
cprds_valid	Output	1	Valid Signal indicating the validity of the output samples
I_out	Output	16	Real serial output samples
Q_out	Output	16	Imaginary serial output samples



### 3.2.2. Synthesis Results

Utilization		Post-Synthesis   Post-Implementation		
				Graph   Table
Resource	Estimation	Available	Utilization %	
LUT	62	53200	0.12	
FF	21	106400	0.02	
IO	68	200	34.00	
BUFG	1	32	3.13	

Figure [43]: CPRDS Synthesis Utilization

### 3.3. CFO Corrector

#### 3.3.1. Top Module

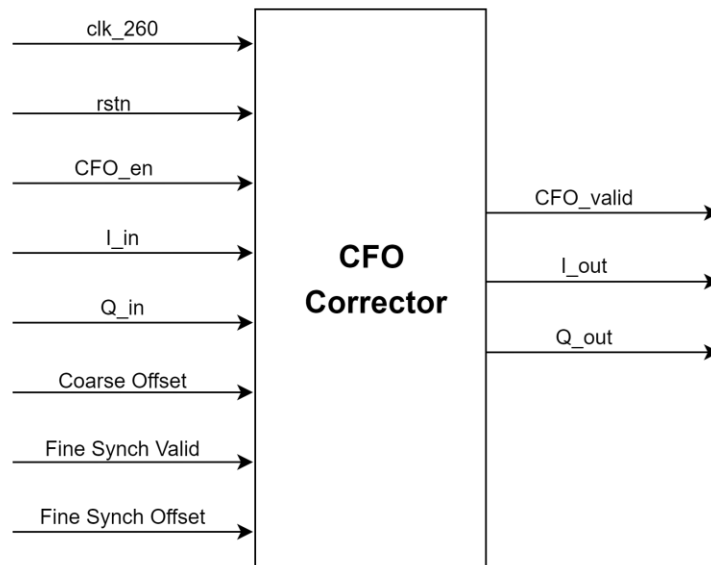


Figure [44]: CFO Corrector Top Module

Table [11]: CFO Corrector Interface Table

Signal Name	Direction	Width	Description
clk_260	Input	1	3.84 MHz clock signal
rstn	Input	1	Global reset signal
CFO_en	Input	1	Enable Signal that indicates the start block's operation
I_in	Input	16	Real serial input samples
Q_in	Input	16	Imaginary serial input samples
Coarse Offset	Input	19	Estimated Carrier Frequency Offset from Coarse Synchronizer

Fine Synch Valid	Input	1	Valid Signal indicating the validity of Fine Synchronizer offset
Fine Synch Offset	Input	19	Estimated Fine Synchronizer Offset
CFO_valid	Output	1	Valid Signal indicating the validity of the output samples after correction
I_out	Output	16	Real serial output samples
Q_out	Output	16	Imaginary serial output samples

### 3.3.2. Detailed Hardware

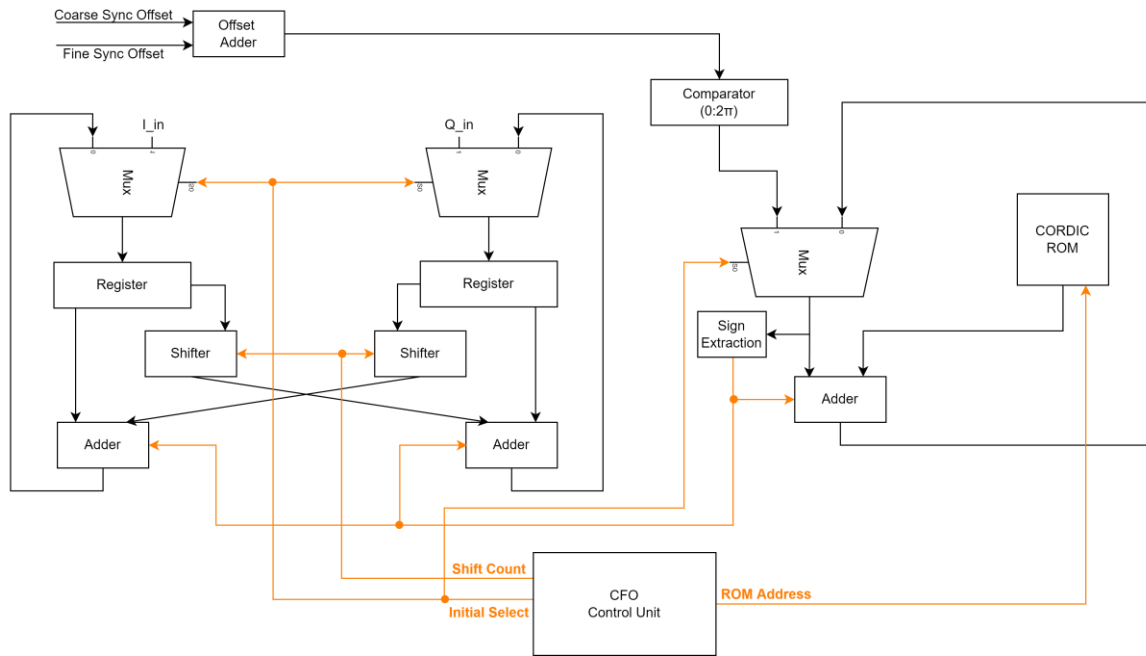


Figure [45]: CFO Corrector Detailed Hardware

### 3.3.3. Design Challenges and Solutions

#### 3.3.3.1. Area Utilization

There is a trade-off between CFO Corrector’s area and latency. Expanded version of a CORDIC Unit could be implemented by using 15 parallel stages and output could be obtained in one clock cycle. Nevertheless, this very low latency will be redundant as CFO Corrector samples a new input every 8 clock cycles coming from Downsampler. So, we decided to go with an iterative implementation by only using one stage and reusing the same hardware for all CORDIC steps and operating at double the frequency. Resulting in no wasted clock cycles and 93.5% improvement in area.

### 3.3.4. Synthesis Results

Utilization		Post-Synthesis   Post-Implementation		
				Graph   Table
Resource	Estimation	Available		Utilization %
LUT	326	53200		0.61
FF	112	106400		0.11
DSP	2	220		0.91
IO	107	200		53.50
BUFG	1	32		3.13

Figure [46]: CFO Corrector Synthesis Utilization

### 3.4. FFT Engine

#### 3.4.1. Top Module

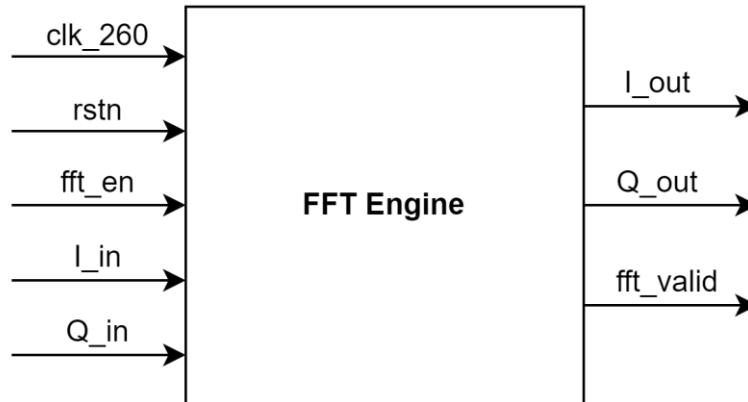


Figure [47]: FFT Top Module

Table [12]: FFT Engine Interface Table

Signal Name	Direction	Width	Description
clk_260	Input	1	3.84 MHz clock signal
rstn	Input	1	Global reset signal
cprds_en	Input	1	Enable Signal that indicates the start block's operation
I_in	Input	16	Real serial input samples
Q_in	Input	16	Imaginary serial input samples
cprds_valid	Output	1	Valid Signal indicating the validity of the output samples
I_out	Output	16	Real serial output samples
Q_out	Output	16	Imaginary serial output samples

#### FFT Specifications:

- 16-point processing
- Discrimination in Frequency (DIF)
- SDF Architecture
- Radix  $2^2$  Algorithm

#### Data flow through stages:

At first, 16-time domain samples coming from CFO Corrector are stored in  $8 \times 4$  memory and to improve system latency the first stage will start to operate as soon as the 9<sup>th</sup> sample is stored in the 1<sup>st</sup> stage's memory. Output of first stage will propagate to 2<sup>nd</sup> stage, and like in 1<sup>st</sup> stage, 2<sup>nd</sup> stage will start operating as soon as the 5<sup>th</sup> output from stage 1 arrives. This will also happen for 3<sup>rd</sup> and 4<sup>th</sup> stage until QPSK symbols begin to show at the output serially one by one. Block's latency is 16 clock cycle, once the pipeline is filled, a QPSK symbol will be ready every one clock cycle.

### 3.4.2. Detailed Hardware

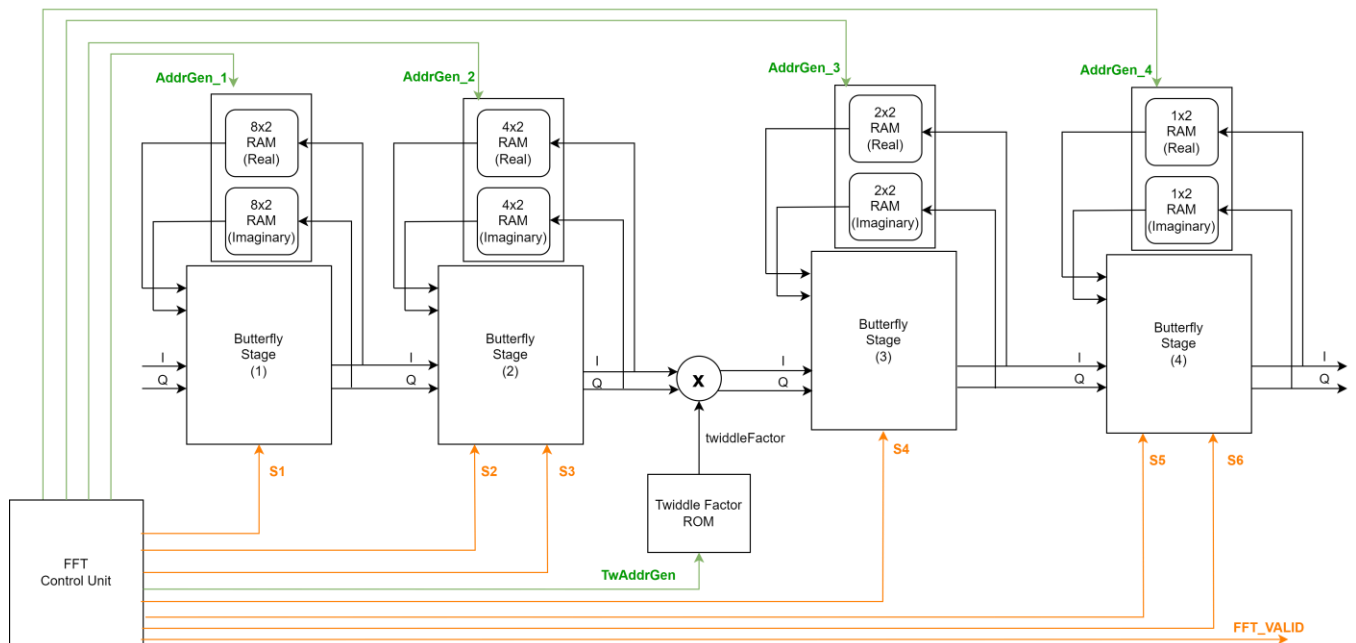


Figure [48]: FFT Engine Detailed Hardware

Regarding DIF architectures, data widths increase linearly as delay-line memory depths decrease exponentially. This means that restraining bit growth in DIF FFT processors results in minimal savings as compared to the potential impacts of quantization. Memories used to implement delay-lines for SDF FFT processors do not require random access. A straightforward sequential access scheme in which read and write pointers are simultaneously incremented for each pair of complex data samples for all four stages.

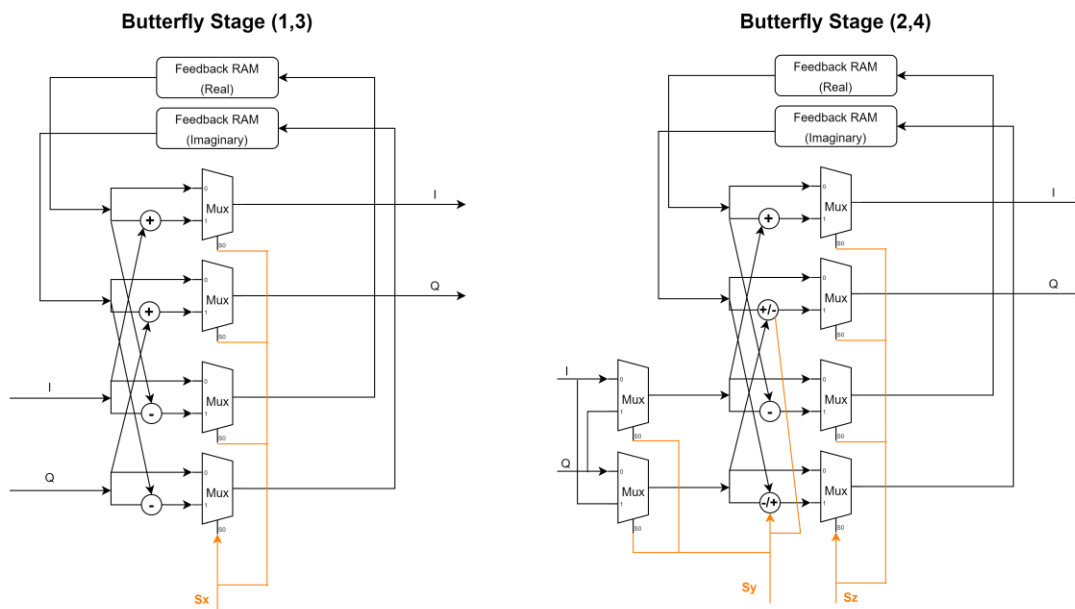


Figure [49]: Butterfly Hardware Structure

As shown in butterfly hardware structure, BF (1,3) and BF (2,4) are identical except that BF (2,4) have some added logic to perform a  $\pm j$  multiplication without the need of a complex multiplier. This is done by adding a multiplexing level to swap between Real and Imaginary stage inputs, and a control signal coming from control unit to invert the sign in the butterfly adders.

In the Radix-2<sup>2</sup> SDF architecture, a twiddle multiplication stage is implemented after every two butterfly stages. At every twiddle stage, a complex hardware multiplier is used to multiply each data sample by a corresponding complex twiddle coefficient of unit magnitude. The product is then truncated down to the bit width of the data stream before entering the subsequent butterfly stage.

### 3.4.3. Synthesis Results

Utilization		Post-Synthesis		Post-Implementation
				Graph   Table
Resource	Estimation	Available	Utilization %	
LUT	719	53200	1.35	
LUTRAM	96	17400	0.55	
FF	192	106400	0.18	
DSP	4	220	1.82	
IO	68	200	34.00	
BUFG	1	32	3.13	

Figure [50]: FFT Synthesis Utilization

### 3.5. Resource Demapper

#### 3.5.1. Top Module

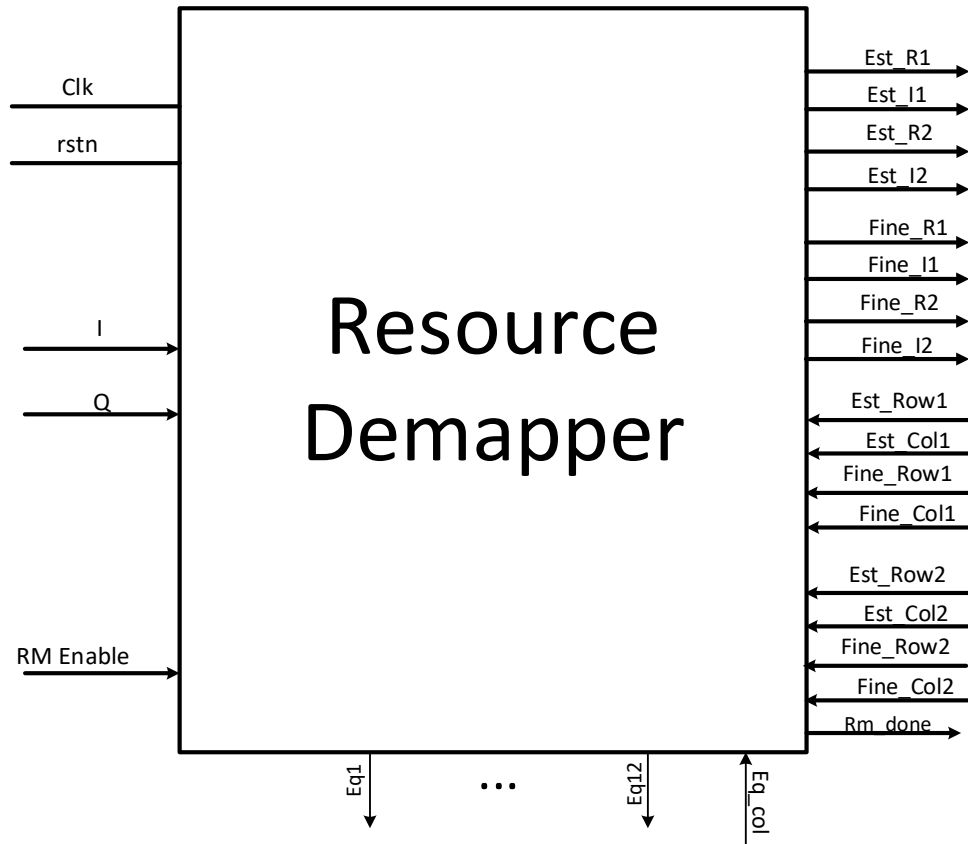


Figure [51]: Resource Demapper Top Module

Table [13]: Resource Demapper Interface Table

Signal Name	Direction	Width	Description
clk	Input	1	260ns clock signal
Rstn	Input	1	Active low reset
I	Input	16	Real part of received sample from fft
Q	Input	16	Imaginary part of received sample from fft
rmEnable	Input	1	Block enable from the fft
Eq_col	Input	4	Number of the column to be equalized
Est_row1	Input	4	The row of the needed pilot by the estimator
Est_col1	Input	4	The column of the needed pilot by the estimator
Est_row2	Input	4	The row of the needed pilot by the estimator
Est_col2	Input	4	The column of the needed pilot by the estimator
Fine_row1	Input	4	The row of the needed pilot by fine synchronizer
Fine_col1	Input	4	The column of the needed pilot by fine synchronizer
Fine_row2	Input	4	The row of the needed pilot by fine synchronizer
Fine_col2	Input	4	The column of the needed pilot by fine synchronizer

Est_R1	Output	16	Received pilot real part
Est_I1	Output	16	Received pilot imaginary part
Est_R2	Output	16	Received pilot real part
Est_I2	Output	16	Received pilot imaginary part
fine_R1	Output	16	Received pilot real part
fine_I1	Output	16	Received pilot imaginary part
fine_R2	Output	16	Received pilot real part
fine_I2	Output	16	Received pilot imaginary part
Eq1 to Eq12 R	Output	16	Received symbol's real part to be equalized
Eq1 to Eq12 I	Output	16	Received symbol's imaginary part to be equalized
Rm_done	Output	1	Signal indicates that storing is done

### 3.5.2. Detailed Hardware

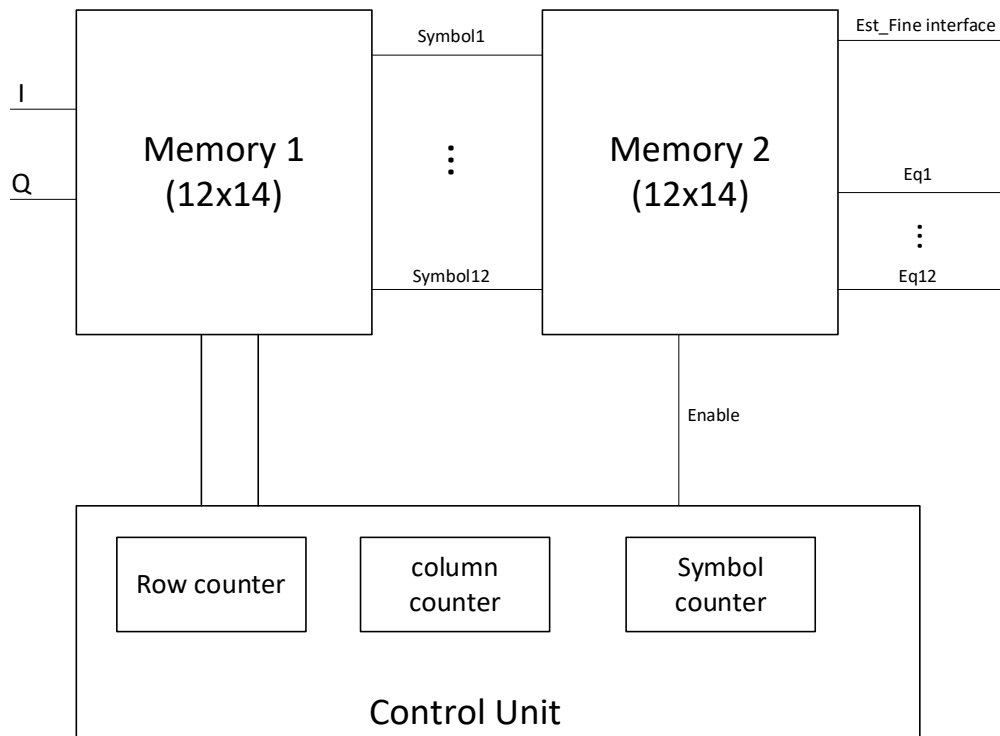


Figure [52]: Resource demapper detailed hardware

The block consists of two memories 12x14 each to store the whole subframe which consists of 12 subcarriers and 14 OFDM symbol, the 1<sup>st</sup> memory takes the output of the FFT sample by sample (QPSK symbol) constructing an OFDM symbol every 16 cycles then after a complete OFDM symbol we start to fill the second column in the memory.

The row and column counter are used to keep tracking how many places are filled and also used as addresses for the data in the first memory then the symbol counter is used to count the number of OFDM symbol transferred from the 1<sup>st</sup> memory to the 2<sup>nd</sup> memory.



After storing the whole subframe (14 OFDM symbol) the 1<sup>st</sup> memory raises the write enable of the 2<sup>nd</sup> memory and transfer to it symbol by symbol till the second memory is full and store the whole subframe, while the 2<sup>nd</sup> memory stores the subframe the 1<sup>st</sup> memory will keep storing in the new subframe.

By this we guarantee the stability of data in the memory within our processing time

### 3.5.3. Design Challenges and Solutions

#### 3.5.3.1. Timing

We need to know the processing time which is the time that we need the data to be constant in the memory, so this time determine our memory width.

$$time = (NRS \text{ generation latency})(clk) + (channel \text{ estimation latency})(clk) + (equalizater \text{ latency})(clk)$$

$$time = 6424 \times 130ns + 7 \times 520ns + 1 \times 520ns \cong 0.85ms$$

Knowing that the subframe time is around 0.95ms so we need to keep the whole subframe constant using the 12 × 14 memories

#### 3.5.3.2. Removing Dummy

The data output from our FFT has 4 dummy samples. The dummy is inserted at the Tx because we use 16-point FFT while the OFDM symbol contain only 12 sample so 4 dummy samples are added to work with the 16-point FFT.

There was a solution of storing the whole received samples letting the 1<sup>st</sup> memory to be 16x14 memory which we considered as high overhead because this gives 4 dummy samples in 14 symbol each of 16bit real and 16 imaginary and this is a total of  $4 * 14 * 16 * 2 = 1792 \text{ bit}$ .

The dummy samples output from the fft will not be stored as we know when they are coming as they are at well-known places so we know when they will come and disable the write enable of the memory so as not to store them.

#### 3.5.3.3. Ordering

The data output from the FFT is out of order as the FFT uses DIF so its input is in order but the output is out of order.

Instead of using complex control to control the storing in different order than the order the data comes in with we decided to normally store the data in the 1<sup>st</sup> memory then while transferring from the 1<sup>st</sup> memory to the 2<sup>nd</sup> memory we use wiring to do the needed ordering. By that the data in the 2<sup>nd</sup> memory are in the required normal order without adding complexity of control.

Table [14]: Ordering table

Input	Stored order
0	0
1	8
2	4
3	2
4	6
5	1
6	9
7	13
8	3
9	11
10	7
11	15

### 3.5.4. Results

#### 3.5.4.1. Synthesis Result

Resource	Estimation	Available	Utilization %
LUT	9875	64000	15.43
FF	11166	128000	8.72
IO	584	400	146.00
BUFG	1	32	3.13

Figure [53]: Resource Demapper Synthesis result

### 3.6. Channel Estimation

#### 3.6.1. Top Module

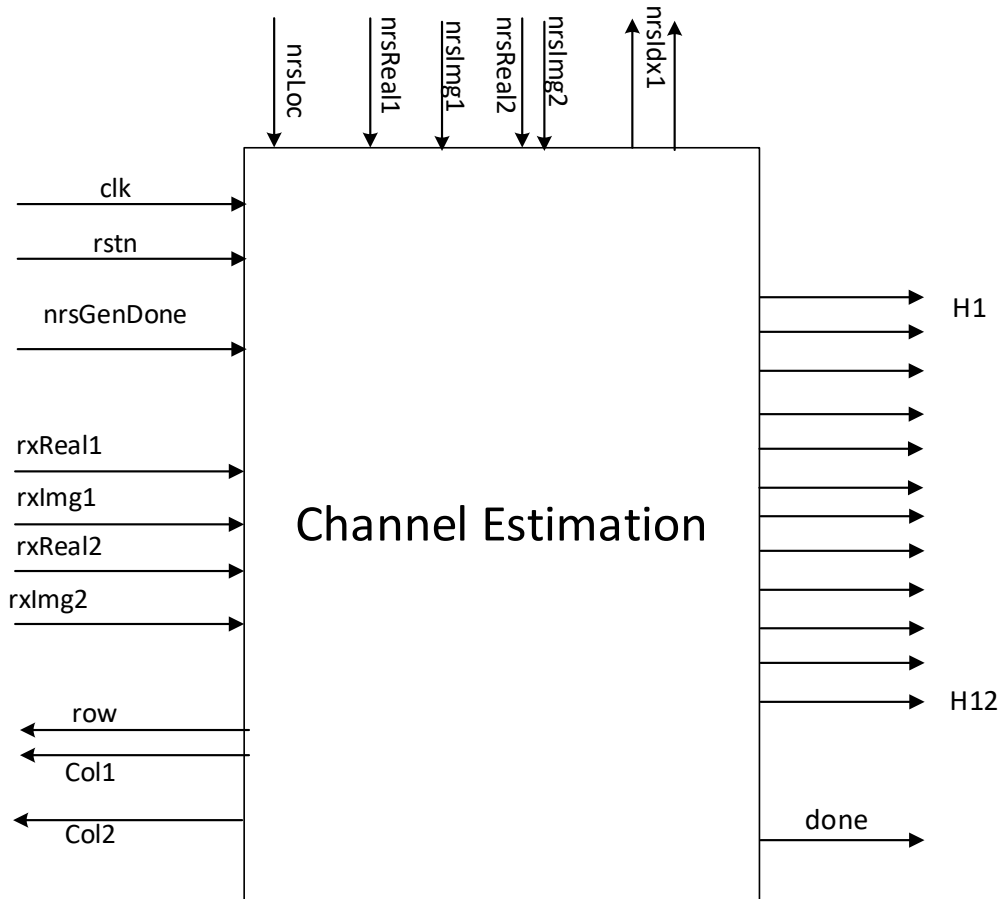


Figure [54]: Channel Estimation Top Module

Table [15]: Channel Estimation Interface Table

Signal Name	Direction	Width	Description
Clk	Input	1	520ns clock signal
Rstn	Input	1	Active low reset signal
nrsGenDone	Input	1	Signal indicate that pilot generation has finished
rxReal1	Input	16	Real part of the received pilot
rxImg1	Input	16	Imaginary part of the received pilot
rxReal2	Input	16	Real part of the received pilot
rxImg2	Input	16	Imaginary part of the received pilot
nrsLoc	Input	4	Index that we get from the NRS index generator
nrsReal1	Input	16	Real part of locally generated pilot
nrslmg1	Input	16	Imaginary part of locally generated pilot
nrsReal2	Input	16	Real part of locally generated pilot
nrslmg2	Input	16	Imaginary part of locally generated pilot

nrsIdx1	Output	3	Index used to access NRS index generator memory
nrsIdx2	Output	3	Index used to access NRS index generator memory
Row	Output	4	Row of the received pilot in the resource block
Col1	Output	4	Column of the received pilot in the resource block
Col2	Output	4	Column of the received pilot in the resource block
H1 ... H12 Real	Output	16	Estimated real part
H1 ... H12 Img	Output	16	Estimated imaginary part
done	Output	1	Signal verifies that estimation is done

### 3.6.2. Detailed Hardware

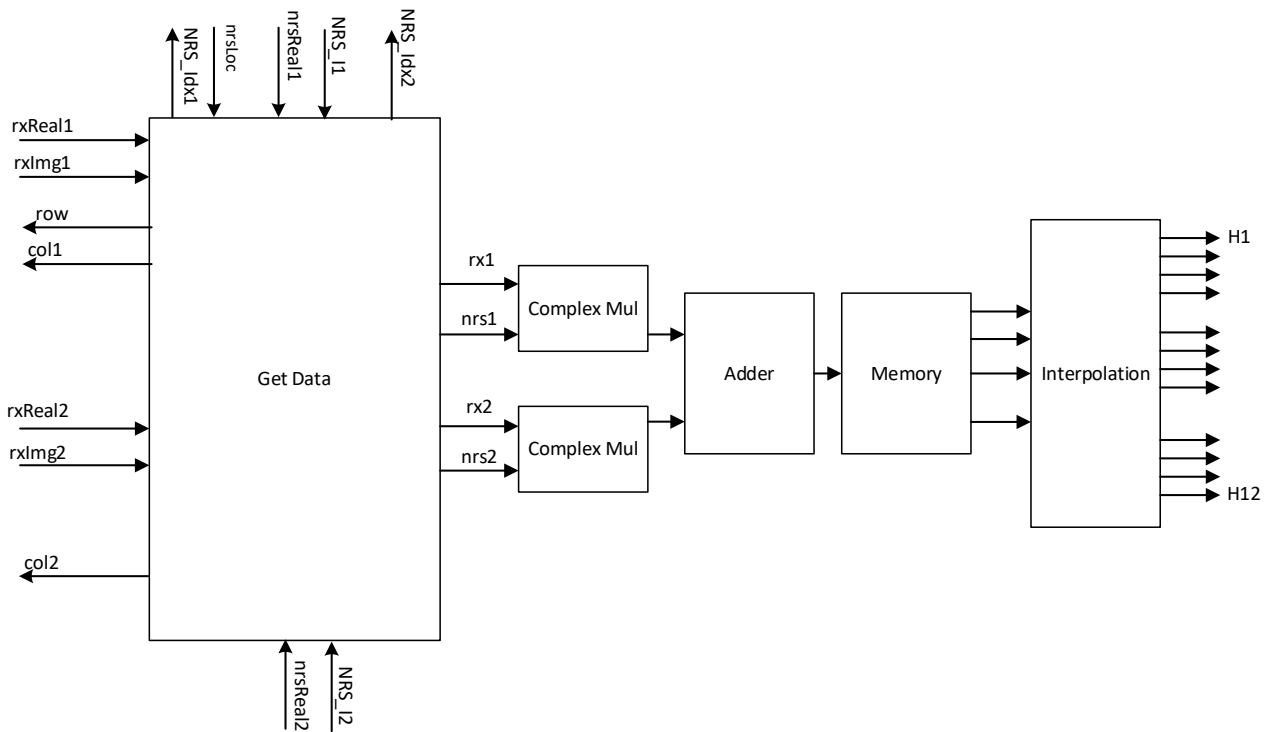



Figure [55]: Channel Estimation detailed hardware

The estimation process is done through the following steps:

- 1- We gather the needed data which is the received pilots (noisy) and the locally generated pilots (noiseless) the received are stored in the resource demapper and the generated in the NRS generation memory.
- 2- Calculate the channel frequency response by dividing which is implemented as multiplication by conjugate
- 3- Getting the average and store them in the memory
- 4- A combinational interpolation block to interpolate between the calculated four values to get the twelve-channel estimate.

## 3.6.3. Results

## 3.6.3.1. Matlab vs RTL

 12x1 complex double

	1
1	-2.1200e+02 + 1.0380e+03
2	9.3200e+02 + 2.3140e+03
3	2.0770e+03 + 3.5890e+03
4	3.2220e+03 + 4.8650e+03
5	-2.9400e+02 + 4.7510e+03
6	-3.8100e+03 + 4.6370e+03
7	-7.3250e+03 + 4.5240e+03
8	-4.2700e+03 + 2.5890e+03
9	-1.2140e+03 + 6.5300e+02
10	1.8410e+03 - 1.2820e+03
11	4.8960e+03 - 3.2170e+03
12	7.9520e+03 - 5.1520e+03

Figure [57]: Matlab estimates

























>	 h1real[15:0]	-214
>	 h1img[15:0]	1038
>	 h2real[15:0]	932
>	 h2img[15:0]	2317
>	 h3real[15:0]	2078
>	 h3img[15:0]	3595
>	 h4real[15:0]	3219
>	 h4img[15:0]	4865
>	 h5real[15:0]	-297
>	 h5img[15:0]	4759
>	 h6real[15:0]	-3819
>	 h6img[15:0]	4645
>	 h7real[15:0]	-7326
>	 h7img[15:0]	4524
>	 h8real[15:0]	-4280
>	 h8img[15:0]	2593
>	 h9real[15:0]	-1219
>	 h9img[15:0]	654
>	 h10real[15:0]	1839
>	 h10img[15:0]	-1281
>	 h11real[15:0]	4900
>	 h11img[15:0]	-3219
>	 h12real[15:0]	7961
>	 h12img[15:0]	-5158

Figure [56]: RTL estimates

### 3.6.3.2. Synthesis Results

Resource	Estimation	Available	Utilization %
LUT	1553	64000	2.43
FF	169	128000	0.13
DSP	16	160	10.00
IO	538	400	134.50
BUFG	1	32	3.13

*Figure [58]: Channel Estimation Synthesis results*

### 3.7. NRS Value Generator

#### 3.7.1. Top module

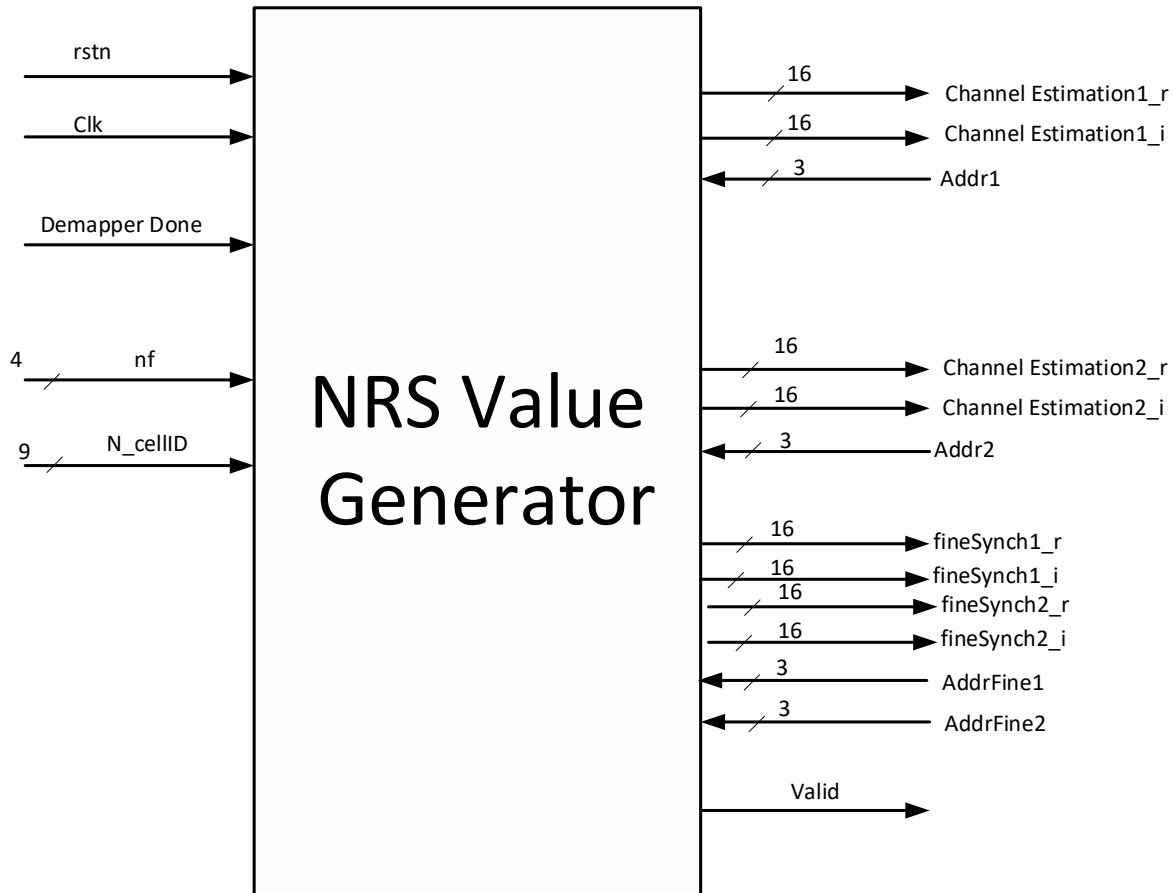


Figure [59]: NRS Value Generator top module

Table [16]: NRS Value Generator interface table

Signal Name	Direction	Width	Description
Clk	Input	1	130ns clock signal
Rstn	Input	1	Active low reset signal
demapperDone	Input	1	Signal indicates that storing subframe is done
Nf	Input	4	Subframe number
N_cellID	Input	9	Cell ID
Addr1	Input	3	Address of first pilot from channel estimation
Addr2	Input	3	Address of second pilot channel estimation
Addrfine1	Input	3	Address of first pilot from fine synchronization
Addrfine2	Input	3	Address of second pilot from fine synchronization
ChannelEstimation1_r	Output	16	First pilot real part
ChannelEstimation1_i	Output	16	First pilot imaginary part
ChannelEstimation2_r	Output	16	Second pilot real part
ChannelEstimation2_r	Output	16	Second pilot imaginary part

fineSynch1_r	Output	16	First pilot real part
fineSynch1_i	Output	16	First pilot imaginary part
fineSynch2_r	Output	16	Second pilot real part
fineSynch2_i	Output	16	Second pilot imaginary part
Valid	Output	1	Signal verifies that generation is done

### 3.7.2. Detailed Hardware

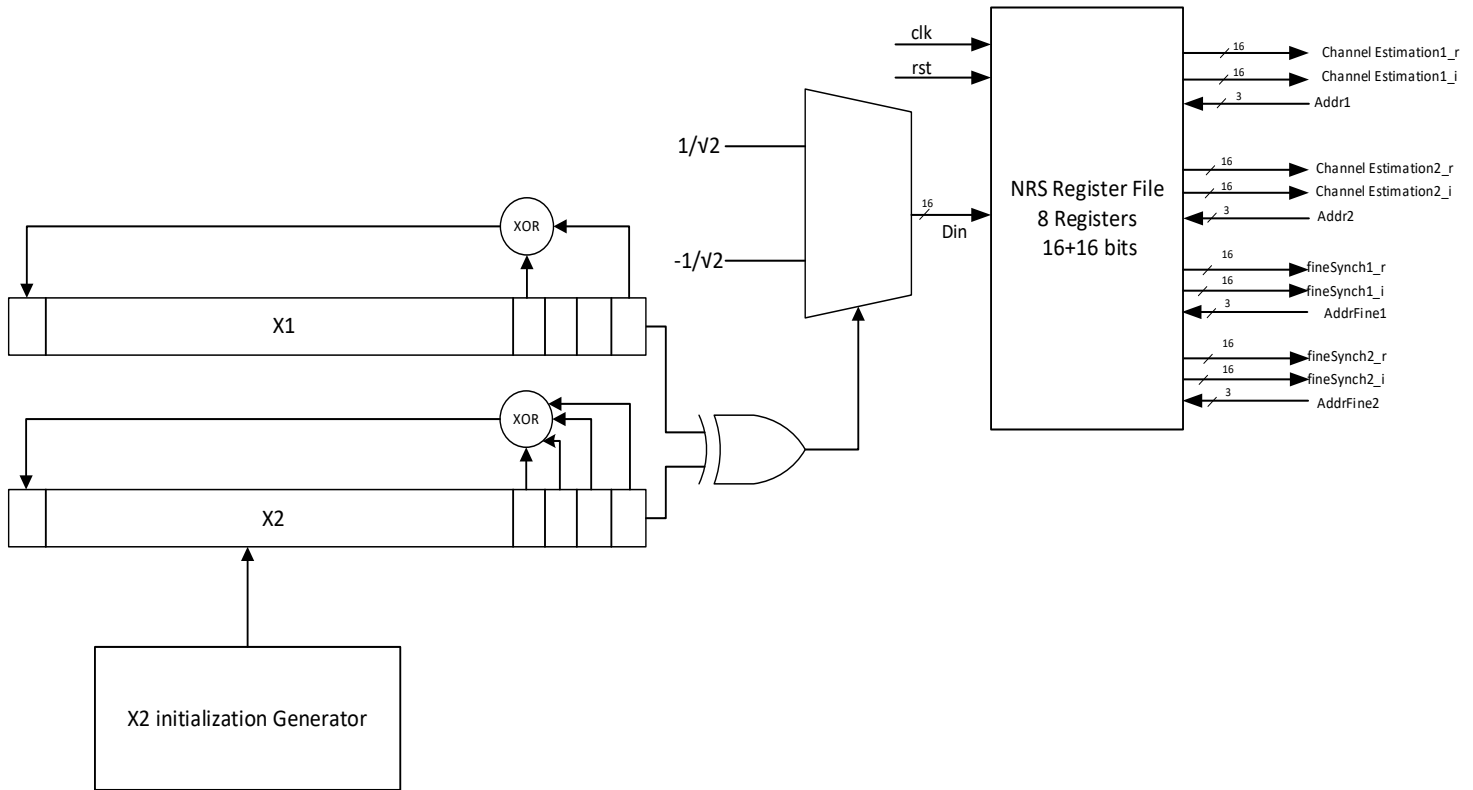


Figure [60]: NRS Value Generator detailed hardware

The pilot value is either  $\frac{1}{\sqrt{2}}$  or  $-\frac{1}{\sqrt{2}}$  depending on the value of the golden sequence. So, x2 initialization generator generates the initializing sequence for x2 then both are XORed giving the golden sequence to choose which value is to be stored in the register file. Other blocks will interface with this register file accessing it with the required address to extract the needed generated pilot.



### 3.7.3. Results

#### 3.7.3.1. Matlab vs RTL

For subframe number = 0 and N\_cellID = 1

	1
1	0.7071 + 0.7071i
2	-0.7071 + 0.7071i
3	-0.7071 - 0.7071i
4	0.7071 + 0.7071i
5	0.7071 - 0.7071i
6	-0.7071 - 0.7071i
7	0.7071 - 0.7071i
8	0.7071 + 0.7071i

Figure [61]: MATLAB function vs Our function

▼	realPilots[0:7][15:0]	02d4,fd2c,fd2c,0	Array
>	[0][15:0]	724	Array
>	[1][15:0]	-724	Array
>	[2][15:0]	-724	Array
>	[3][15:0]	724	Array
>	[4][15:0]	724	Array
>	[5][15:0]	-724	Array
>	[6][15:0]	724	Array
>	[7][15:0]	724	Array
▼	imagPilots[0:7][15:0]	02d4,02d4,fd2c,0	Array
>	[0][15:0]	724	Array
>	[1][15:0]	724	Array
>	[2][15:0]	-724	Array
>	[3][15:0]	724	Array
>	[4][15:0]	-724	Array
>	[5][15:0]	-724	Array
>	[6][15:0]	-724	Array
>	[7][15:0]	724	Array

Figure [62]: RTL results

### 3.7.3.2. Synthesis Results

Resource	Utilization	Available	Utilization %
LUT	190	64000	0.30
FF	125	128000	0.10
DSP	1	160	0.63
IO	157	400	39.25
BUFG	1	32	3.13

*Figure [63]: NRS Values Generator Synthesis results*

### 3.8. NRS Index Generator

#### 3.8.1. Top module

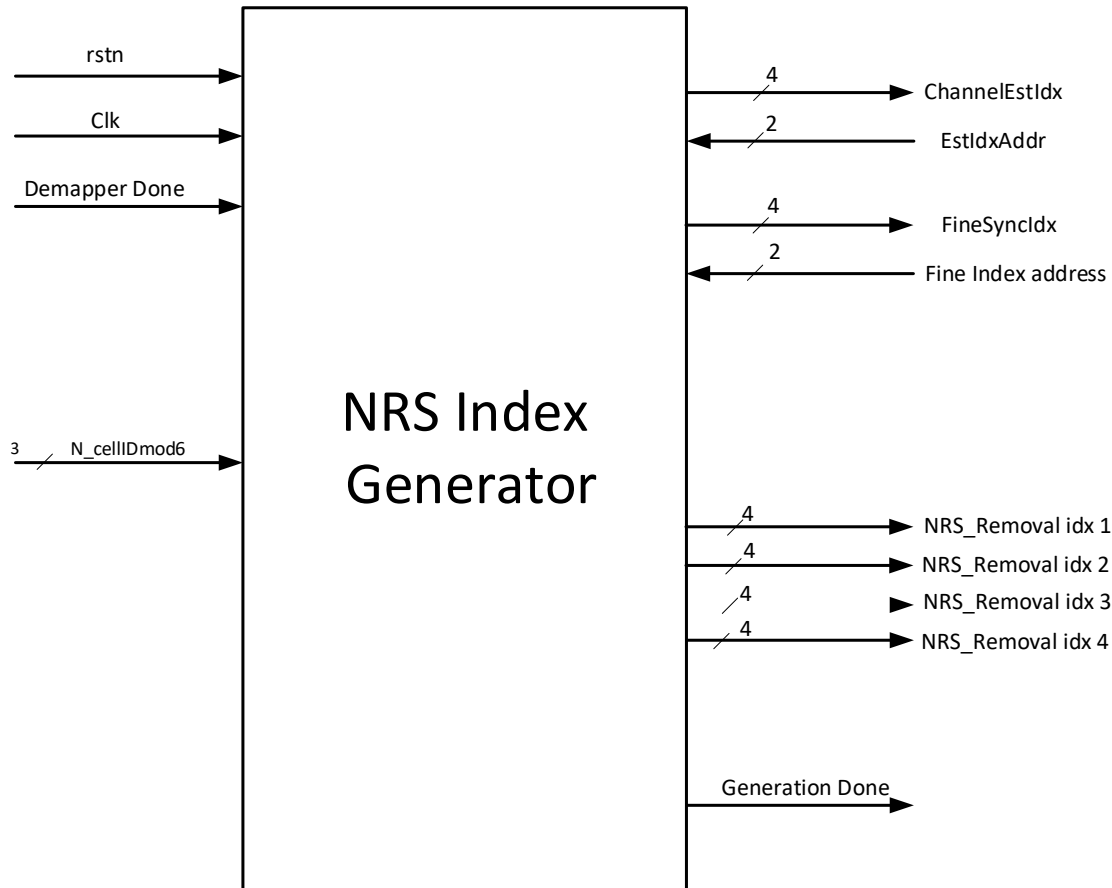


Figure [64]: NRS Index Generator top module

Table [17]: NRS Index Generator interface table

Signal Name	Direction	Width	Description
Clk	Input	1	520ns clock signal
Rstn	Input	1	Active low reset signal
demapperDone	Input	1	Signal indicates that storing subframe is done
N_cellIDmod6	Input	3	Cell ID modulus 6
EstIdxAddr	Input	2	Address of pilot needed by channel estimation
FineSyncAddr	Input	2	Address of pilot needed by fine synchronization
ChannelEstIdx	Output	4	Index of the pilot needed by channel est. in RB
FineSyncIdx	Output	4	Index of the pilot needed by fine sync. in RB
NRSremovalIdx1	Output	4	Index of first pilot to be given to NRS removal
NRSremovalIdx2	Output	4	Index of second pilot to be given to NRS removal
NRSremovalIdx3	Output	4	Index of third pilot to be given to NRS removal
NRSremovalIdx4	Output	4	Index of fourth pilot to be given to NRS removal
GenerationDone	Output	1	Signal verifies that index generation is done

### 3.8.2. Detailed hardware

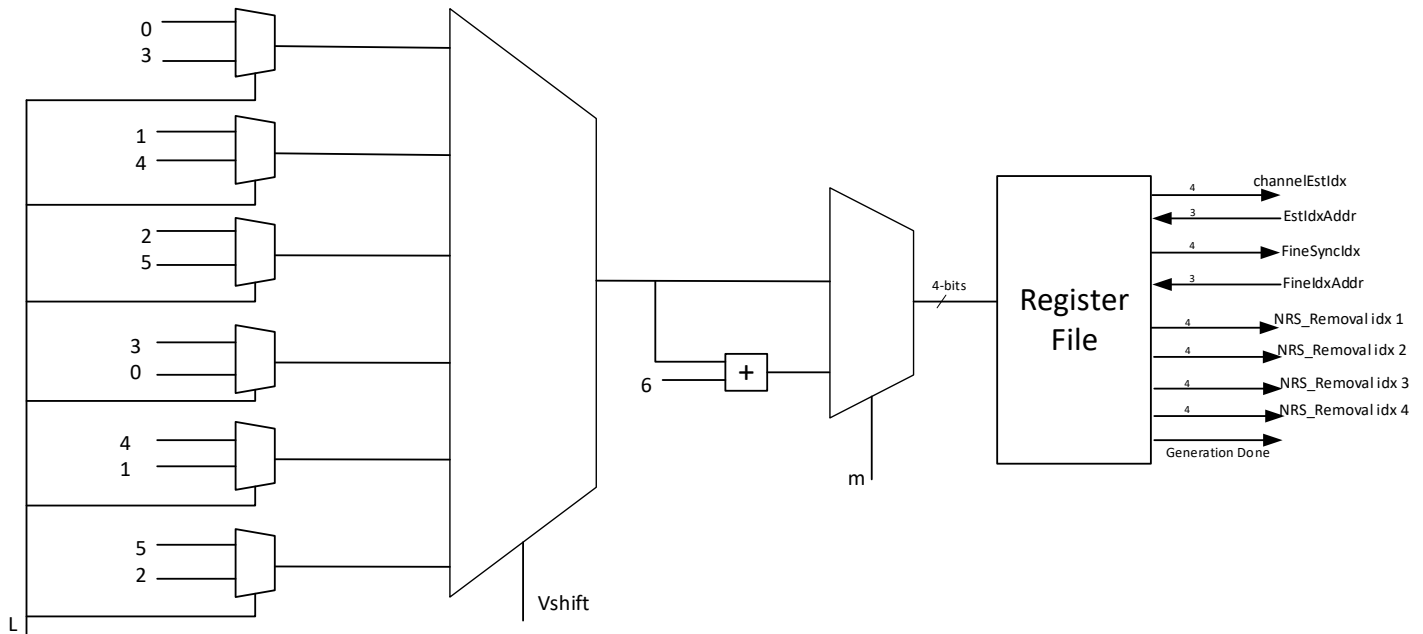


Figure [65]: NRS Index Generator detailed hardware

The design intends to implement the equations in the standard to calculate the value of the indices to extract them from the subframe

### 3.8.3. Design Challenges and Solutions

#### 3.8.3.1. Calculations

Instead of using adders or any arithmetic block the design is implemented as multiplexer this is because the pilots are always in OFDM symbol number 5 or 6 and the rest of the equation are all set of choices from certain values

By that we reduce the consumed power using multiplexers instead of arithmetic units.

#### 3.8.3.2. Memory

As the pilots are always in pair per subcarrier and always at OFDM symbol 5 or 6. So, we only need to know four values of the four subcarriers and there is no need to store eight values as every subcarrier of the calculated four has two pilots also no need to store the number of OFDM symbol as it is well known to any block in the system that the pilots are at OFDM symbol 5 and 6.

By that we have used half the size of the memory storing four numbers other than eight.

### 3.8.4. Results

#### 3.8.4.1. Matlab vs RTL

For subframe number = 1 and N\_cellID = 0

8x3 double		
	1	2
1	0	5
2	6	5
3	3	6
4	9	6

k1	0
k2	6
k3	3
k4	9
l1	5
l2	6

Figure [66]: MATLAB function vs Our function

idxMem[0:3][3:0]	0,6,3,9
> [0][3:0]	0
> [1][3:0]	6
> [2][3:0]	3
> [3][3:0]	9

Figure [67]: RTL results

#### 3.8.4.2. Synthesis Results

Resource	Estimation	Available	Utilization %
LUT	17	230400	0.01
FF	20	460800	0.01
IO	35	360	9.72
BUFG	1	544	0.18

Figure [68]: NRS Index Generator Synthesis results

### 3.9. Channel Equalizer

#### 3.9.1. Top module

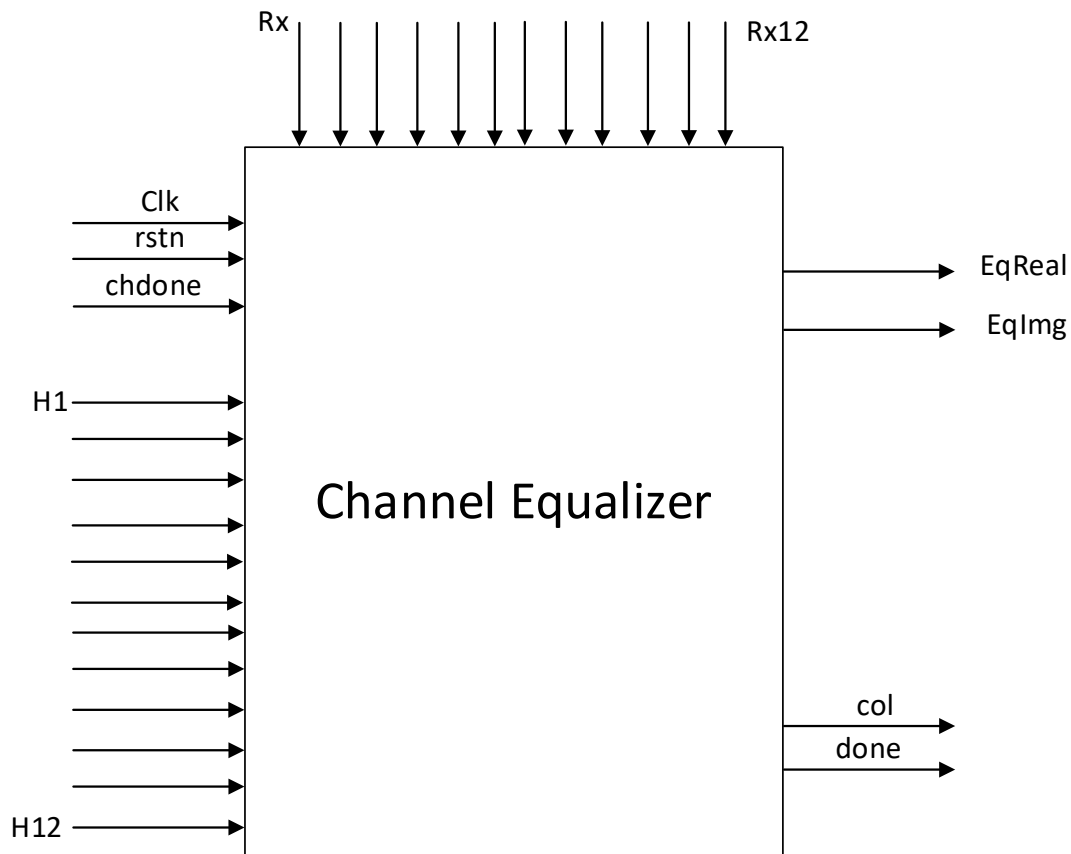


Figure [69]: Channel Equalizer top module

Table [18]: Channel Equalizer interface table

Signal Name	Direction	Width	Description
Clk	Input	1	520ns clock signal
Rstn	Input	1	Active low reset signal
chDone	Input	1	Signal indicates that channel estimation is done
H1 ... H12	Input	16	Channel estimates per subcarrier
Rx1 ... Rx12	Input	16	OFDM symbol to be equalized
Col	Output	4	Number of required OFDM symbol to be equalized
EqReal	Output	12	MSB of real part of the equalized symbol
EqImg	Output	12	MSB of imaginary part of the equalized symbol
Done	Output	1	Signal indicates that symbol has equalized

## 3.9.2. Detailed Hardware

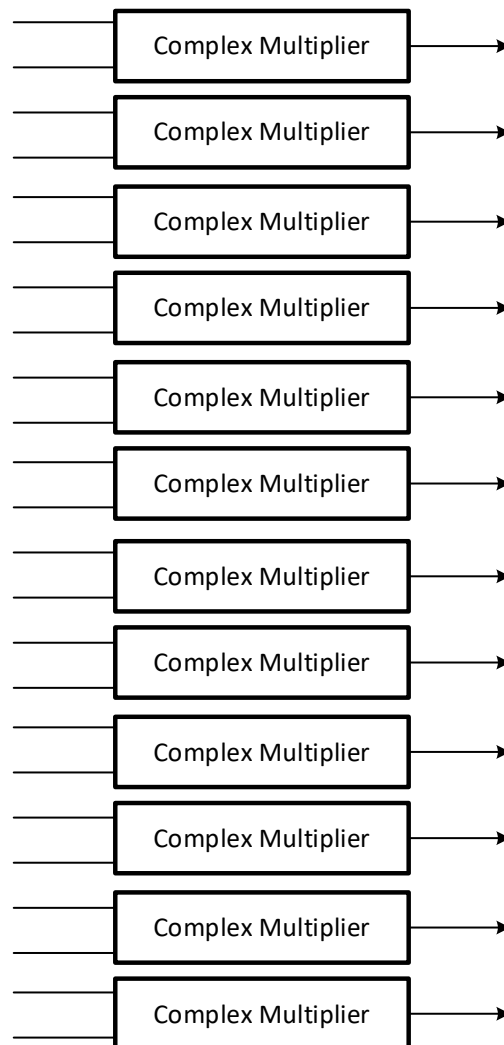


Figure [70]: Channel Equalizer detailed hardware

The design is a set of twelve complex multiplier (conjugate) to equalize the data symbols by dividing them by the channel estimated value.

There is a counter that counts the number of equalized OFDM symbols, the value of the counter is sent to the resource demapper to extract the need OFDM symbol to equalized.

Also, this counter value will be used to detect the last column as we need to know when we reached the last OFDM symbol to achieve the timing needed in Parallel to Serial block.

### 3.9.3. Design Challenges and Solutions

There was a challenge in communication between this block and parallel to serial block because the data are stored in the resource demapper for certain time which doesn't include the overhead of converting each symbol to serial and this conversion takes around 12 clock cycles.

The counter is passed to the parallel to serial and it gets registered there to be used as the storing time of RB is enough for all Symbols except the last one.

### 3.9.4. Results

#### 3.9.4.1. Matlab vs RTL

	1
1	-1.5360e+03 - 4.3010e+03i
2	-1.5545e+04 + 1.8665e+04i
3	9.1300e+02 - 1.0220e+03i
4	1.4462e+04 - 2.0280e+03i
5	8.5270e+03 - 1.0636e+04i
6	-2.6700e+02 - 4.1810e+03i
7	2.0200e+03 - 1.9694e+04i
8	6.8800e+02 + 7.6900e+02i
9	-3.0800e+02 + 5.5440e+03i
10	3.0752e+04 - 3.3890e+03i
11	-1.2190e+03 - 3.6500e+02i
12	1.9860e+03 - 2.1600e+03i

Figure [72]: Matlab equalized OFDM symbol

> eq1real[15:0]	-1537	Array
> eq1img[15:0]	-4301	Array
> eq2real[15:0]	-15544	Array
> eq2img[15:0]	18665	Array
> eq3real[15:0]	911	Array
> eq3img[15:0]	-1019	Array
> eq4real[15:0]	14459	Array
> eq4img[15:0]	-2031	Array
> eq5real[15:0]	8524	Array
> eq5img[15:0]	-10636	Array
> eq6real[15:0]	-263	Array
> eq6img[15:0]	-4177	Array
> eq7real[15:0]	2025	Array
> eq7img[15:0]	-19794	Array
> eq8real[15:0]	688	Array
> eq8img[15:0]	769	Array
> eq9real[15:0]	-308	Array
> eq9img[15:0]	5541	Array
> eq10real[15:0]	30744	Array
> eq10img[15:0]	-3384	Array
> eq11real[15:0]	-1221	Array
> eq11img[15:0]	-365	Array
> eq12real[15:0]	1983	Array
> eq12img[15:0]	-2157	Array
done	1	Logic

Figure [71]: RTL equalized OFDM symbol

#### 3.9.4.2. Synthesis results

Resource	Estimation	Available	Utilization %
LUT	391	230400	0.17
FF	33	460800	0.01
DSP	48	1728	2.78
IO	800	360	222.22
BUFG	1	544	0.18

Figure [73]: Equalizer Synthesis results



### 3.10. Parallel to Serial and NRS removal

#### 3.10.1. Top module

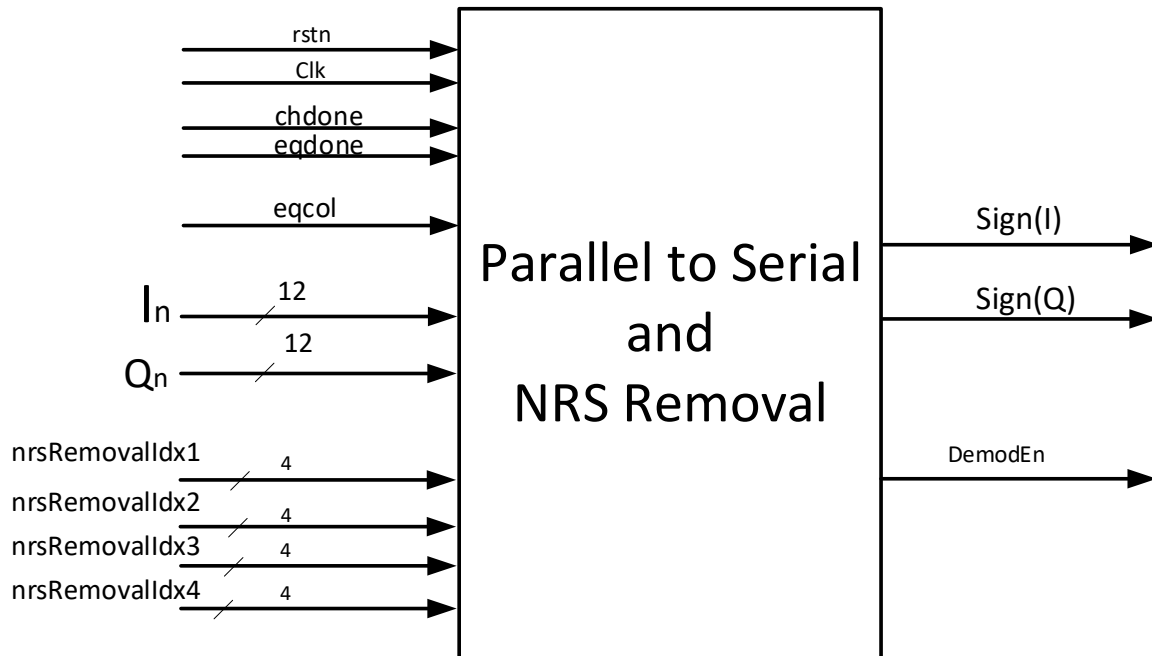


Figure [74]: Parallel to Serial and NRS removal top module

Table [19]: Parallel to Serial and NRS removal interface table

Signal Name	Direction	Width	Description
Clk	Input	1	520ns clock signal
Rstn	Input	1	Active low reset signal
chDone	Input	1	Signal indicates that channel estimation is done
Eqdone	Input	1	Signal indicates that channel equalization is done
In	Input	12	MSB of the real part of the equalized symbol (sign)
Qn	Input	12	MSB of the imaginary part of the equalized symbol (sign)
Eqcol	Input	4	Number of equalized OFDM symbol
nrsRemovalIdx1	Input	4	Index of first pilot to be removed
nrsRemovalIdx2	Input	4	Index of second pilot to be removed
nrsRemovalIdx3	Input	4	Index of third pilot to be removed
nrsRemovalIdx4	Input	4	Index of fourth pilot to be removed
Signi	Output	1	Sign of real part
SignQ	Output	1	Sign of imaginary part
DemodEn	Output	1	Enable signal to bit processing indicate valid data

As the demodulation is hard demodulation so it needs only the sign of the QPSK symbol the equalizer send us 12 bits representing the sign of every QPSK symbol in the OFDM symbol. Here we take these bits in payload shift register and start outputting this bits in serial.

### 3.10.2. Design Challenges and Solutions

The main challenge was in handling the last OFDM symbol as the time of storing the subframe doesn't include converting it to serial data.

The time was sufficient to convert every OFDM symbol except for the last one for that the design has special registers to store the needed values for the last column.

We register the last set of QPSK symbols to be output in serial then manage to disable the enable after all the subframe has been converted.

### 3.10.3. Results

#### 3.10.3.1. Synthesis results

Resource	Estimation	Available	Utilization %
LUT	47	230400	0.02
FF	19	460800	0.01
IO	51	360	14.17
BUFG	1	544	0.18

Figure [75]: Parallel to Serial and NRS removal Synthesis results

## 3.11. Fine Synchronizer

### 3.11.1. Top Module

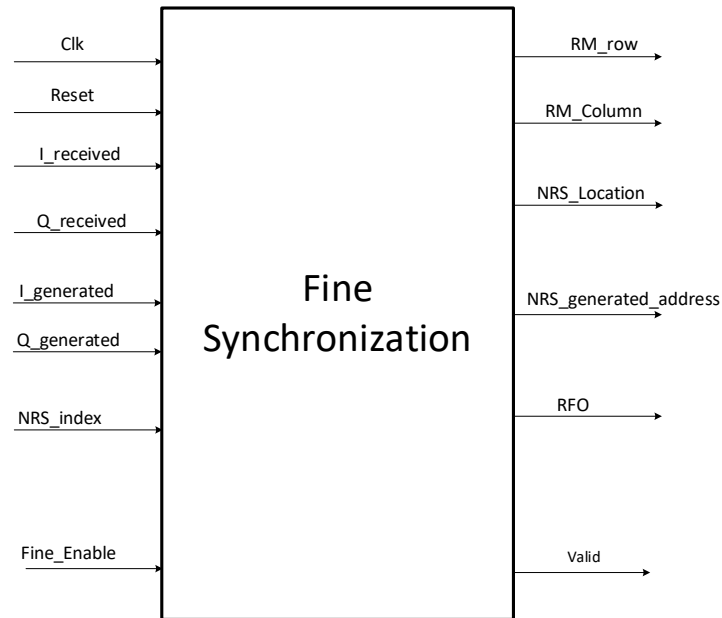


Figure [76]: Fine Synchronization Top Module

Table [20]: Fine Synchronization Interface Table

Signal Name	Direction	Width	Description
Clk_260	Input	1	3.84 MHz clock signal
Reset	Input	1	Global reset signal
Fine_Enable	Input	1	Enable signal for the Fine Synchronization module from the NRS Value Generator
I_received1	Input	16	Real value of the first-time domain received NRS signal
Q_received1	Input	16	Imaginary value of the first-time domain received NRS signal
I_received2	Input	16	Real value of the second-time domain received NRS signal
Q_received2	Input	16	Imaginary value of the second-time domain received NRS signal

I_generated1	Input	16	Real value of the first-time domain generated NRS signal
Q_generated1	Input	16	Imaginary value of the first-time domain generated NRS signal
I_generated2	Input	16	Real value of the second-time domain generated NRS signal
Q_generated2	Input	16	Imaginary value of the second-time domain generated NRS signal
NRS_index	Input	4	NRS index from the NRS Index Generator block
RM_row1	Output	4	Row address to the Resource De-Mapper to get the first received NRS
RM_Column1	Output	4	Column address to the Resource De-Mapper to get the first received NRS
RM_row2	Output	4	Row address to the Resource De-Mapper to get the second received NRS
RM_Column2	Output	4	Column address to the Resource De-Mapper to get the second received NRS
NRS_Location	Output	3	NRS Location to the NRS Index Generator block
NRS_generated_address1	Output	3	NRS address to the NRS Value Generator block to get the second received NRS
NRS_generated_address2	Output	3	NRS address to the NRS Value Generator block to get the second received NRS
RFO	Output	19	Residual Frequency offset to the CFO Block
valid	Output	1	Valid signal that verifies the integrity of the output bus data

### 3.11.2. Detailed Hardware

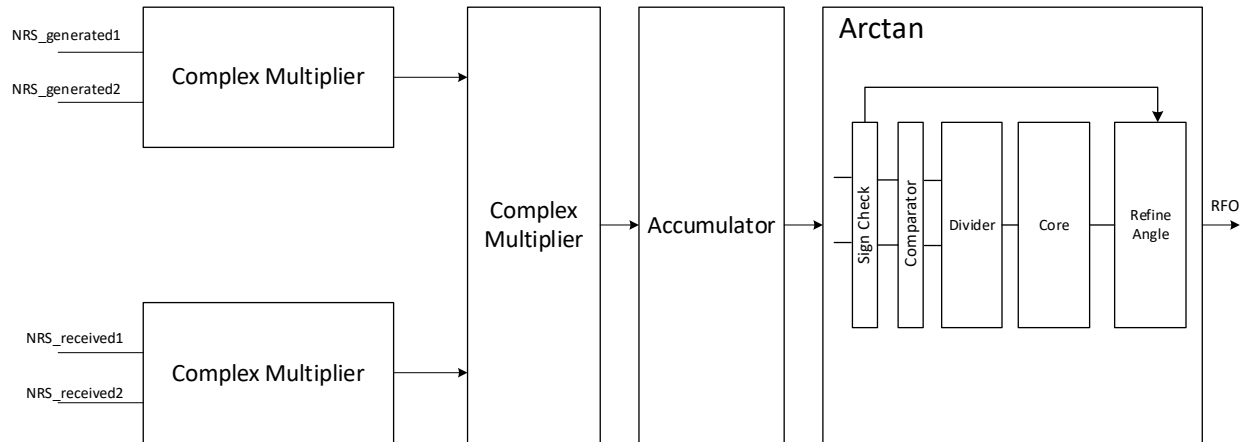


Figure [77]: Fine Synchronization Detailed Design

#### Fine Synchronization Description:

- Fetching each pair takes place as
  1. The block first sends the grid Location of this pair to the NRS address generation block.
  2. The NRS address generation block sends back the row indices of these pairs.
  3. The block then sends the NRS address in the Resource Element De-Mapper as row and column addresses in order to fetch the received NRS. And also sends the NRS address to the locally generated NRS memory in the NRS value generation block.
- Each pair of received NRS is complex multiplied as well as each pair of locally generated NRS signals
- The received complex product result is divided by the generated complex product result, but instead of division we use complex multiplication by using the complex conjugate. There is no need to account for the magnitude in this operation because the complex division will not affect the magnitude as it results in unity factor.
- The above operations are repeated for four iterations and each time the accumulator accumulates the resulting phase
- Frequency offset can be extract by using the Arctan function

### Arctan Synchronization Description:

The Low power implementation of the arctan is using the linear range of the arctan function in order to obtain the real arctan value.

$$z = [0,1]$$

$$\theta = [0:45]$$

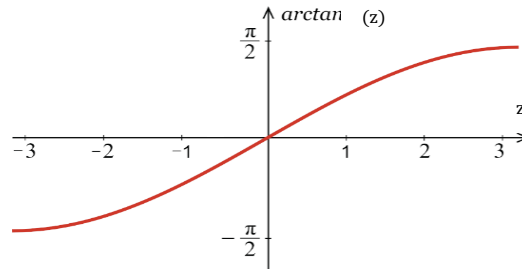


Figure [78]: Arctan Linear Range

The implementation of the arctan is divided into 5 stages

- Checking the sign of the real and imaginary parts of the complex quantity that we are calculating the arctan of and storing their sign to be used later in the Redefine angle stage.
- Passing the absolute values of the x (real part) and y (imaginary part), compare them and the smaller one is then used as numerator for the division operation while the greater is the denominator. This is in order to guarantee that the division z quantity is in range of [0,1].
- As the numerator and denominator of the division are identified in the comparator stage, this stage divides them using Non-restoring Algorithm
- Core is the main stage of this arctan which uses the value of this division to get the result of the angle from [0:45] using the following equations:

$$\tan^{-1} z = \begin{cases} 56z, & 0 < z < 0.25 \\ 50z + 1.5, & 0.25 < z < 0.5 \\ 40z + 6.5, & 0.5 < z < 0.75 \\ 32z + 13, & 0.75 < z < 1 \end{cases}$$

- If the numerator was the real part,  $x < y$  then  $\theta = 90 - \tan^{-1} z$
- If the numerator was the imaginary part,  $y < x$  then  $\theta = \tan^{-1} z$
- The resulted  $\theta$  lies in the first quadrature in range of [0:90]

- In the Refine angle block, final value of  $\theta_{final}$  is determined through the full range of [0:360] using the stored signs in the first stage using the following equations:

$$\theta_{final} = \begin{cases} \theta, & x + ve, y + ve \\ 180 - \theta, & x - ve, y + ve \\ \theta - 180, & x - ve, y - ve \\ -\theta, & x + ve, y - ve \end{cases}$$

The Calculated RFO value is a 19 bits result used by the CFO Correction block. 10 for the fraction and 9 for the integer.

### 3.11.3. Design Challenges and Solutions

The non-restoring algorithm divides absolute numbers and gives the final results based on this. So, it will not work well with the used fixed-point representation. The solution was to shift right the denominator by 10 as the fixed-point representation has 10 bits for the fraction and 6 bits for the integer. That's how it is guaranteed that the quotient which is the final division result is following the fixed-point representation.

### 3.11.4. Results

#### 3.11.3.1. MATLAB vs. RTL



Figure [79]: Fine Synchronizer RTL Results

138432 in fixed point representation. To convert it,  $138432/1024 = 135.1875$ .

#### 3.11.3.2. Synthesis Results

Utilization		Post-Synthesis   Post-Implementation		
		Graph   <b>Table</b>		
Resource	Estimation	Available	Utilization %	
LUT	473	230400	0.21	
FF	196	460800	0.04	
DSP	12	1728	0.69	
IO	180	360	50.00	
BUFG	1	544	0.18	

Figure [80]: Fine Synchronizer Synthesis Results

## 3.12. Demodulator

### 3.12.1. Top Module

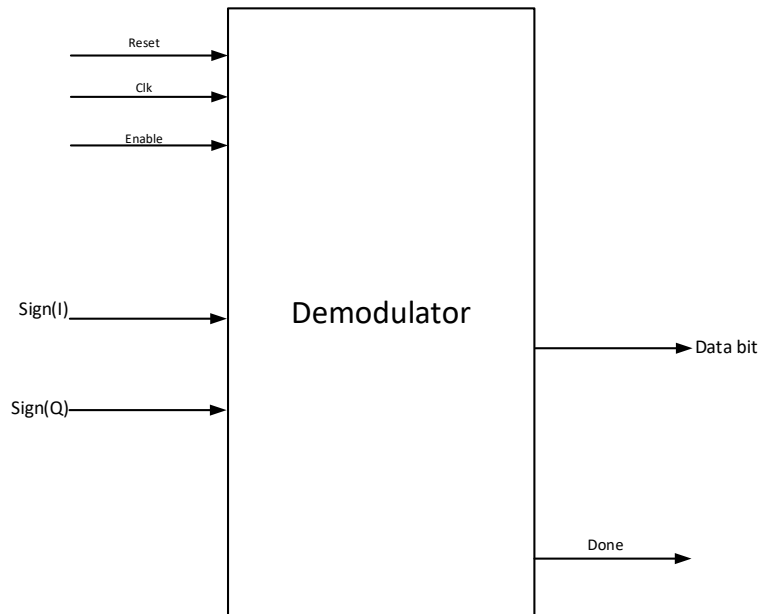


Figure [81]: Demodulator Top Module

Table [21]: Demodulator Interface Table

Signal Name	Direction	Width	Description
Clk_260	Input	1	3.84 MHz clock signal
Reset	Input	1	Global reset signal
Enable	Input	1	Enable signal for the Demodulator module to start operating
Sign_I	Input	1	sign of In-phase component received from the P/S block
Sign_Q	Input	1	sign of Quadrature component received from the P/S block
Data_bit	Output	1	Serial data bits output to descrambler
Done	Output	1	signal that verifies the integrity of the output bus data



### 3.12.2. Detailed Hardware

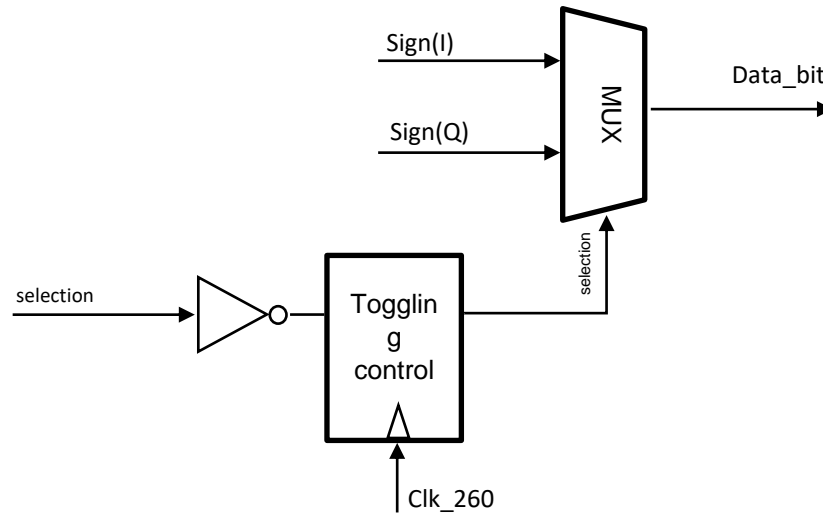


Figure [82]: Demodulator Detailed Hardware

### 3.12.3. Results

All the upcoming MATLAB results are for a transport block size of 24 bits that consists of 12 bits of zeros and 12 bits of ones.

#### 3.12.3.1. MATLAB vs. RTL

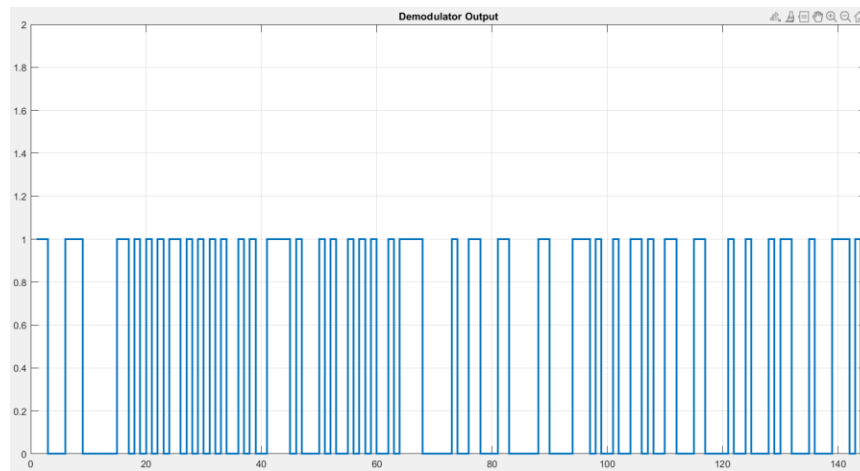


Figure [83]: Demodulator MATLAB Results



Figure [84]: Demodulator RTL Results

### 3.12.3.2. Synthesis Results

<b>Utilization</b>		<b>Post-Synthesis</b>   Post-Implementation	
		Graph   <b>Table</b>	
Resource	Estimation	Available	Utilization %
LUT	2	230400	0.01
FF	1	460800	0.01
IO	7	360	1.94
BUFG	1	544	0.18

Figure [85]: Demodulator Synthesis Results

### 3.13. Descrambler

#### 3.13.1. Top Module

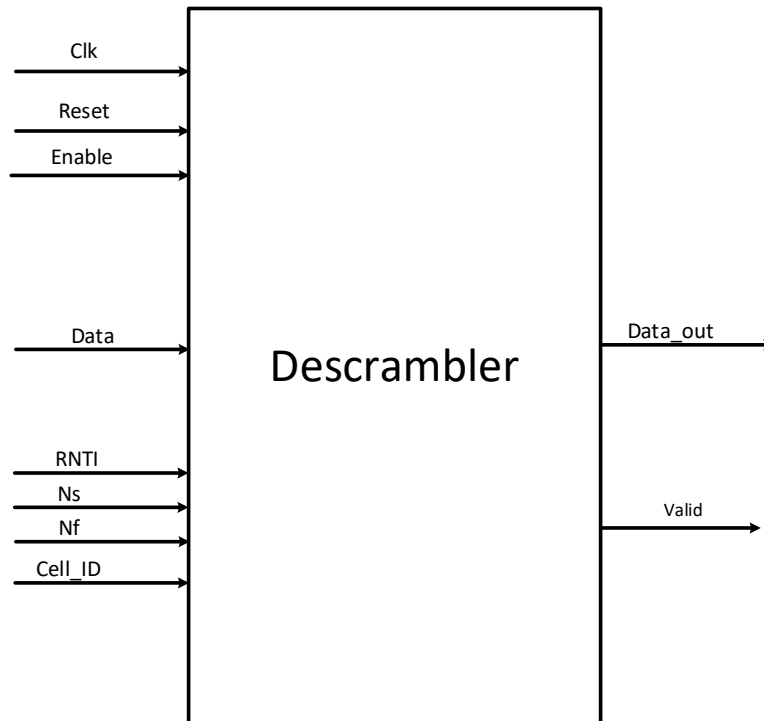


Figure [86]: Descrambler Top Module

Table [22]: Descrambler Interface Table

Signal Name	Direction	Width	Description
Clk_260	Input	1	3.84 MHz clock signal
Reset	Input	1	Global reset signal
Enable	Input	1	Enable signal for the Scrambler module to start operating
Data	Input	1	Serial input data bits from demodulator
RNTI	Input	16	Radio Network Temporary Identifier which is an upper layer parameter
Ns	Input	5	First slot of transmission
Nf	Input	1	First frame of transmission

Nsf	Input	4	Number of subframes used in codeword
Nrep	Input	12	Number of repetitions used in codeword
Cell_ID	Input	9	The Cell Identifier which is an upper layer parameter
Data_out	Output	1	Serial output data bits to the rate matcher
Valid	Output	1	signal that verifies the integrity of the output bus data

3.13.2. Detailed Hardware

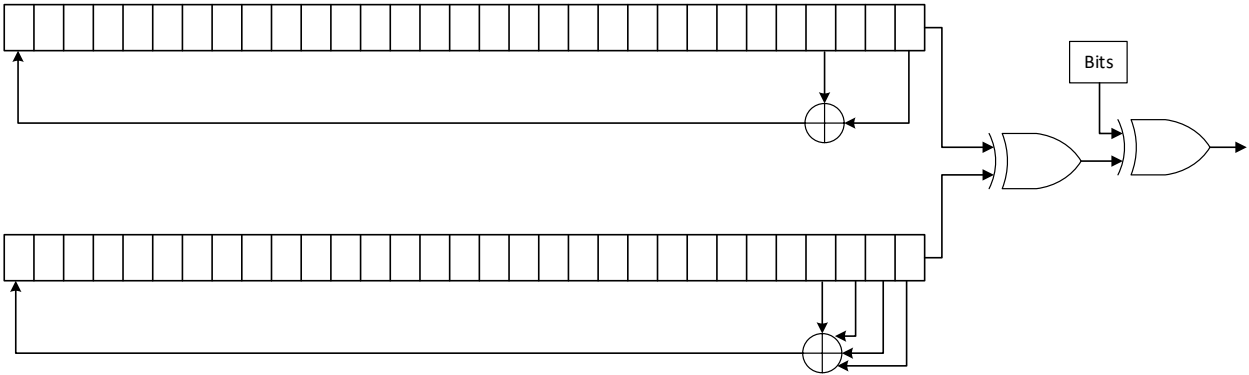


Figure [87]: Descrambler Detailed Design

**Description:** The two linear feedback shift registers are initialized with their values and then they take 1600 clock cycle to reach the desired golden sequence than should be XOR-ed with the input bitstream, until it finishes the received codeword from the demodulator. the codeword that is successive repetitions of the codeword subframes.

The linear feedback shift registers are re-initialized every  $\min(N_{rep}, 4)$  transmissions of the codeword.

### 3.13.3. Results

TBS = 24,  $N_{ID}^{cell} = 1$ ,  $n_f = 20$ ,  $n_s = 0$ ,  $n_{RNTI} = 1000$

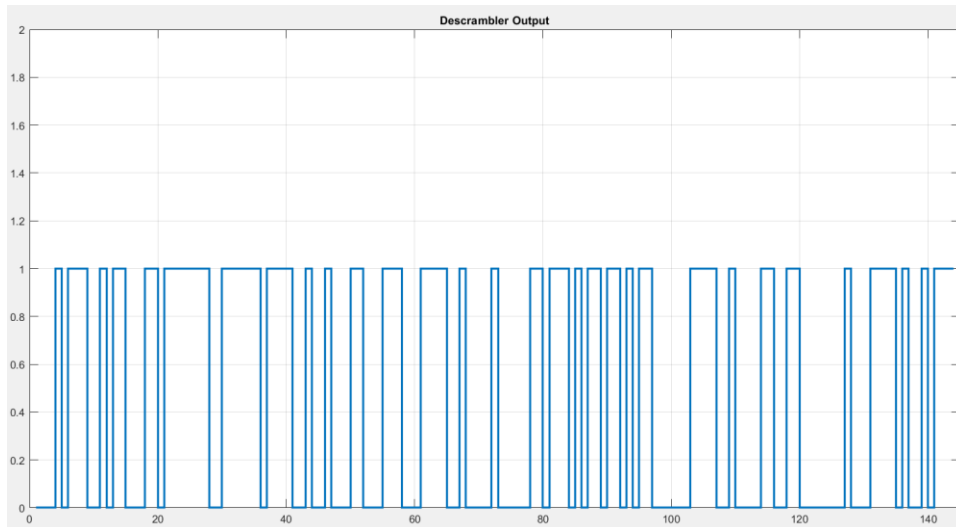


Figure [88]: Descrambler MATLAB Results



Figure [89]: Descrambler RTL Results

Utilization	Post-Synthesis   Post-Implementation		
	Estimation	Available	Utilization %
LUT	71	230400	0.03
FF	94	460800	0.02
IO	53	360	14.72
BUFG	1	544	0.18

Figure [90]: Descrambler Synthesis Results

### 3.14. Rate De-Matcher

#### 3.14.1. Top Module

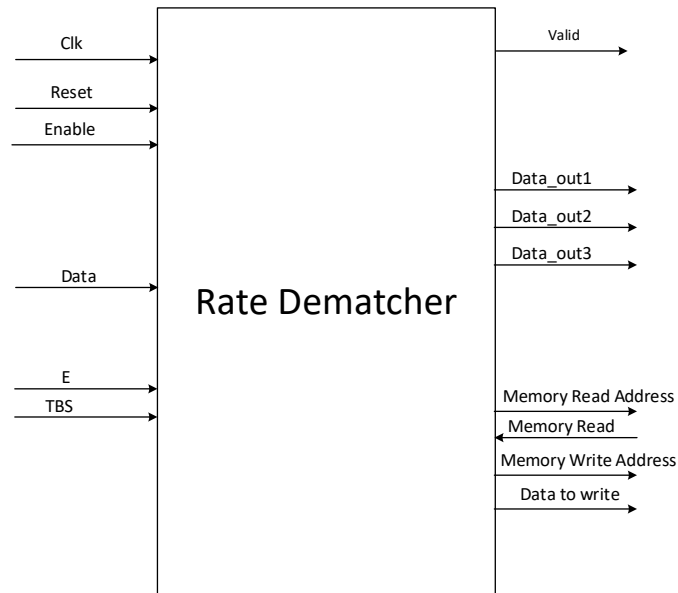


Figure [79]: Rate Dematcher Top Module

Table [23]: Rate De-Matcher Interface Table

Signal Name	Direction	Width	Description
Clk_260	Input	1	3.84 MHz clock signal
Clk_130	Input	1	7.69 MHz clock signal
Reset	Input	1	Global reset signal
Enable	Input	1	Enable signal for the Rate De-matcher.
Data	Input	1	Serial input data bits from Descrambler.
E	Input	24	Size of the input data to the Block.
TBS	Input	12	Transport Block Size of the incoming data
Matcher_repeat	Input	1	If decode didn't decode correctly at first trial
Data_out1	Output	1	First output to decoder
Data_out2	Output	1	Second output to decoder
Data_out3	Output	1	Third output to decoder
Valid	Output	1	signal that verifies the integrity of the output bus data

## 3.14.2. Detailed Hardware

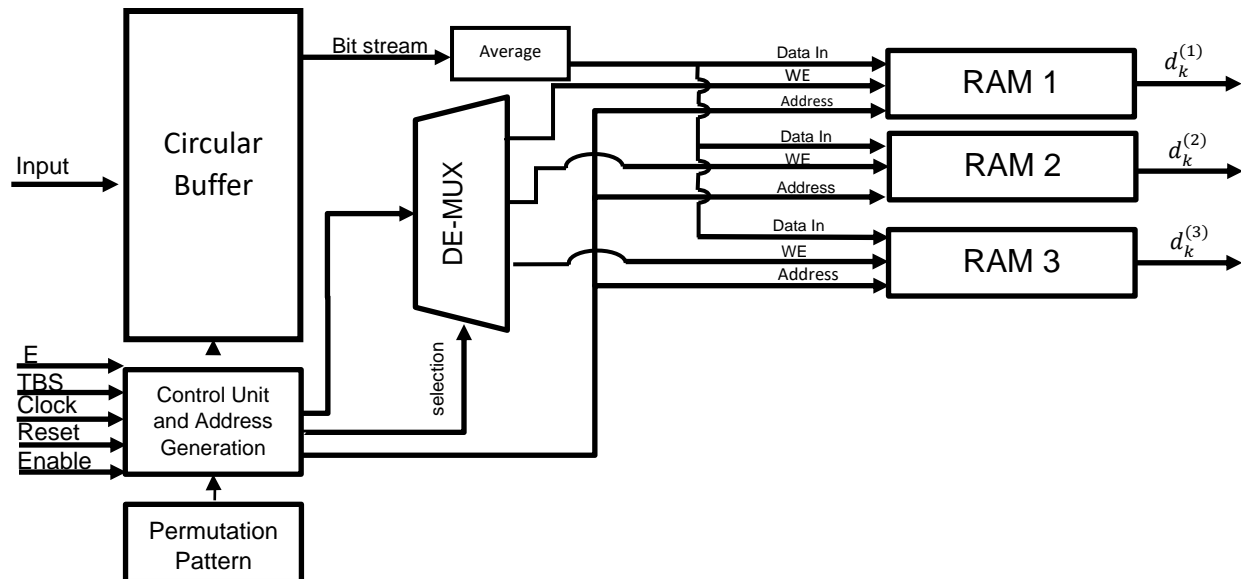


Figure [80]: Rate De-Matcher Detailed Design

**Description:**

- The input data is collected at the bit collecting memory whenever there's an enable signal high which indicates that the input from the descrambler is valid.
- Bits are written to the first memory until reach the circular buffer length. If the incoming stream is not over, the write pointer rolls over to the start of the circular buffer again to read the memory content and add the incoming input stream to them.
- when from the input data length E is received, bit collection memory output is averaged by dividing them by the number of repetitions and taking the majority vote.
- The data after majority vote is stored in each RAM each at a time, and the inter-column permutation matrix is performed by changing the address using the control unit.
- The control unit generated the addresses based on the ROM storing the intercolumn permutation pattern. And it also generates the write enable for each memory
- when the 3 RAMs are filled, they are read each row at a time without the dummy bits and the output is given to the decoder.

The Rate De-matcher control unit executes the following state machines in order to perform the block operations correctly without interfering with the reception of the next transport block as the reception is continuous in time. So, to handle this the control unit is built as two separate finite state machines that once the first one finishes it triggers the operation of the second state machine which perform the interleaving process and the output.

Address generation unit handles the three RAMs filling in order to account for the first  $N_D$  dummy bits and then store data at the right locations. Memory unrolling is performed in order to make the memory easier with only one address decoder instead of two row and column decoders.

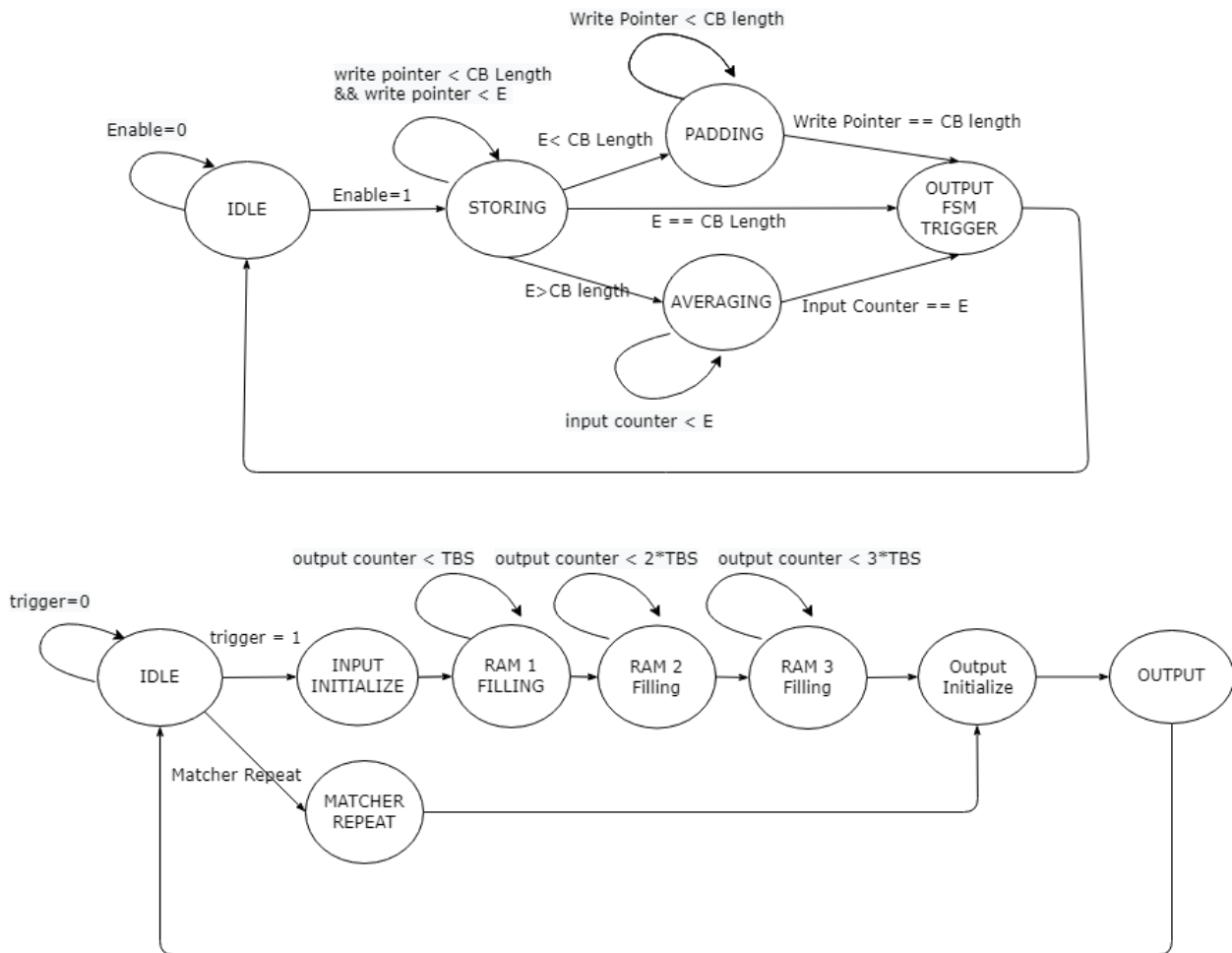


Figure [91]: Rate De-Matcher Control Finite State Machines



### 3.14.3. Design Challenges and Solutions

The block's first memory in the bit collecting stage cannot stop for the time interval that the three rams are being filled as the received subframes are continuous in time and every new subframe has data that propagates down the chain and needs to be stored correctly. In order to fix this the first memory has to be a dual port memory so the reading and writing processes are decoupled from each other. The first port is read/write port and the second port is a read only port.

A new problem arises from this implementation that in case of repetitions the memory has to read first the memory content and then add the incoming input to the stored value so for this to happen the first port has to operate at twice the frequency of the block with flock clock of 130 nsec. This solution was chosen because this new clock as already generated and used in our system chain at different other blocks so no overhead would appear from such scenario

### 3.14.4. Results

#### 3.14.4.1. MATLAB v. RTL

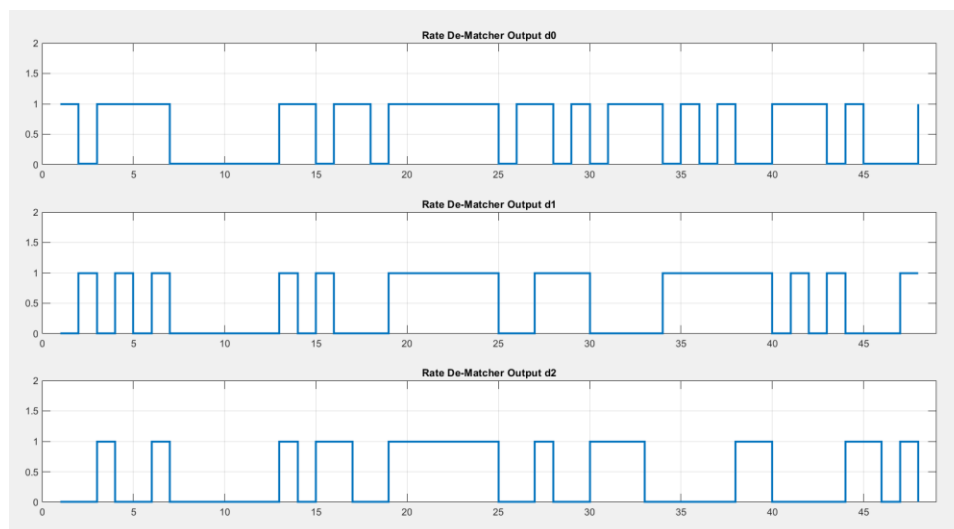


Figure [92]: Rate De-Matcher MATLAB Results



Figure [93]: Rate De-Matcher RTL Results

### 3.14.4.2. Synthesis Results

<b>Utilization</b>		<b>Post-Synthesis</b>   Post-Implementation	
		Graph   <b>Table</b>	
Resource	Estimation	Available	Utilization %
LUT	479	230400	0.21
FF	267	460800	0.06
BRAM	4.50	312	1.44
IO	46	360	12.78
BUFG	2	544	0.37

Figure [94]: Rate De-Matcher Synthesis Results

### 3.15. Viterbi Decoder

#### 3.15.1. Block Interface

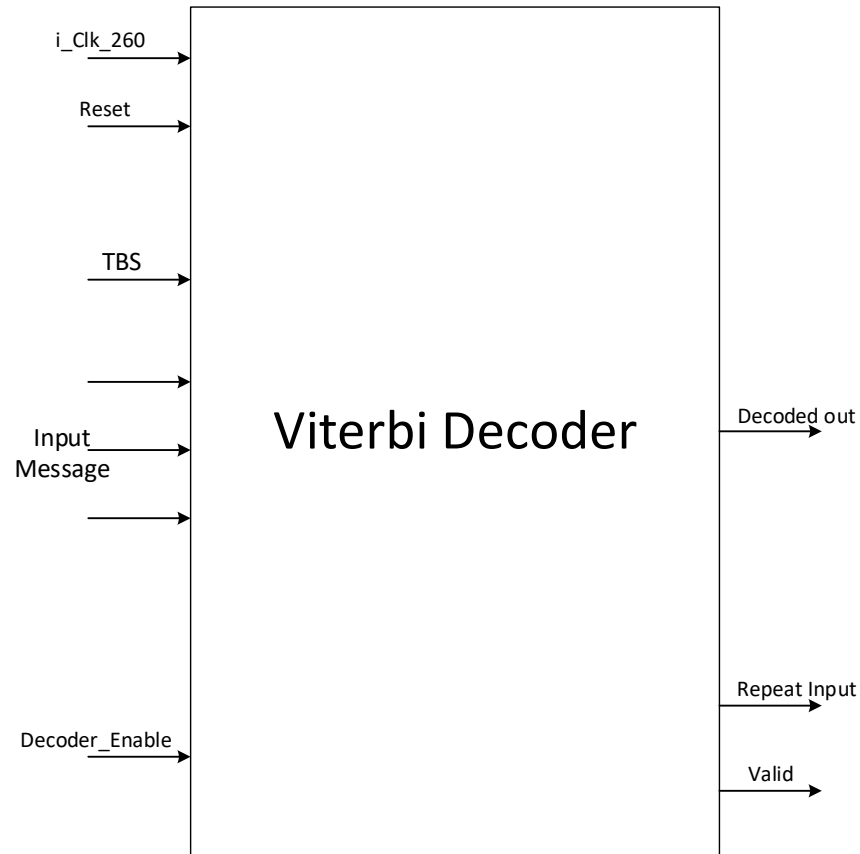


Figure [95]: Decoder Interface

Table [24]: Decoder Interface Table

Signal Name	Direction	Width	Description
Clk	Input	1	Clock signal to the block (260ns)
Reset	Input	1	Reset signal to the block
TBS	Input	12	Transport Block Size
Input Message	Input	3	Inputs divided to 3 parallel bits
Decoder_Enable	Input	1	Signal to enable the decoder
Decoded_out	Output	1	Output serial decoded bits
Valid	Output	1	Valid signal to next block
Repeat_Input	Output	1	Signal to previous block to repeat the input for another iteration

### 3.15.2. Detailed Hardware

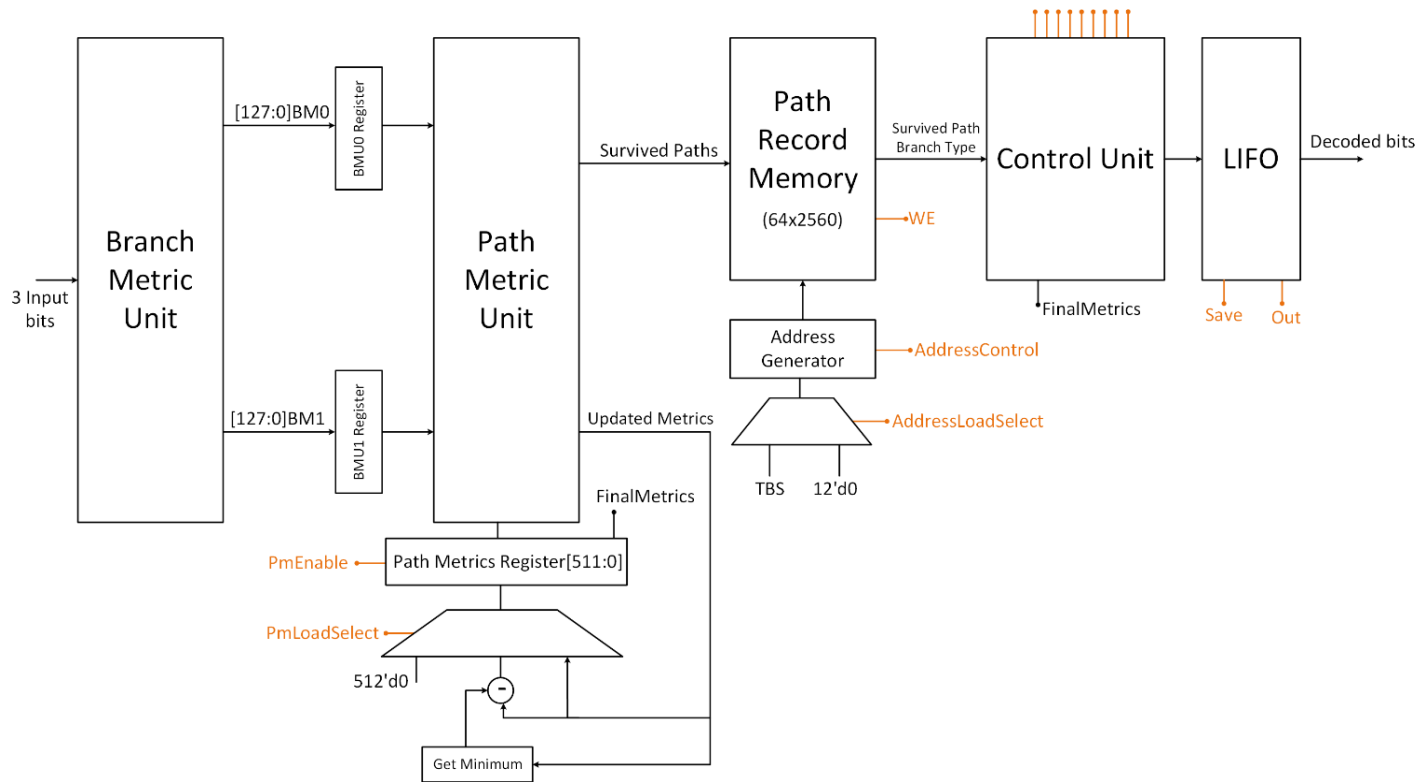


Figure [96]: Detailed hardware of the decoder

#### 3.15.2.1. Branch Metric Unit (BMU)

This block is responsible for calculating the hamming distance between the input 3 bits and the expected outputs from all branches in the trellis diagram. Every state has two output branches as shown in the figure. This means that we need 128 Hamming Distance Units for 64 states.

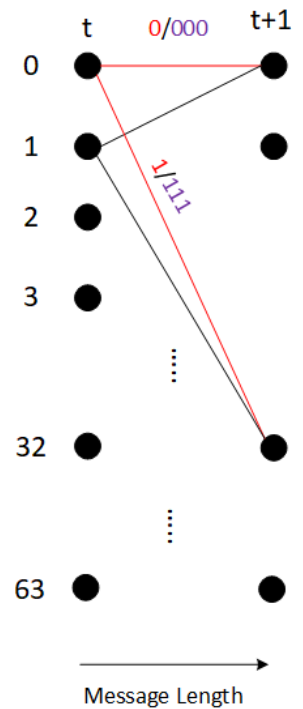


Figure [97]: Trellis Diagram

3.15.2.2. Path Metric Unit (PMU)

This block contains Add-Compare-Select units that work in this following flow:

1. Add the branch metrics to the saved path metrics.
2. Compares the two input paths to the next states.
3. Selects the path with higher metric.
4. Accumulates this metric in the path metrics memory.
5. Saves the selected path (high or low branch) in the path record memory.

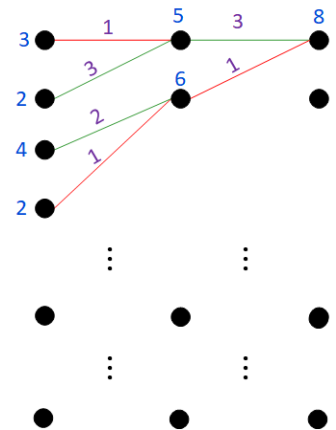


Figure [98]: Example of Path Metric Unit operation

In the shown figure, we can see an example of the path metric unit operation. The example shows that there's two different paths that are entering the same next state. The key to differentiate between them is to compare the path metrics of them after adding the new branch metrics to the path metrics then selecting the path that has the larger metric to be our survived path in this state. For this example, at the left side, we can see that the survived path that enters the first state is the path that has all green branches.

3.15.2.3. Path Record Memory

This block is a memory that saves the transitions in each state and used in the traceback unit. The size of the memory is 64x2560 bits as we need to store the condition of the branch entering the state whether it's the upper branch (0 is stored) or the lower branch (1 is stored). The encoding of the stored values will be elaborated in the next section.

3.15.2.4. Control Unit

It controls the entire operation of the decoding algorithm using a finite state machine that has these operations:

- Manages the calculation and saving of the survived paths in the path record memory.
- Performs the traceback operation by evaluating the winning path and reading from the path record memory.
- Checking the Tailbiting condition and controls the output flow from the LIFO memory.
- Performs the Wrap Around Viterbi Algorithm (WAVA) elaborated before.

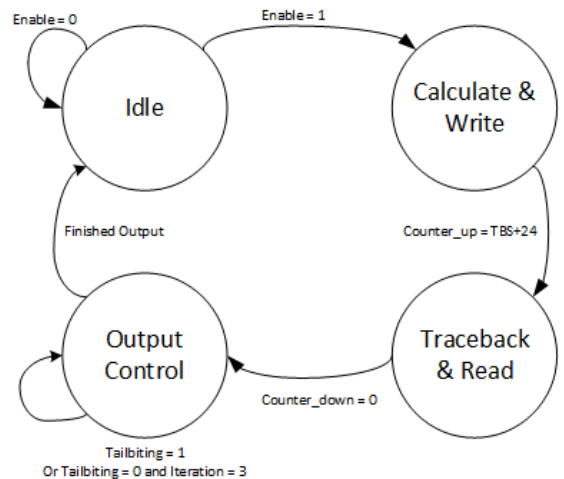


Figure [99]: Finite State Machine implemented in the control unit

### 3.15.2.5. LIFO Memory

A LIFO Memory of size (1x2560) is implemented to store the decoded bits from the traceback operation. Last-In-First-Out mechanism is required as the traceback operation starts from the last bit of the message to the start bit of the message.

## 3.15.3. Hardware Challenges and Solutions

### 3.15.3.1. Path Metrics are Monotonically Increasing

As the decoder proceeds in the trellis structure, the path metrics are being accumulated due to the Add-Compare-Select (ACS) operation. Moreover, the values are monotonically increasing as the branch metrics are positive values from 0 to 3. Also, given the fixed size of the path metrics registers (8 bits), these registers will overflow and the decoder will not operate correctly.

To avoid the overflow of these registers, in the shown figure, a simple hardware that is controlled by the control unit is added to subtract the minimum value stored in these registers occasionally before the overflow occurs. This avoids the overflow problem and also will not affect the operation as it only cares about the relation between the path metrics not the actual values of them.

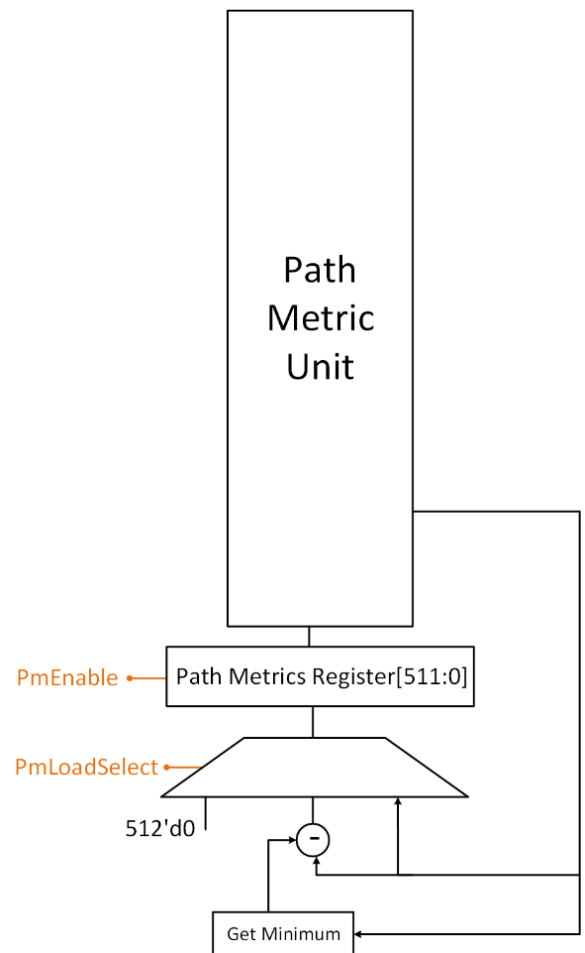


Figure [100]: Hardware added to avoid overflow

3.15.3.2. Path Record Memory Size

Traceback operation is done by knowing the branch and the two states connected to it in order to find the actual decoded bit and to go to the previous state. These parameters can be calculated in the first stages but they need to be stored as the traceback operation must start from the end of the message to the start of it. We can calculate the size of the memory using:

$$Memory\ Size = n_{states} * \log_2 n_{states} * message\ length$$

In our case, the memory size will approximately be 983,040 bits. This is a very large memory to be implemented. To reduce this size, a better traceback implementation is done that only encodes all the parameters said before to a single bit that tells whether the branch that is connecting the two states together is an upper or lower branch then with a simple left shift operation, we can figure out the previous state simply as shown in the figure.

The figure shows an example of the used traceback operation method where the current state is 23 and the previous state is required to complete tracing back to the initial state. The available two previous states are 46 and 47 only according to the trellis diagram of the encoder. The control unit reads the bit stored in the location of the path record memory that is [t+1][23] and then performs a shift left operation to the current value 23 then finally adds the stored bit read from the memory. If the saved bit was 0', the previous state will be 46. And if the saved bit was 1', the previous state will be 47. In conclusion, by saving only one bit, we could perform the traceback operation correctly without having a very large memory.

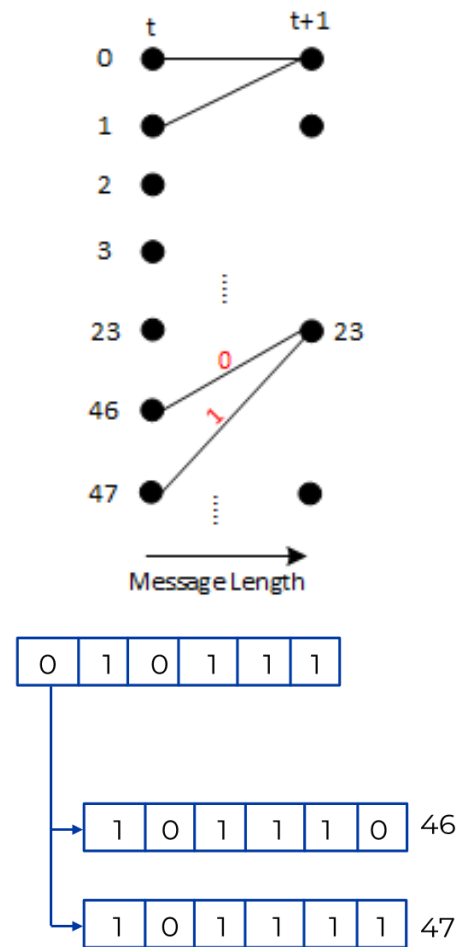


Figure [101]: Another implementation of traceback operation to reduce memory size

### 3.15.4. MATLAB Results

High Level Implementation of the algorithm was done on MATLAB and was tested with a random vector with the maximum transport block size (2560). The figure below shows the different error counts against different SNR values.

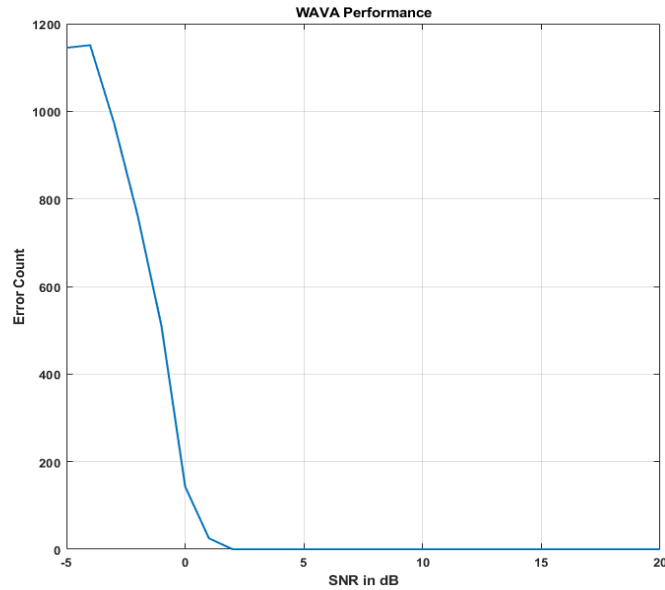


Figure [102]: MATLAB Implementation of WAVA Results

### 3.15.5. Synthesis Results

The Figure below shows the overall synthesized area in FPGA cells on the targeted FPGA. Synthesis is done using Vivado Design Suite which includes block's utilization in resources (LUTs, FFs, DSPs, etc.)

Resource	Estimation	Available	Utilization %
LUT	4571	53200	8.59
FF	615	106400	0.58
BRAM	8	140	5.71
IO	21	200	10.50
BUFG	1	32	3.13

Figure [103]: Viterbi Decoder Synthesis Utilization



## 3.16. Cyclic Redundancy Check

### 3.16.1. Top Module

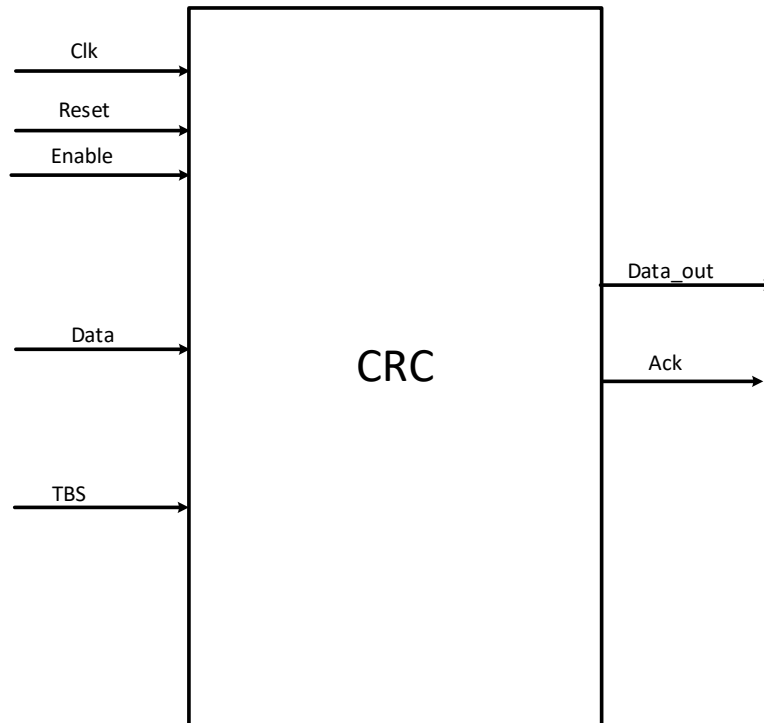


Figure [104]: CRC Top Module

Table [25]: CRC Interface Table

Signal Name	Direction	Width	Description
Clk_260	Input	1	3.84 MHz clock signal
Reset	Input	1	Global reset signal
Enable	Input	1	Enable signal for the Demodulator module to start operating
Data	Input	1	Data received from the decoder
TBS	Input	12	Transport Block Size of the incoming data
Data_out	Output	1	Serial data bits output
Ack	Output	1	Ack to indicate data validity

### 3.16.2. Detailed Hardware

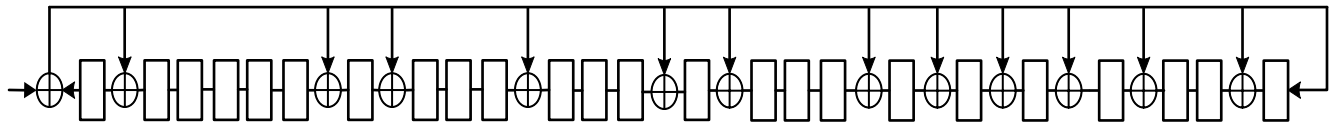


Figure [105]: CRC Detailed Design

#### Description:

The CRC value is generated by XORing the input bit with the value of the final register and the result is used as feedback to all the XORs implementing the polynomial. This implementation reduces the number of cycles taken to perform the check.

The Register at first is initialized to 0 then after passing the received data bitstream of length equal TBS+ 24 bits CRC the register should contain Zeros once again and that's when the acknowledge signal is asserted.

### 3.16.3. Results

#### 3.16.3.1. MATLAB vs. RTL

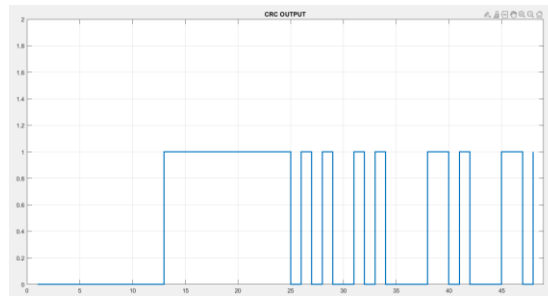


Figure [106]: CRC MATLAB Results



Figure [107]: CRC RTL Results

#### 3.16.3.2. Synthesis Results

Utilization	Post-Synthesis   Post-Implementation		
	Estimation	Available	Utilization %
LUT	35	64000	0.05
FF	38	128000	0.03
IO	18	400	4.50
BUFG	1	32	3.13

Figure [108]: CRC Synthesis Results

## 4.1. Synopsys Design Compiler Synthesis Results

### 4.1.1. Coarse Synchronizer

#### 4.1.1.1. Area Results

```

38 Cell Count
39 -----
40 Hierarchical Cell Count:      296
41 Hierarchical Port Count:     20302
42 Leaf Cell Count:             64753
43 Buf/Inv Cell Count:          9328
44 CT Buf/Inv Cell Count:        0
45 Combinational Cell Count:    58963
46 Sequential Cell Count:       5790
47 Macro Count:                  0
48 -----
49
50
51 Area
52 -----
53 Combinational Area:   108330.628376
54 Noncombinational Area: 27328.041517
55 Buf/Inv Area:        6164.017928
56 Net Area:            0.000000
57 -----
58 Cell Area:           135658.669893
59 Design Area:        135658.669893

```

Figure [109]: Coarse Synchronizer DC Area Results

#### 4.1.1.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	40.2665	33.8177	3.2332e+04	106.4160	( 12.15%)	
register	144.2135	0.1875	1.0016e+05	244.5638	( 27.92%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	66.1815	81.5036	3.7729e+05	524.9745	( 59.93%)	
<b>Total</b>	<b>250.6615 uW</b>	<b>115.5088 uW</b>	<b>5.0979e+05 nW</b>	<b>875.9543 uW</b>		

Figure [110]: Coarse Synchronizer DC Power Results

## 4.1.2. CP Remover and Downsampler

### 4.1.2.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      1
27 Hierarchical Port Count:     16
28 Leaf Cell Count:             159
29 Buf/Inv Cell Count:          19
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:     138
32 Sequential Cell Count:        21
33 Macro Count:                  0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:           158.536001
40 Noncombinational Area:        111.720004
41 Buf/Inv Area:                 10.108000
42 Net Area:                      0.000000
43 -----
44 Cell Area:                     270.256005
45 Design Area:                   270.256005

```

Figure [111]: CP Remover and Downsampler DC Area Results

### 4.1.2.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
sequential	8.2474	0.9466	371.2713	9.5652	( 56.55%)	
combinational	2.8438	3.6286	876.8418	7.3492	( 43.45%)	
<b>Total</b>	<b>11.0912 uW</b>	<b>4.5752 uW</b>	<b>1.2481e+03 nW</b>	<b>16.9145 uW</b>		

Figure [112]: CP Remover and Downsampler DC Power Results

## 4.1.3. CFO Corrector

## 4.1.3.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      20
27 Hierarchical Port Count:     1221
28 Leaf Cell Count:             3401
29 Buf/Inv Cell Count:          342
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:     3289
32 Sequential Cell Count:        112
33 Macro Count:                  0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:           6419.112010
40 Noncombinational Area:        595.840019
41 Buf/Inv Area:                 191.786001
42 Net Area:                      0.000000
43 -----
44 Cell Area:                     7014.952029
45 Design Area:                   7014.952029

```

Figure [113]: CFO Corrector DC Area Results

## 4.1.3.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
sequential	47.9756	5.0920	2.0349e+03	55.1025	( 25.15%)	
combinational	74.4077	63.9070	2.5655e+04	163.9699	( 74.85%)	
Total	122.3833 uW	68.9990 uW	2.7690e+04 nW	219.0724 uW		

Figure [114]: CFO Corrector DC Power Results

#### 4.1.4. FFT Engine

##### 4.1.4.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      33
27 Hierarchical Port Count:     1956
28 Leaf Cell Count:             5326
29 Buf/Inv Cell Count:          658
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:    4686
32 Sequential Cell Count:       640
33 Macro Count:                 0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:          8883.602024
40 Noncombinational Area:      2926.797905
41 Buf/Inv Area:               365.484002
42 Net Area:                   0.000000
43 -----
44 Cell Area:                   11810.399929
45 Design Area:                 11810.399929

```

Figure [115]: FFT Engine DC Area Results

##### 4.1.4.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
sequential	170.2249	14.3775	1.0827e+04	195.4299	( 37.58%)	
combinational	114.4933	174.1690	3.5901e+04	324.5651	( 62.42%)	
Total	284.7182 uW	188.5465 uW	4.6728e+04 nW	519.9951 uW		

Figure [116]: FFT Engine DC Power Results

## 4.1.5. Resource Demapper

## 4.1.5.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:          2
27 Hierarchical Port Count:         1366
28 Leaf Cell Count:                  52845
29 Buf/Inv Cell Count:               14861
30 CT Buf/Inv Cell Count:            0
31 Combinational Cell Count:         41689
32 Sequential Cell Count:            11156
33 Macro Count:                      0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:                53577.188558
40 Noncombinational Area:            59040.031784
41 Buf/Inv Area:                     10611.803801
42 Net Area:                          0.000000
43 -----
44 Cell Area:                         112617.220342
45 Design Area:                       112617.220342
46

```

Figure [117]: Resource Demapper Area report

## 4.1.5.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	223.0984	0.1518	1.9729e+05	420.5371	( 55.85%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	3.2476	13.8096	3.1540e+05	332.4582	( 44.15%)	
Total	226.3460 uW	13.9614 uW	5.1269e+05 nW	752.9954 uW		

Figure [118]: Resource Demapper Power report

## 4.1.6. Channel Estimation

### 4.1.6.1. Area Results

```
24 Cell Count
25 -----
26 Hierarchical Cell Count:      91
27 Hierarchical Port Count:     6129
28 Leaf Cell Count:             9681
29 Buf/Inv Cell Count:          1526
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:     9513
32 Sequential Cell Count:        168
33 Macro Count:                  0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:    18878.020079
40 Noncombinational Area: 893.760029
41 Buf/Inv Area:          903.069999
42 Net Area:              0.000000
43 -----
44 Cell Area:             19771.780108
45 Design Area:          19771.780108
46
```

Figure [119]: Channel Estimation Area report

### 4.1.6.2. Power Results

45		Internal	Switching	Leakage	Total			
46	Power Group	Power	Power	Power	Power	(	%	) Attrs
47								
48	io_pad	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
49	memory	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
50	black_box	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
51	clock_network	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
52	register	1.6089	0.1219	3.0614e+03	4.7923	(	5.51%	)
53	sequential	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
54	combinational	3.1737	3.1101	7.5868e+04	82.1514	(	94.49%	)
55								
56	Total	4.7826 uW	3.2320 uW	7.8929e+04 nW	86.9436 uW			
57	1							

Figure [120]: Channel Estimation Power report



## 4.1.7. NRS Values Generator

## 4.1.7.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      5
27 Hierarchical Port Count:     304
28 Leaf Cell Count:             2207
29 Buf/Inv Cell Count:          241
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:    1874
32 Sequential Cell Count:       333
33 Macro Count:                  0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:           2703.091985
40 Noncombinational Area:       1799.490056
41 Buf/Inv Area:                 173.165997
42 Net Area:                      0.000000
43 -----
44 Cell Area:                     4502.582040
45 Design Area:                   4502.582040
46

```

Figure [121]: NRS Values Generator Area report

## 4.1.7.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	14.0364	5.1099e-02	5.6948e+03	19.7823	( 56.59%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	0.7627	1.6479	1.2767e+04	15.1777	( 43.41%)	
Total	14.7991 uW	1.6990 uW	1.8462e+04 nW	34.9600 uW		

Figure [122]: NRS Values Generator Power report

## 4.1.8. NRS Index Generator

### 4.1.8.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:          2
27 Hierarchical Port Count:         52
28 Leaf Cell Count:                 113
29 Buf/Inv Cell Count:              13
30 CT Buf/Inv Cell Count:           0
31 Combinational Cell Count:        93
32 Sequential Cell Count:           20
33 Macro Count:                     0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:              109.325999
40 Noncombinational Area:          106.400003
41 Buf/Inv Area:                   7.182000
42 Net Area:                        0.000000
43 -----
44 Cell Area:                       215.726003
45 Design Area:                     215.726003
46

```

Figure [123]: NRS Index Generator Area report

### 4.1.8.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	0.2137	1.2599e-02	349.6761	0.5760	( 47.60%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	1.7619e-02	2.3247e-02	593.1061	0.6340	( 52.40%)	
Total	0.2313 uW	3.5846e-02 uW	942.7822 nW	1.2100 uW		

Figure [124]: NRS Index Generator Power report

## 4.1.9. Channel Equalizer

### 4.1.9.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      132
27 Hierarchical Port Count:     9888
28 Leaf Cell Count:             30919
29 Buf/Inv Cell Count:          2866
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:    30886
32 Sequential Cell Count:        33
33 Macro Count:                  0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:      61535.642101
40 Noncombinational Area:  175.560006
41 Buf/Inv Area:           1605.310007
42 Net Area:                0.000000
43 -----
44 Cell Area:                61711.202107
45 Design Area:              61711.202107
46

```

Figure [125]: Channel Equalizer Area report

### 4.1.9.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	0.3335	2.6553e-03	589.7083	0.9258	( 0.28%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	42.4840	34.2846	2.4959e+05	326.3558	( 99.72%)	
<b>Total</b>	<b>42.8175 uW</b>	<b>34.2872 uW</b>	<b>2.5018e+05 nW</b>	<b>327.2816 uW</b>		

Figure [126]: Channel Equalizer Power report

## 4.1.10. Parallel to Serial and NRS removal

### 4.1.10.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:          0
27 Hierarchical Port Count:         0
28 Leaf Cell Count:                 196
29 Buf/Inv Cell Count:              43
30 CT Buf/Inv Cell Count:           0
31 Combinational Cell Count:        177
32 Sequential Cell Count:           19
33 Macro Count:                     0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:               211.736000
40 Noncombinational Area:           95.494001
41 Buf/Inv Area:                    23.142000
42 Net Area:                         0.000000
43 -----
44 Cell Area:                        307.230001
45 Design Area:                     307.230001
46

```

Figure [127]: Parallel to Serial and NRS removal Area report

### 4.1.10.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	0.1828	2.4141e-02	330.8464	0.5378	( 30.30%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	6.5207e-02	4.2960e-02	1.1291e+03	1.2372	( 69.70%)	
Total	0.2480 uW	6.7101e-02 uW	1.4599e+03 nW	1.7750 uW		

Figure [128]: Parallel to Serial and NRS removal Power report

## 4.1.11. Fine Synchronizer

## 4.1.11.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      45
27 Hierarchical Port Count:     3363
28 Leaf Cell Count:             8948
29 Buf/Inv Cell Count:          931
30 CT Buf/Inv Cell Count:       0
31 Combinational Cell Count:    8738
32 Sequential Cell Count:       210
33 Macro Count:                 0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:          17132.794030
40 Noncombinational Area:      1117.200036
41 Buf/Inv Area:               528.542002
42 Net Area:                   0.000000
43 -----
44 Cell Area:                   18249.994066
45 Design Area:                 18249.994066
46

```

Figure [129]: Fine Synchronization Area Report

## 4.1.11.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	4.2890	0.2169	3.7918e+03	8.2977	( 9.39%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	4.8291	5.1848	7.0050e+04	80.0642	( 90.61%)	
Total	9.1181 uW	5.4017 uW	7.3842e+04 nW	88.3618 uW		

Figure [130]: Fine Synchronization Power Report

## 4.1.12. Demodulator

### 4.1.12.1. Area Results

24	Cell Count	
25	-----	
26	Hierarchical Cell Count:	0
27	Hierarchical Port Count:	0
28	Leaf Cell Count:	5
29	Buf/Inv Cell Count:	2
30	CT Buf/Inv Cell Count:	0
31	Combinational Cell Count:	4
32	Sequential Cell Count:	1
33	Macro Count:	0
34	-----	
35		
36		
37	Area	
38	-----	
39	Combinational Area:	4.256000
40	Noncombinational Area:	5.320000
41	Buf/Inv Area:	1.330000
42	Net Area:	0.000000
43	-----	
44	Cell Area:	9.576000
45	Design Area:	9.576000
46		

Figure [131]: Demodulator Area Report

### 4.1.12.2. Power Results

45		Internal	Switching	Leakage	Total			
46	Power Group	Power	Power	Power	Power	(	%	) Attrs
47	-----							
48	io_pad	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
49	memory	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
50	black_box	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
51	clock_network	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
52	register	2.6281e-02	3.0077e-03	18.8780	4.8166e-02	(	62.66%	)
53	sequential	0.0000	0.0000	0.0000	0.0000	(	0.00%	)
54	combinational	5.7401e-03	1.7533e-03	21.2143	2.8708e-02	(	37.34%	)
55	-----							
56	Total	3.2021e-02 uW	4.7610e-03 uW	40.0922 nW	7.6874e-02 uW			
57	1							

Figure [132]: Demodulator Power Report

## 4.1.13. Descrambler

## 4.1.13.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      1
27 Hierarchical Port Count:     22
28 Leaf Cell Count:             344
29 Buf/Inv Cell Count:          43
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:    249
32 Sequential Cell Count:       95
33 Macro Count:                  0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:          298.718000
40 Noncombinational Area:      500.080016
41 Buf/Inv Area:                28.196000
42 Net Area:                     0.000000
43 -----
44 Cell Area:                    798.798016
45 Design Area:                  798.798016
46

```

Figure [133]: Descrambler Area Report

## 4.1.13.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	1.9440	5.8881e-02	1.6997e+03	3.7026	( 61.22%)	
sequential	1.9461e-03	4.0243e-03	17.1607	2.3131e-02	( 0.38%)	
combinational	0.1122	0.1356	2.0746e+03	2.3224	( 38.40%)	
Total	2.0582 uW	0.1985 uW	3.7915e+03 nW	6.0481 uW		

Figure [134]: Descrambler Power Report







## 4.1.16. Cyclic Redundance Check

### 4.1.16.1. Area Results

```

24 Cell Count
25 -----
26 Hierarchical Cell Count:      1
27 Hierarchical Port Count:     24
28 Leaf Cell Count:             169
29 Buf/Inv Cell Count:          34
30 CT Buf/Inv Cell Count:        0
31 Combinational Cell Count:    131
32 Sequential Cell Count:       38
33 Macro Count:                  0
34 -----
35
36
37 Area
38 -----
39 Combinational Area:           171.836002
40 Noncombinational Area:       202.160007
41 Buf/Inv Area:                19.418000
42 Net Area:                     0.000000
43 -----
44 Cell Area:                    373.996008
45 Design Area:                  373.996008
46

```

Figure [139]: CRC Area Report

### 4.1.16.2. Power Results

Power Group	Internal Power	Switching Power	Leakage Power	Total Power	( % )	Attrs
io_pad	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
memory	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
black_box	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
clock_network	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
register	0.7795	3.8260e-02	693.2999	1.5111	( 55.58%)	
sequential	0.0000	0.0000	0.0000	0.0000	( 0.00%)	
combinational	7.6499e-02	9.0566e-02	1.0404e+03	1.2075	( 44.42%)	
Total	0.8560 uW	0.1288 uW	1.7337e+03 nW	2.7186 uW		

Figure [140]: CRC Power Report

## 4.2. DC Results for RX Chain

### 4.2.1. Timing

```

1 *****
2 Report : timing
3     -path full
4     -delay max
5     -max_paths 10
6 Design : rx_top
7 Version: G-2012.06-SP2
8 Date   : Wed Jul 12 21:33:50 2022
9 *****
10 -----
11 | Design Timing Summary
12 | -----
13 -----
14
15      WNS(ns)      TNS(ns)  TNS Failing Endpoints  TNS Total Endpoints      WHS(ns)      THS(ns)
16      -----      -----
17      21.643        0.000                0                29814            0.044        0.000
18
19
20 All user specified timing constraints are met.

```

Figure [141]: Timing Report

All specified timing constraints have been met with total available slack of **21.643 ns**.



### 4.2.3. Power Consumption

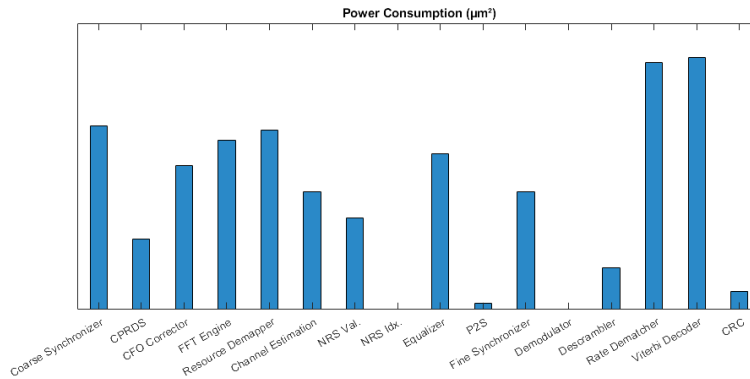


Figure [144]: Power Consumption Histogram

Table [27]: Total Power Consumption Table

Block	Total Power (µW)
Coarse Synchronizer	875.9543
CP Remover & Downsampler	16.9145
CFO Corrector	219.0724
FFT Engine	519.9951
Resource Demapper	752.9954
Channel Estimation	86.9436
NRS Value Generator	34.96
NRS Index Generator	1.21
Channel Equalizer	327.2816
Parallel to Serial	1.775
Fine Synchronizer	88.3618
Demodulator	1.05
Descrambler	6.0481
Rate Dematcher	7994.9
Viterbi Decoder	9485.6
CRC	2.7186

```

1
2 *****
3 Report : power
4       -analysis_effort low
5 Design : rx_top
6 Version: G-2012.06-SP2
7 Date   : Wed Jul 13 07:52:31 2022
8 *****
9
10
11 Power Group      Internal      Switching      Leakage      Total
12                   Power          Power          Power          Power    ( % ) Attrs
13 -----
14 io_pad            0.0000         0.0000         0.0000         0.0000 ( 0.00%)
15 memory            0.0000         0.0000         0.0000         0.0000 ( 0.00%)
16 black_box         0.0000         0.0000         0.0000         0.0000 ( 0.00%)
17 clock_network     40.2665        33.8177        3.2332e+04     106.4160 ( 0.51%)
18 register          7396.1260       3.0161         48.038e+05     12.2029e+03 ( 60.27%)
19 sequential        369.1974        21.0250        2.2530e+04     412.7523 ( 0.00%)
20 combinational     366.1195        572.6384        69.350e+05     7.8736e+03 ( 39.22%)
21 -----
22 Total             8.1718e+03 uW   630.4972 uW    11.7937e+06 nW  20.5960e+03 uW

```

Figure [145]: Total Power DC Report

**Total Power Consumption = 20596 µW**

## 4.3. FPGA Implementation Results

### Targeted FPGA: ZYNQ-7 ZC702 Evaluation Board

#### 4.3.1. Post-Implementation FPGA View

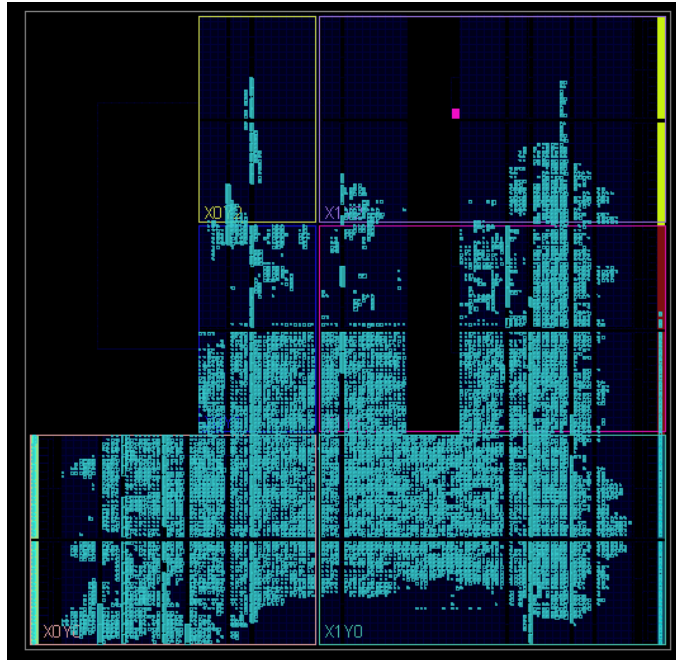


Figure [146]: Post-Implementation FPGA View

#### 4.3.2. Timing

```

1 Copyright 1986-2019 Xilinx, Inc. All Rights Reserved.
2 -----
3 | Tool Version : Vivado v.2019.1 (win64) Build 2552052 Fri May 24 14:49:42 MDT 2019
4 | Date       : Sat Jul 2 22:30:56 2022
5 | Host      : Jarvis running 64-bit major release (build 9200)
6 | Command   : report_timing_summary -max_paths 10 -file wrapper_timing_summary_routed.rpt -pb wrapper_timing_summary_routed.pb -rpx wrapper_timing_summary_routed.rpx -warn_on_violation
7 | Design    : wrapper
8 | Device    : 7z020-clg484
9 | Speed File : -1 PRODUCTION 1.11 2014-09-11
10 -----
11
12 -----
13 | Design Timing Summary
14 | -----
15
16 -----
17 | WNS(ns)    TNS(ns)    TNS Failing Endpoints    TNS Total Endpoints    WHS(ns)    THS(ns)    THS Failing Endpoints    THS Total Endpoints    WPWS(ns)    TPWS(ns)    TPWS Failing Endpoints    TPWS Total Endpoints
18 |-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
19 | 21.643     0.000             0                29814             0.044     0.000             0                29814             15.750     0.000             0                14584
20
21
22 All user specified timing constraints are met.

```

Figure [147]: Vivado Timing Report

## 4.3.3. Area Utilization

Utilization		Post-Synthesis	Post-Implementation		
Resource	Utilization	Available	Utilization %		
LUT	16893	53200	31.75		
LUTRAM	216	17400	1.24		
FF	14315	106400	13.45		
BRAM	15.50	140	11.07		
DSP	131	220	59.55		
IO	128	200	64.00		
BUFG	4	32	12.50		

Figure [148]: FPGA Area Utilization

## 4.3.4. Power Consumption:

**Summary**

Power analysis from Implemented netlist. Activity derived from constraints files, simulation files or vectorless analysis.

<b>Total On-Chip Power:</b>	<b>0.11 W</b>
<b>Design Power Budget:</b>	<b>Not Specified</b>
<b>Power Budget Margin:</b>	<b>N/A</b>
<b>Junction Temperature:</b>	<b>26.3°C</b>
Thermal Margin:	58.7°C (4.9 W)
Effective $\theta_{JA}$ :	11.5°C/W
Power supplied to off-chip devices:	0 W
Confidence level:	Low

Figure [149]: FPGA Power Consumption Summary





We assumed perfect synchronization while testing on the chain using 3 NB-IoT subframes using number of repetitions ( $N_{rep}$ ) = 2 with data transport block size (TBS) = 136. As shown in the example shown in the figure below, the CRC Ack's indicating a successfully received transport block bits.

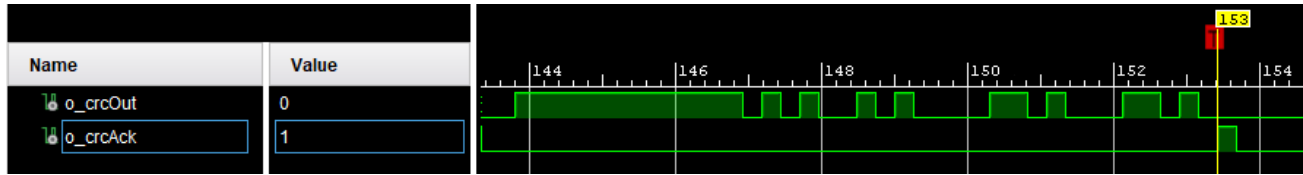


Figure [151]: RX Chain Output

We calculated receiver's performance and plotted the BER vs. SNR curve for the same  $N_{rep}$  and TBS as shown in the figure below.

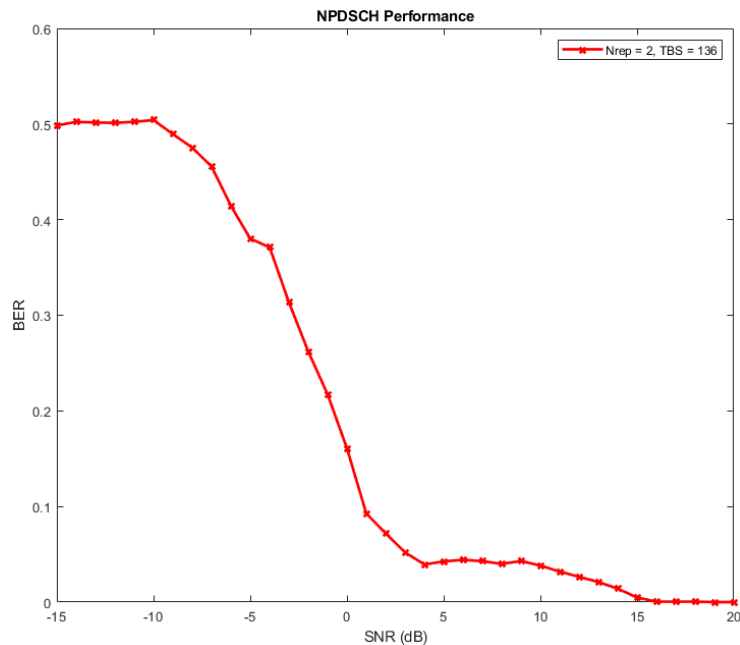


Figure [152152]: BER vs SNR Curve

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